

# CPV involving $b \rightarrow u$ transitions from BaBar and Belle

Full title and outline:

- CPV in  $B \rightarrow \pi\pi$
- measurements of  $\phi_3/\gamma$
- and  $\sin(2\phi_1 + \phi_3)/(2\beta + \gamma)$



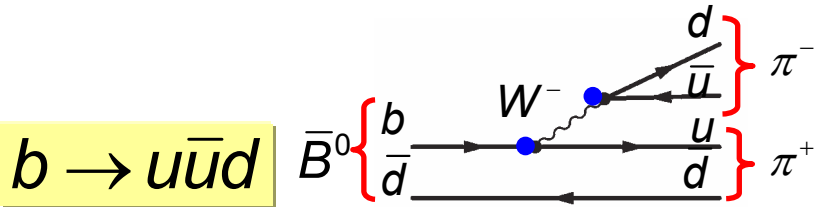
227M  $\bar{B}B$



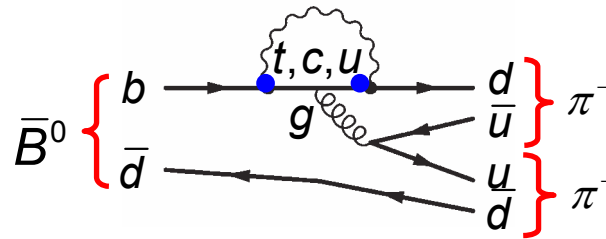
275M  $\bar{B}B$

*for most of the results*

# CPV in $B^0 \rightarrow \pi^+ \pi^-$

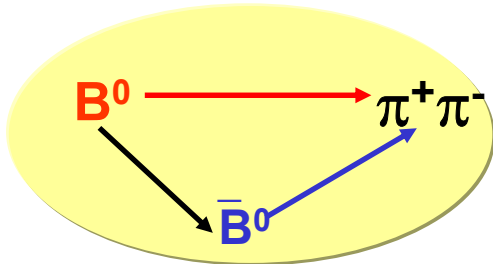


tree:  $\propto V_{ub} V_{ud}^* \propto \lambda^3$



penguin:  $\propto V_{tb} V_{td}^* \propto \lambda^3$

$$\lambda \equiv \frac{q}{p} \frac{\bar{A}_f}{A_f} = e^{-i\phi_M} \frac{\bar{A}_f}{A_f}$$



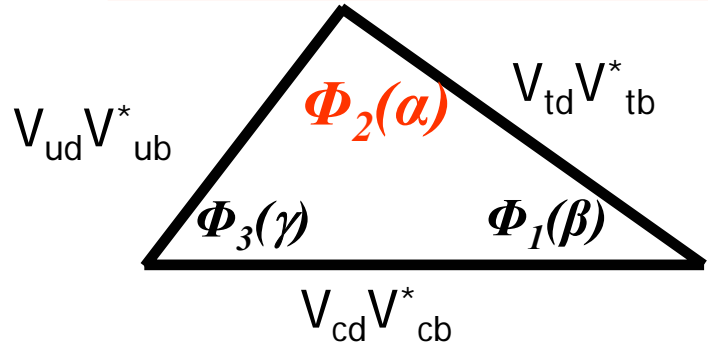
Mixing ind. CPV

$$\frac{2 \operatorname{Im} \lambda}{1 + |\lambda|^2}$$

Direct CPV

$$-\frac{1 - |\lambda|^2}{1 + |\lambda|^2}$$

$$A_{CP} = \frac{\Gamma(\bar{B}^0(\Delta t) \rightarrow \pi^+ \pi^-) - \Gamma(B^0(\Delta t) \rightarrow \pi^+ \pi^-)}{\Gamma(\bar{B}^0(\Delta t) \rightarrow \pi^+ \pi^-) + \Gamma(B^0(\Delta t) \rightarrow \pi^+ \pi^-)} = S_{\pi\pi} \sin(\Delta m_d \Delta t) + A_{\pi\pi} \cos(\Delta m_d \Delta t)$$



$$\Phi_2(\alpha) \equiv \arg(-V_{ud} V_{ub}^* / V_{td} V_{tb}^*)$$

$$S_{\pi\pi} = \sin 2\alpha \Rightarrow \sqrt{1 - A_{\pi\pi}^2} \sin 2(\alpha + \theta_{peng})$$

$\underbrace{\hspace{10em}}_{\alpha_{eff}}$

$$A_f \equiv -C_f$$



# Methodology



## Event selection

Include all  $B \rightarrow h^+h^-$  ( $h = \pi/K$ )

$B \rightarrow h^+h^-$  ( $h^-$  identified as  $\pi^-$ )

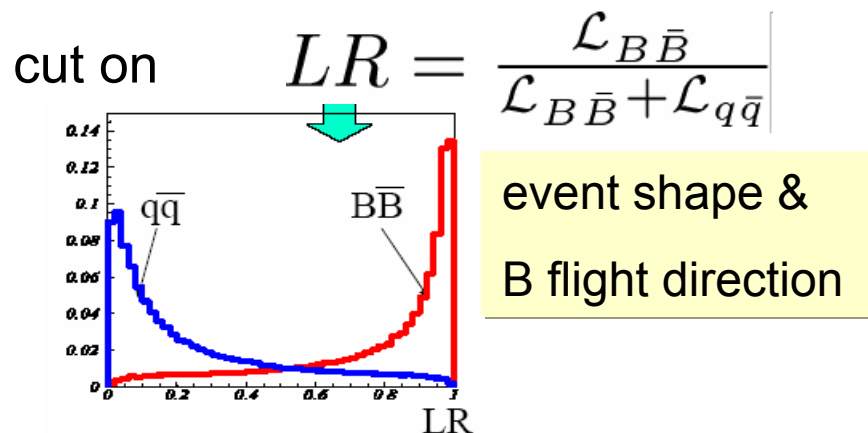
$5.29 > M_{ES} > 5.2$  GeV,  $|\Delta E| < 150$  MeV

$5.287 > M_{bc} > 5.271$  GeV,  $|\Delta E| < 64$  MeV

## Background treatment

$|\cos(\theta_S)| < 0.8$

Simultaneous fit to the signal and background components using discriminating variables:  $\theta_c$ ,  $\Delta E$ ,  $M_{ES}$ , **Fisher discr.** based on momentum flow relative to the  $h^+h^-$  thrust axis



## Flavour tagging

Use charged particles that are not associated with the reconstructed B

Tagging efficiency  $\sim 30\%$

$$M_{ES} = \sqrt{(s/2 + \vec{p}_i \vec{p}_B)^2 / E_i^2 - p_B^2} \quad \Delta E = E_B^* - E_{beam}^* \quad M_{bc} = \sqrt{(E_{beam}^*)^2 - (p_B^*)^2}$$



# Event yields

## Unbinned maximum likelihood fit

$$L_k = \exp\left(-\sum_i n_i \varepsilon_{i,k}\right) \prod_j \left[ \sum_i n_i \varepsilon_{i,k} P_{i,k}(\vec{x}_j, \vec{\alpha}_i) \right]$$

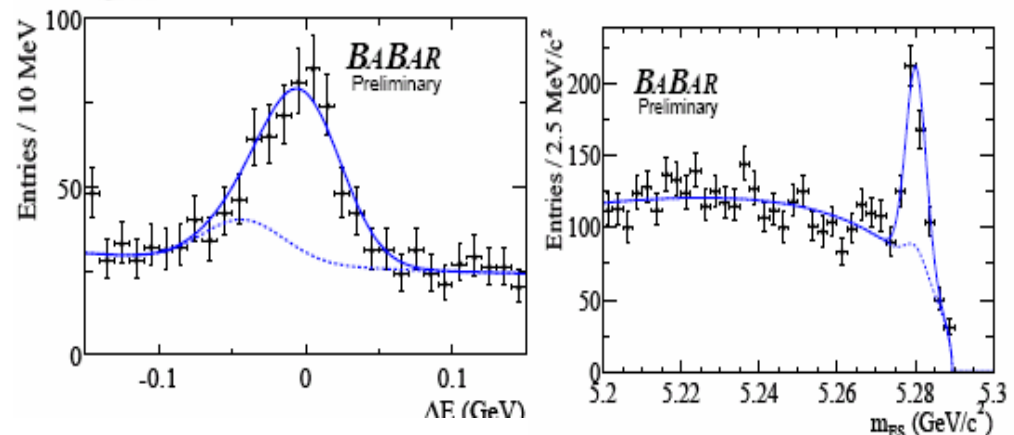
### • First step.

- ⇒ signal and background yields,  
Kπ charge asymmetries
- ◆ no flavor-tagging nor Δt in the fit

k: four flavor tagging categories  
 i: 8 signal and backgr.hypotheses  
 $\pi^+\pi^-$ ,  $K^+\pi^-$ ,  $K^-\pi^+$ ,  $K^+K^-$ , bkg.  
 $n_i$ : event yield of type i  
 $\varepsilon_{i,k}$ : tagging efficiency  
 $x_j$ :  $m_{ES}$ ,  $\Delta E$ , F,  $\theta^+$ ,  $\theta^-$ ,  $\Delta t$   
 $\alpha_i$ : PDF parameters

## Signal enhanced ΔE and M<sub>ES</sub> distributions

68030 candidate events  
 467±33 signal events  
 1606±51 Kπ events





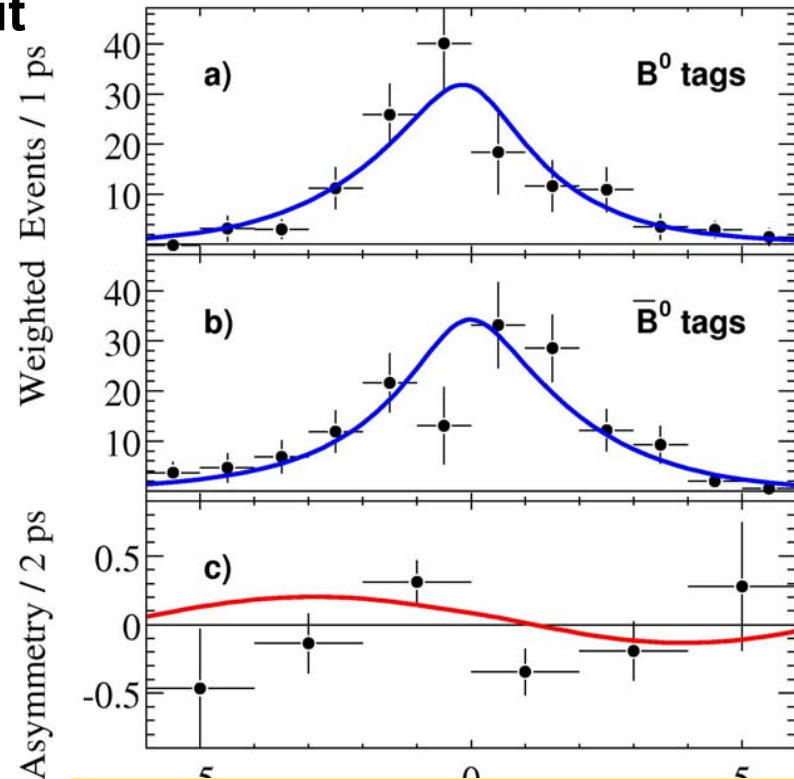
# CP fit results

## 2nd step

– unbinned maximum likelihood fit with 46 parameters

- $S_{\pi\pi}$ ,  $C_{\pi\pi}$
- 12 for background PDF of  $m_{ES}$ ,  $\Delta E$  and  $F$
- 8 for background  $\Delta t$  PDF
- 12 for background flavor-tagging efficiency
- 12 for background flavor-tagging efficiency asymmetries.

Data points: event weighting techn.



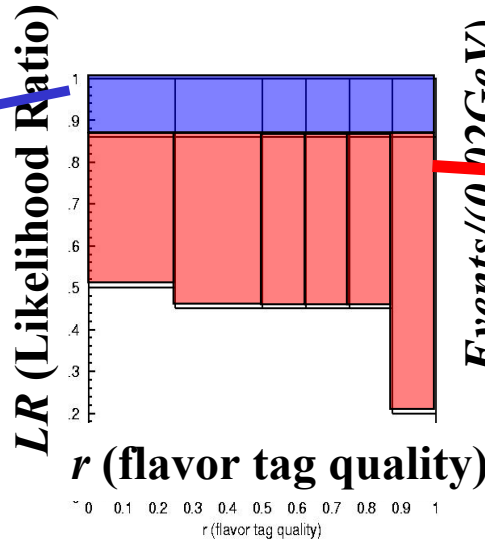
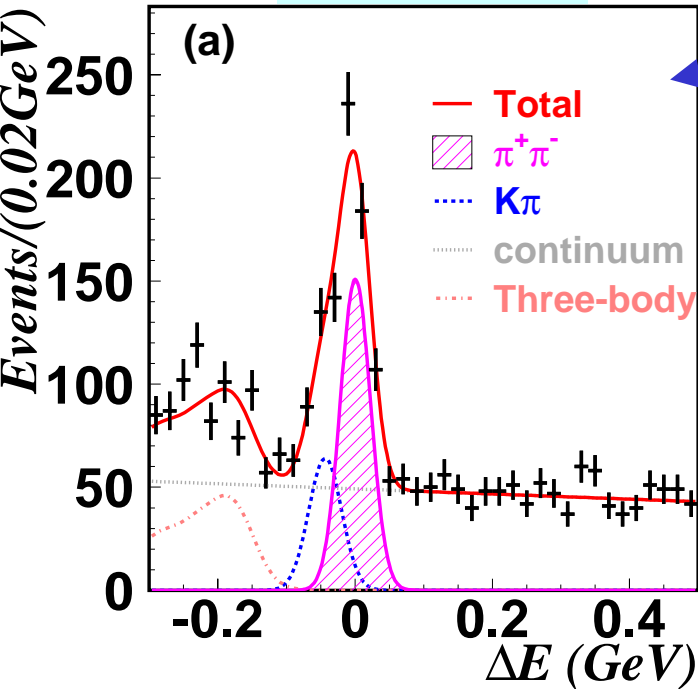
$$C_{\pi\pi} = -0.09 \pm 0.15(\text{stat}) \pm 0.04(\text{sys})$$

$$S_{\pi\pi} = -0.30 \pm 0.17(\text{stat}) \pm 0.03(\text{sys})$$

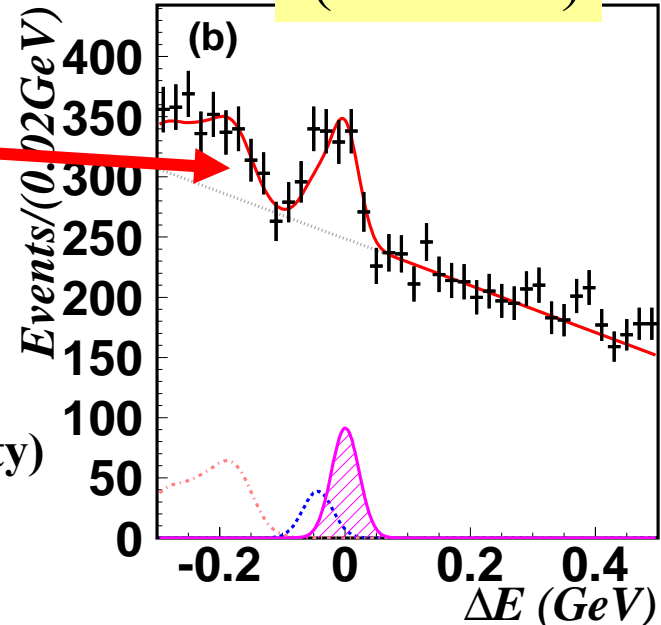
# Signal yields

Unbinned 2-dim maximum likelihood fit to  $\Delta E$ - $M_{bc}$

(LR > 0.86)



(LR < 0.86)



$M_{bc} > 5.2, -0.3 < \Delta E < 0.5$  GeV

Signal  $\oplus K\pi \oplus$  3-body B decays  $\oplus \bar{q}q$  bgr.

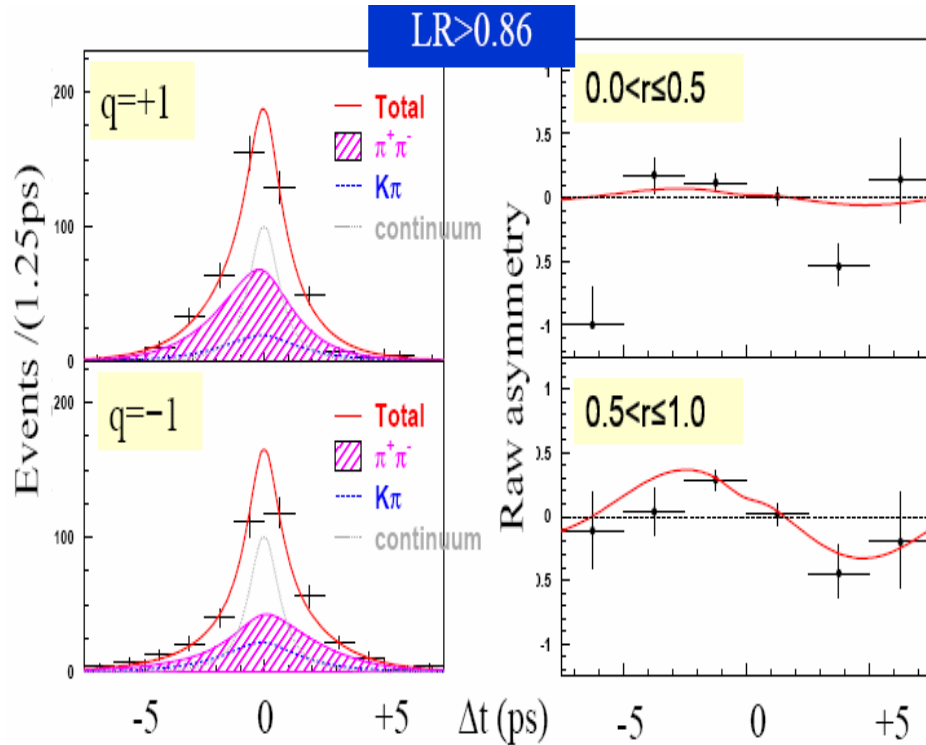
total number of events

2820 candidate events

666 ± 43 signal events

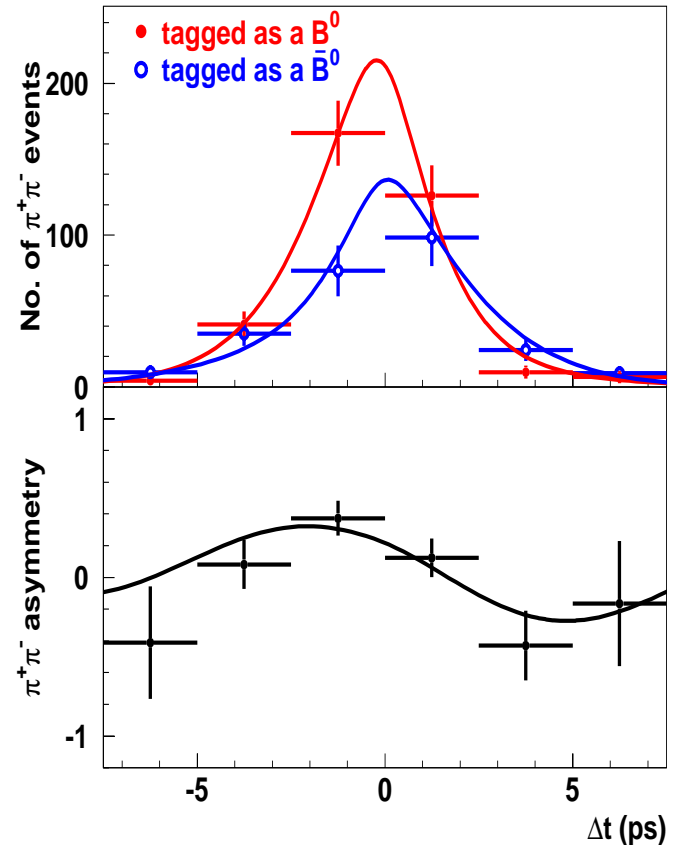
247 ± 31  $K\pi$  events

Unbinned maximum likelihood fit with 2 parameters:  $A_{\pi\pi}$ ,  $S_{\pi\pi}$

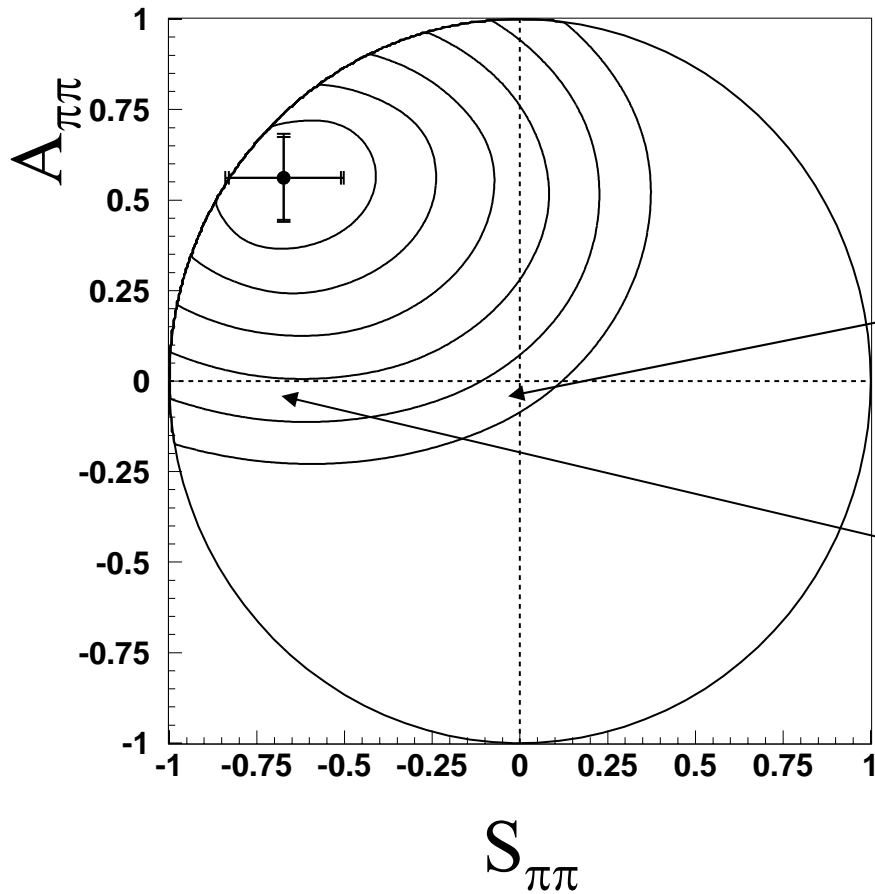


$$A_{\pi\pi} = +0.56 \pm 0.12(\text{stat}) \pm 0.06(\text{sys})$$

$$S_{\pi\pi} = -0.67 \pm 0.16(\text{stat}) \pm 0.06(\text{sys})$$



background subtracted  
fit projection for all



Large CP Violation,

$$(A,S)=(0,0)$$

$$1\text{-C.L.}=5.62 \times 10^{-8}, 5.4\sigma$$

$$(A,S)=(0,-0.62)$$

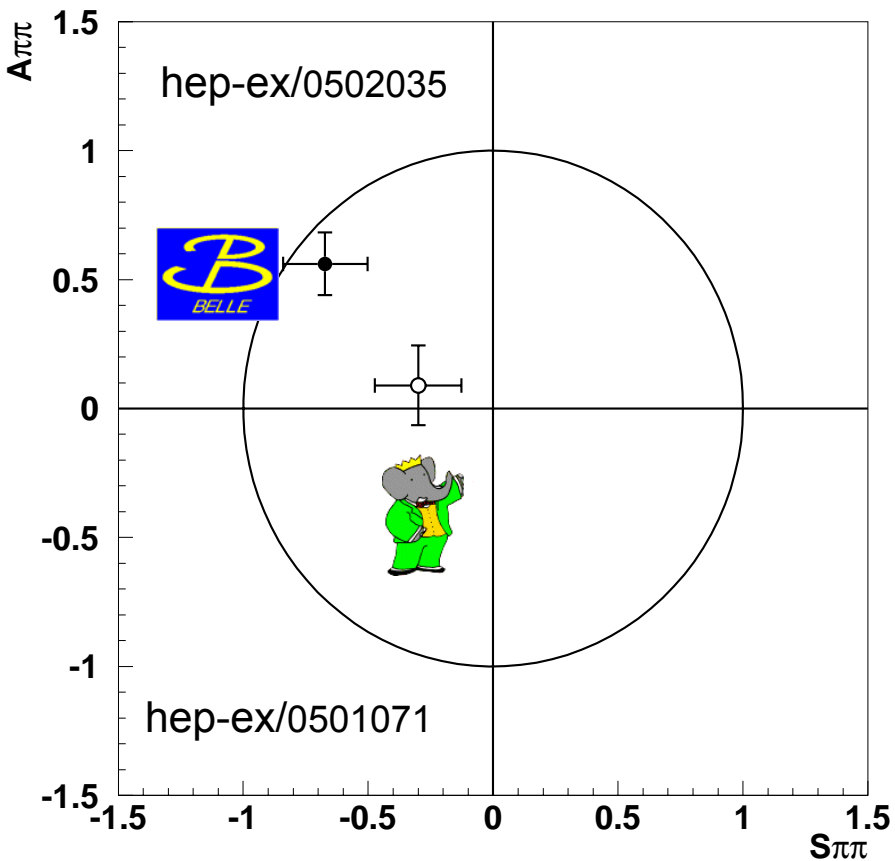
$$1\text{-C.L.}=5.13 \times 10^{-5}, 4.0\sigma$$

Large Direct CP violation,  
confirmation of the  
previous Belle results

both statistical and systematic errors are taken into account.

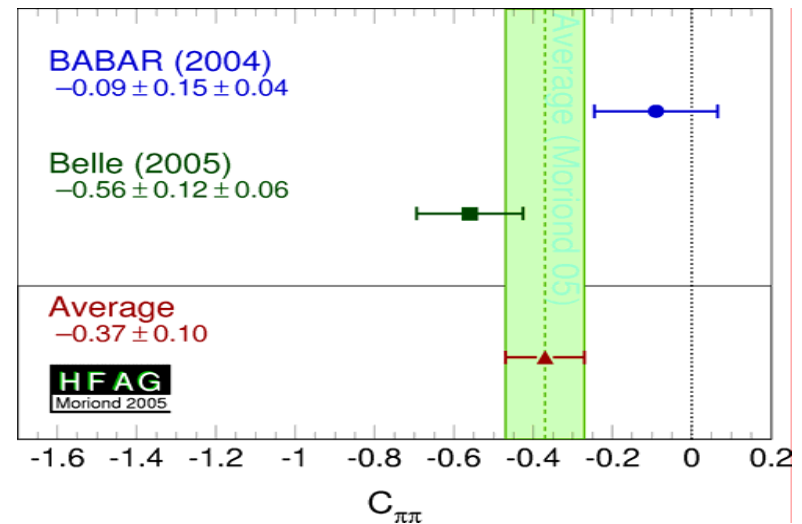
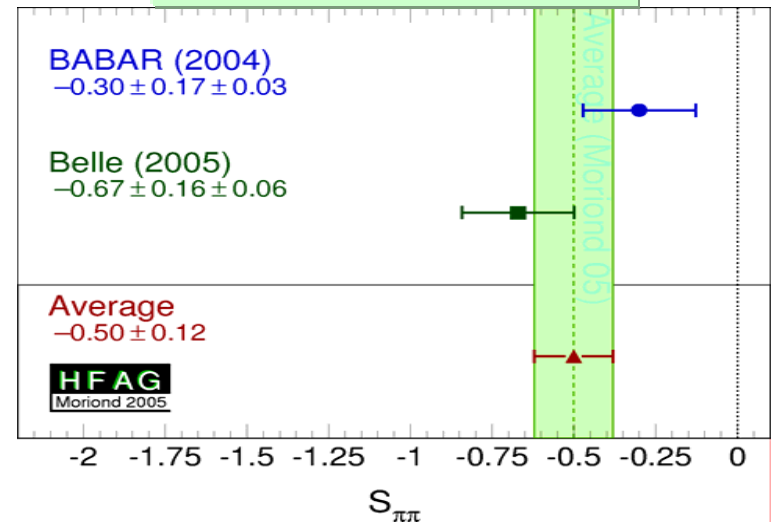
C.L. = Confidence Level

# CPV parameters in $B^0 \rightarrow \pi^+ \pi^-$

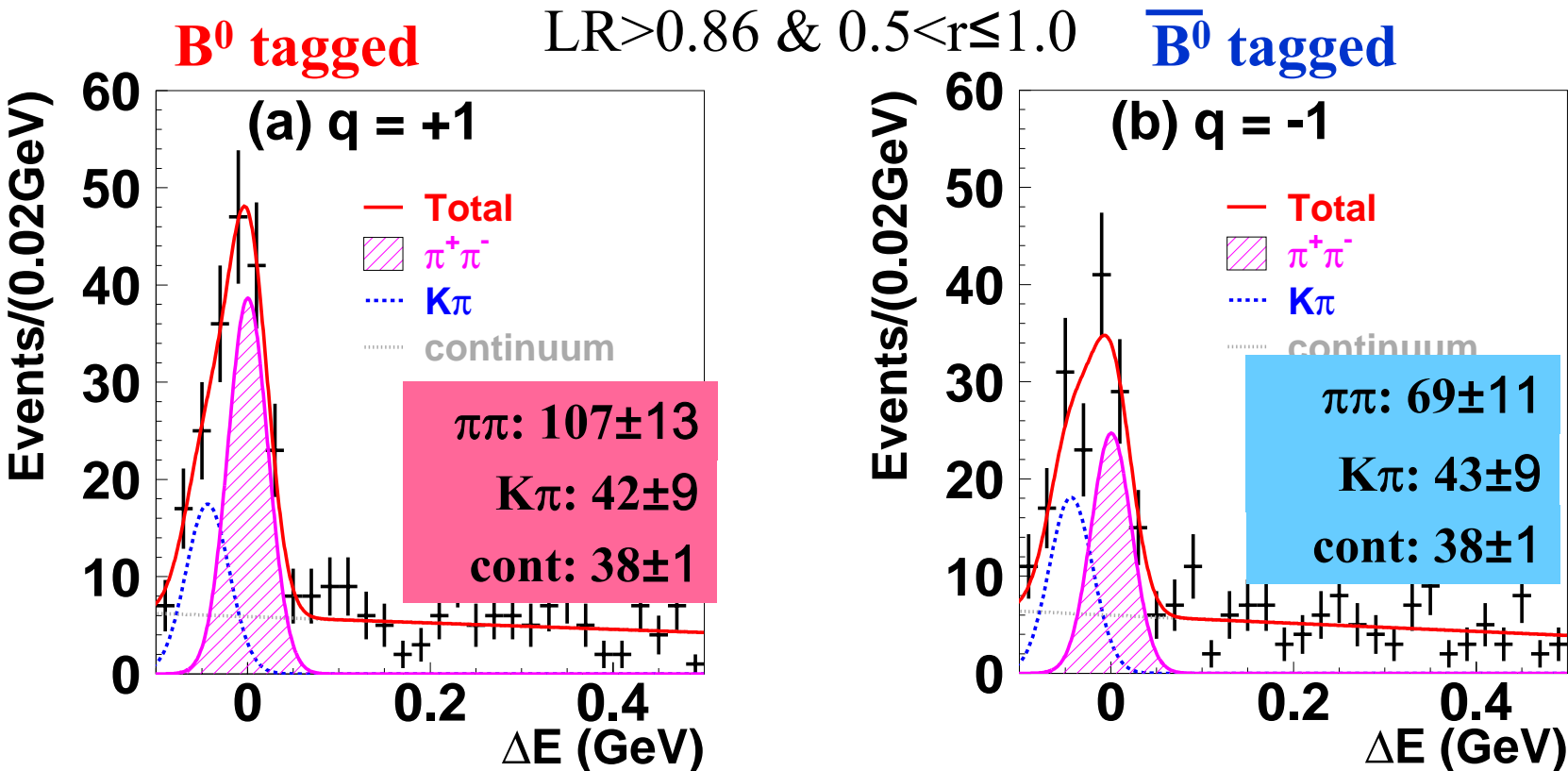


$\sim 2.3\sigma$  difference between  
*Belle & BaBar*

## HFAG Moriond 2005



# Time-integrated asymmetry



$$A_{\pi\pi} = +0.52 \pm 0.14$$

consistent with time-dependent fit

$$SU(3) : A_{CP}(K^+\pi^-) \sim -\frac{1}{3} A_{CP}(\pi^+\pi^-)$$

$$-\frac{1}{3} A_{CP}(\pi^+\pi^-) = -0.19 \pm 0.04$$

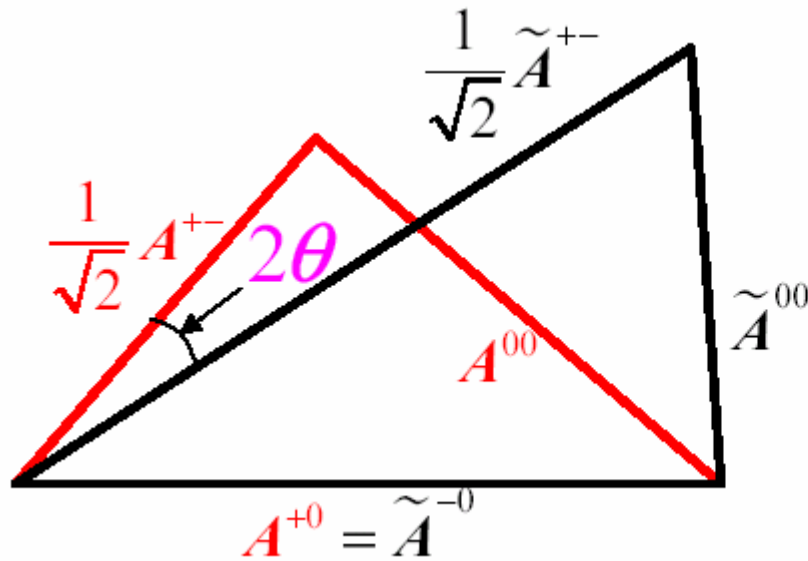
$$A_{CP}(K^+\pi^-) = -0.109 \pm 0.019$$

M. Gronau, J.L. Rosner, PLB 595, 339 (2004)

# Isospin analysis

$$S_{\pi\pi} = \sqrt{1 - A_{\pi\pi}^2} \sin(2\phi_2 + 2\theta)$$

The cleanest method to extract  $\phi_2$



M. Gronau, D. London, PRL 65, 3381 (1990)

	<i>Amplitude for</i>
$A^{+-}(\bar{A}^{+-})$	$B^0(\bar{B}^0) \rightarrow \pi^+\pi^-$
$A^{00}(\bar{A}^{00})$	$B^0(\bar{B}^0) \rightarrow \pi^0\pi^0$
$A^{+0}(\bar{A}^{-0})$	$B^+(B^-) \rightarrow \pi^+\pi^-(\pi^-\pi^0)$

$$\tilde{A}^{ij} = e^{2\phi_3} \bar{A}^{ij} \quad \equiv \text{both real and positive}$$



$$Br(\pi^0\pi^0) = (2.3_{-0.5-0.3}^{+0.4+0.2}) \times 10^{-6}$$

$$A_{CP}(\pi^0\pi^0) = +0.44_{-0.52}^{+0.53} \pm 0.17$$



$$Br(\pi^0\pi^0) = (1.17 \pm 0.32 \pm 0.10) \times 10^{-6}$$

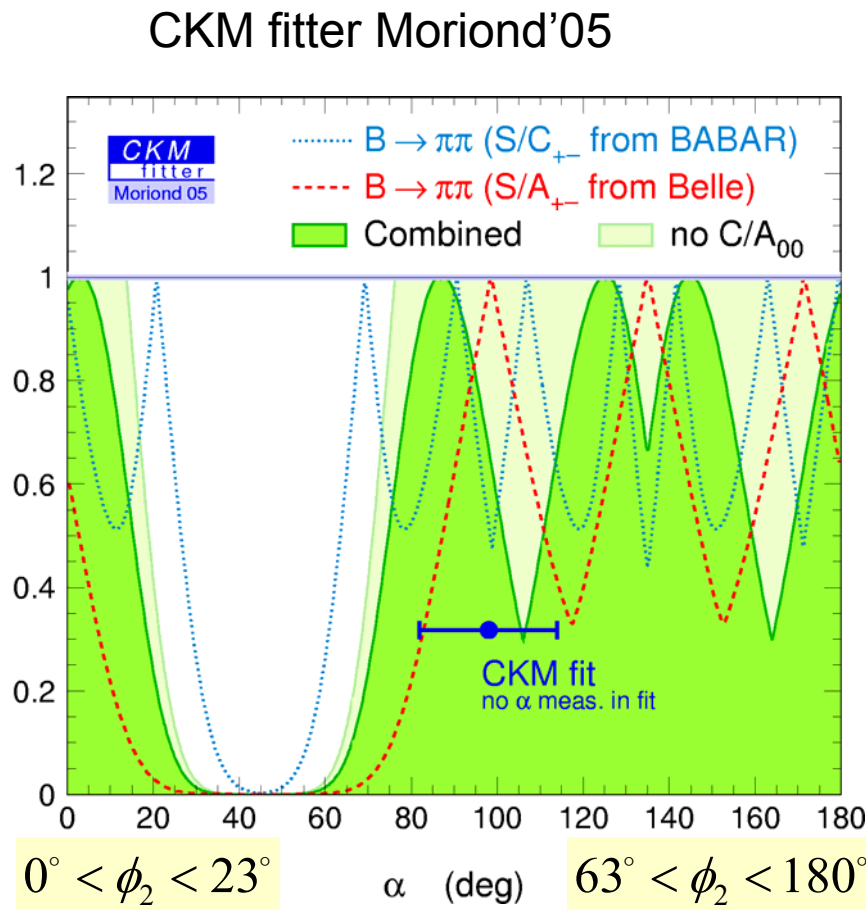
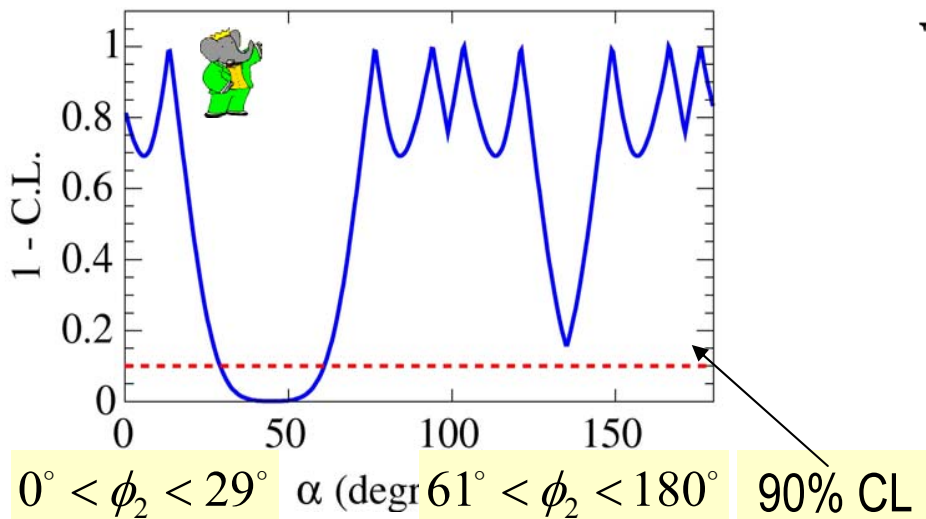
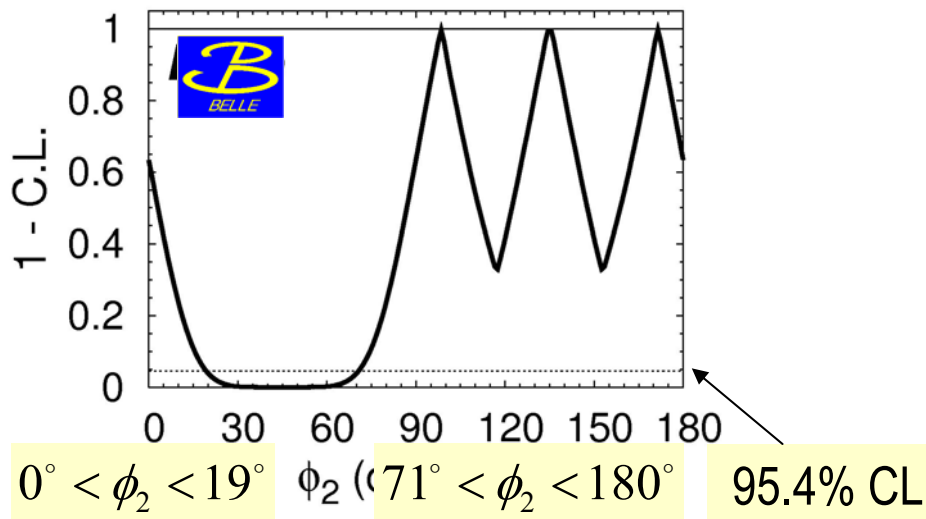
$$A_{CP}(\pi^0\pi^0) = +0.12 \pm 0.56 \pm 0.06$$

HFAG summer 2004 values for the branching ratios of  $B^0 \rightarrow \pi^+\pi^-$ ,  $\pi^0\pi^0$ ,  $B^+ \rightarrow \pi^+\pi^0$  and  $A_{CP}(B^0 \rightarrow \pi^0\pi^0)$ .

statistical treatment:


J. Charles *et al.*, hep-ph/0406184


# Constraints on $\phi_2(\alpha)$ from isospin analysis



# Measurements of $\Phi_3/\gamma$

## DCPV in $B \rightarrow K^+ \pi^-$

  $A_{K\pi}^{CP} = -0.133 \pm 0.030 \pm 0.009$

  $A_{K\pi}^{CP} = -0.101 \pm 0.025 \pm 0.005$

AVERAGE  $A_{K\pi}^{CP} = -0.109 \pm 0.019$

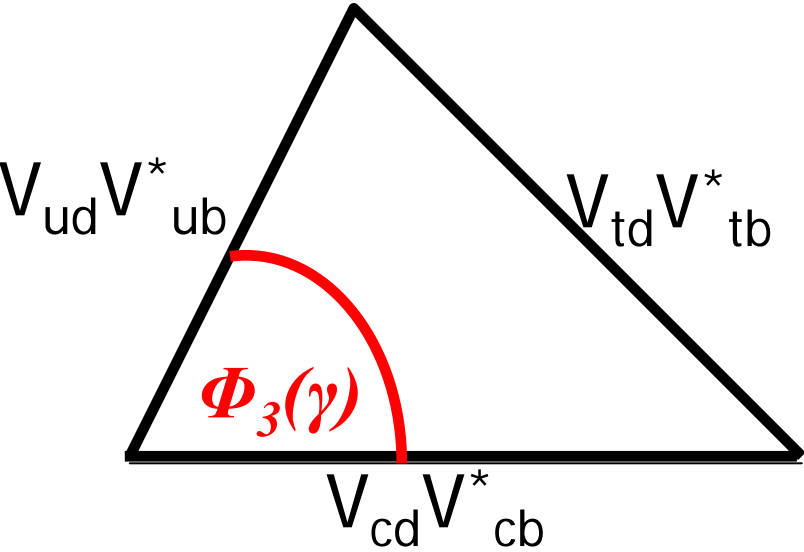
**>5 $\sigma$**



**$\Phi_3 \neq 0$**

$\bar{b} \rightarrow \bar{u} u s$  (tree)  $\oplus$   $\bar{b} \rightarrow \bar{s} u \bar{u}$  (penguin)

*Hard to extract  $\phi_3/\gamma$*



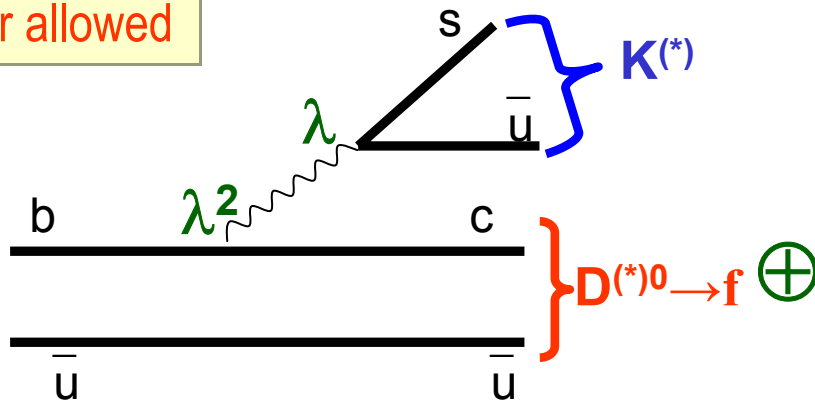
$\Phi_3/\gamma \equiv \arg(-V_{ud} V_{ub}^* / V_{cd} V_{cb}^*)$

**phase of  $V_{ub}$**

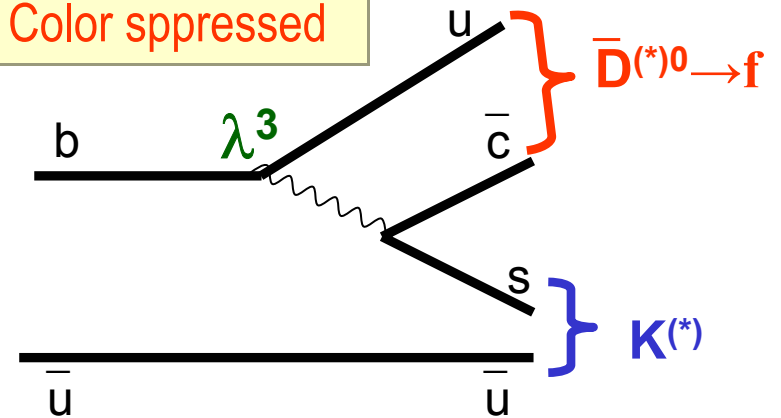
# Ways to measure $\Phi_3$ in $B \rightarrow DX_s$

DCPV in interference between  $b \rightarrow u$  &  $b \rightarrow c$

Color allowed



Color suppressed



$\bar{D}^{(*)}$  &  $D^{(*)}$  decay to the same final state  $f$  ( $f = \pi\pi, KK, K\pi\dots$ )

theoretically clean: only tree diagrams

$$A_{CP} \equiv (\Gamma_{B^+} - \Gamma_{B^-}) / (\Gamma_{B^+} + \Gamma_{B^-}) \propto r_B \sin(\gamma) \sin(\delta)$$

- $\delta$  = the strong phase between  $A(b \rightarrow u)$  &  $A(b \rightarrow c)$
- $r_B \equiv A(b \rightarrow u) / A(b \rightarrow c)$

experimentally challenging !!!

many methods with:

various  $f$

various  $X_s$

various observables

statistics required:

$$> 0.5 \text{ ab}^{-1}$$

# The Gronau-Wyler-London Method (GLW)

[Phys. Lett. B 253 (1991) 483]  
 [Phys. Lett. B 265 (1991) 172]

**$B^\pm \rightarrow D_{CP} K^{(*)\pm}$ ,  $D_{CP}$  is CP-eigenstate**

CP+ :  $D^0 \rightarrow \pi^+\pi^-, K^+K^-$     CP- :  $D^0 \rightarrow K_S\pi^0, K_S\eta, K_S\omega, K_S\phi, \dots$

*4 observables (3 independent)*

$$A_{CP^\pm} \equiv \frac{\Gamma(B^- \rightarrow D_{CP^\pm}^0 K^-) - \Gamma(B^+ \rightarrow D_{CP^\pm}^0 K^+)}{\Gamma(B^- \rightarrow D_{CP^\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP^\pm}^0 K^+)}$$

$$R_{CP^\pm} \equiv \frac{\Gamma(B^- \rightarrow D_{CP^\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP^\pm}^0 K^+)}{2\Gamma(B^- \rightarrow D^0 K^-)}$$

*3 unknowns*

$$= \pm 2r_B \sin \gamma \sin \delta_B / R_{CP^\pm}$$

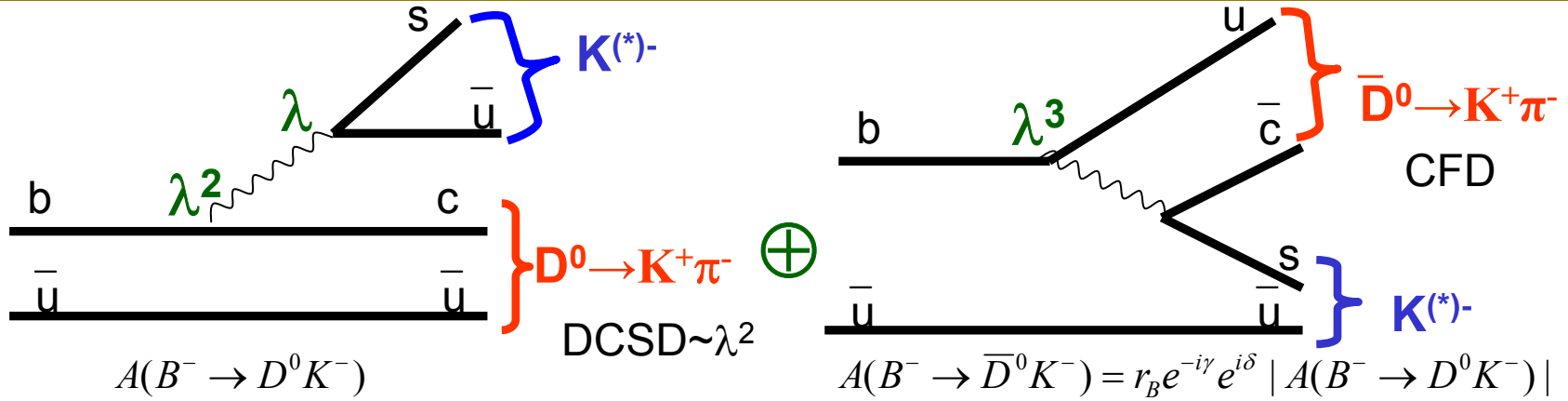
$$= 1 \pm 2r_B \cos \gamma \cos \delta_B + r_B^2$$

$\text{Br}(B \rightarrow DK) \sim 10^{-4} \otimes \text{Br}(D \rightarrow f_{CP}) \sim 10^{-2}$

$r_B \sim 0.1$

statistically limited

# The Atwood-Dunietz-Soni Method (ADS)



both amplitudes of comparable size  $\Rightarrow$  big CPV, small effective Br

count B candidates with  $K^+ K^-$  pairs

$$A_{ADS} \equiv \frac{\Gamma(B^- \rightarrow [K^+ \pi^-] K^-) - \Gamma(B^+ \rightarrow [K^- \pi^+] K^+)}{\Gamma(B^- \rightarrow [K^+ \pi^-] K^-) + \Gamma(B^+ \rightarrow [K^- \pi^+] K^+)}$$

$$R_{ADS} \equiv \frac{\Gamma(B^- \rightarrow [K^+ \pi^-] K^-) + \Gamma(B^+ \rightarrow [K^- \pi^+] K^+)}{\Gamma(B^- \rightarrow [K^- \pi^+] K^-) + \Gamma(B^+ \rightarrow [K^+ \pi^-] K^+)}$$

$$r_D = \frac{|A(D^0 \rightarrow K^+ \pi^-)|}{|A(D^0 \rightarrow K^- \pi^+)|} = 0.060 \pm 0.003$$

Phys.Rev.Lett.91:171801,2003

$$= 2r_B r_D \sin \gamma \sin(\delta_B + \delta_D) / R_{ADS}$$

$$= 2r_B r_D \cos \gamma \cos(\delta_B + \delta_D) + r_B^2 + r_D^2$$

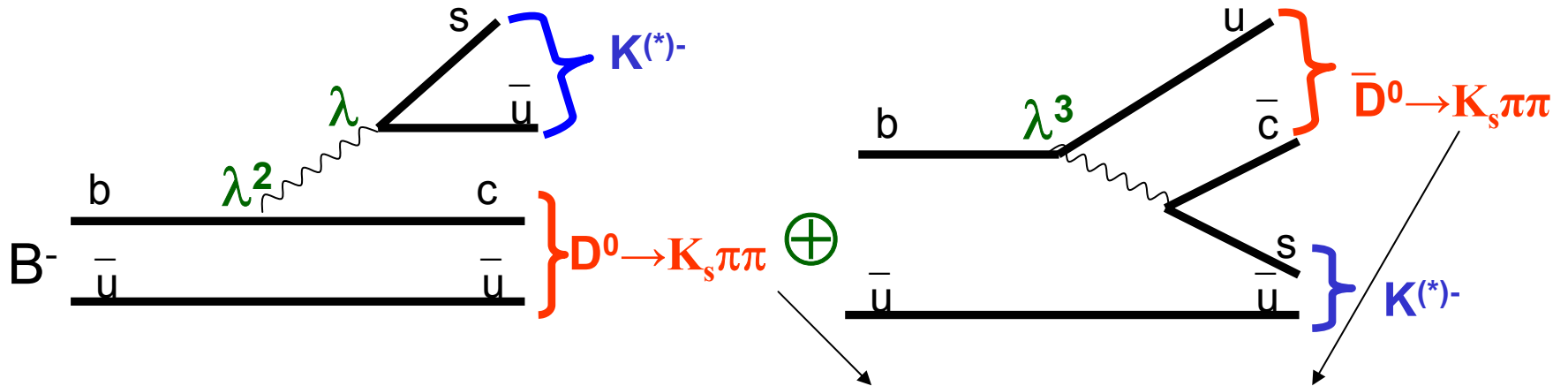
$\delta_D$  - D decay strong phase, unknown

$$R_{ADS}(D\pi) + R_{ADS}(D\gamma) = 2(r_B^2 + r_D^2)$$

$\delta_D$  - differs by  $\pi$  for  $D^* \rightarrow D\gamma$  &  $D^* \rightarrow D\pi^0$

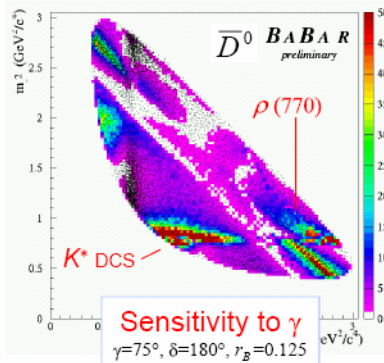
# Dalitz analysis of $B^\pm \rightarrow D^{(*)0} K^{(*)\pm}$ , $D^0 \rightarrow K_S \pi^+ \pi^-$

Giri, Grossman, Sofer & Zupan [Phys. Rev. D 68 (2003) 054018]

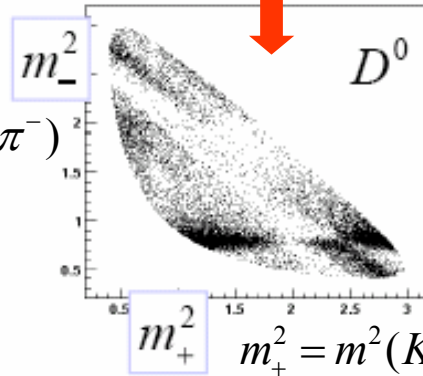


$$M_-(m_-^2, m_+^2) = |A(B^- \rightarrow D^0 K^-)| \{f(m_-^2, m_+^2) + r_B e^{-i\gamma} e^{i\delta} f(m_+^2, m_-^2)\}$$

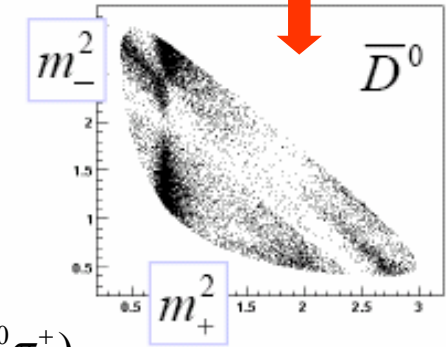
CP



$$m_-^2 = m^2(K_S^0 \pi^-)$$



$$m_+^2 = m^2(K_S^0 \pi^+)$$



$$M_+(m_-^2, m_+^2) = |A(B^+ \rightarrow \bar{D}^0 K^+)| \{f(m_+^2, m_-^2) + r_B e^{i\gamma} e^{i\delta} f(m_-^2, m_+^2)\}$$

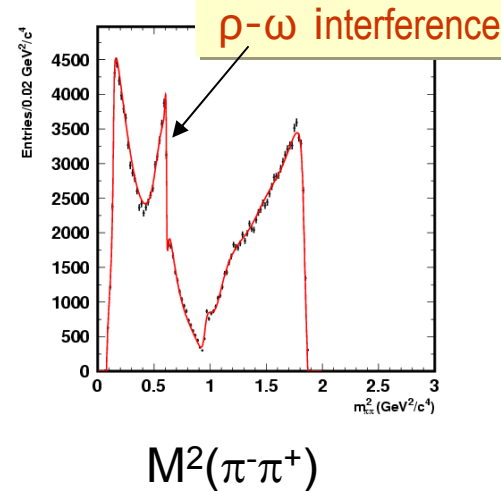
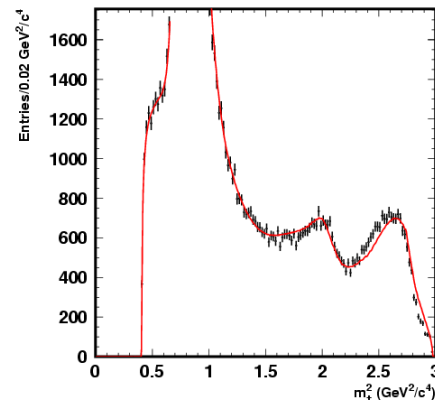
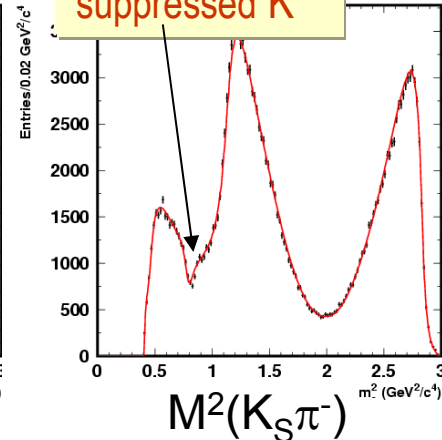
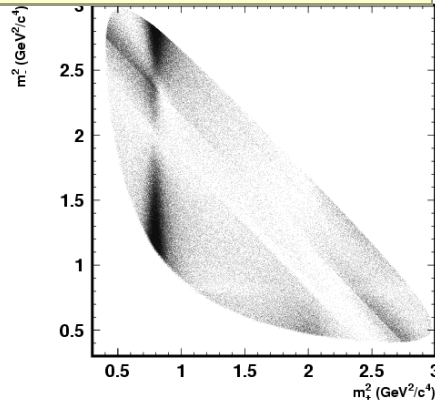
# $D^0 \rightarrow K_S \pi^+ \pi^-$ decay model



187k  $D^* \rightarrow D^0 \pi$ ,  $D^0 \rightarrow K_S \pi^+ \pi^-$

Intermediate state	Amplitude	Phase ( $^\circ$ )	Fit fraction
$K_S \sigma_1$	$1.57 \pm 0.10$	$214 \pm 4$	9.8%
$K_S \rho^0$	1.0 (fixed)	0 (fixed)	21.6%
$K_S \omega$	$0.0310 \pm 0.0010$	$113.4 \pm 1.9$	0.4%
$K_S f_0(980)$	$0.394 \pm 0.006$	$207 \pm 3$	4.9%
$K_S \sigma_2$	$0.23 \pm 0.03$	$210 \pm 13$	0.6%
$K_S f_2(1270)$	$1.32 \pm 0.04$	$348 \pm 2$	1.5%
$K_S f_0(1370)$	$1.25 \pm 0.10$	$69 \pm 8$	1.1%
$K_S \rho^0(1450)$	$0.89 \pm 0.07$	$1 \pm 6$	0.4%
$K^*(892)^+ \pi^-$	$1.621 \pm 0.010$	$131.7 \pm 0.5$	61.2%
$K^*(892)^- \pi^+$	$0.154 \pm 0.005$	$317.7 \pm 1.6$	0.55%
$K^*(1410)^+ \pi^-$	$0.22 \pm 0.04$	$120 \pm 14$	0.05%
$K^*(1410)^- \pi^+$	$0.35 \pm 0.04$	$253 \pm 6$	0.14%
$K_0^*(1430)^+ \pi^-$	$2.15 \pm 0.04$	$348.7 \pm 1.1$	7.4%
$K_0^*(1430)^- \pi^+$	$0.52 \pm 0.04$	$89 \pm 4$	0.43%
$K_2^*(1430)^+ \pi^-$	$1.11 \pm 0.03$	$320.5 \pm 1.8$	2.2%
$K_2^*(1430)^- \pi^+$	$0.23 \pm 0.02$	$263 \pm 7$	0.09%
$K^*(1680)^+ \pi^-$	$2.34 \pm 0.26$	$110 \pm 5$	0.36%
$K^*(1680)^- \pi^+$	$1.3 \pm 0.2$	$87 \pm 11$	0.11%
non-resonant	$3.8 \pm 0.3$	$157 \pm 4$	9.7%

Doubly Cabibbo suppressed  $K^*$



13 distinct resonances + NR

Isobar model (CLEO):

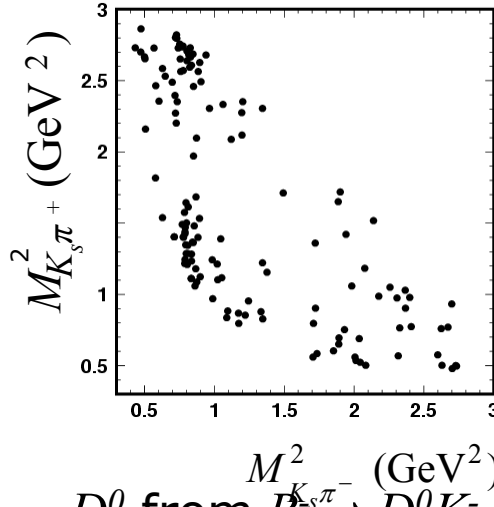
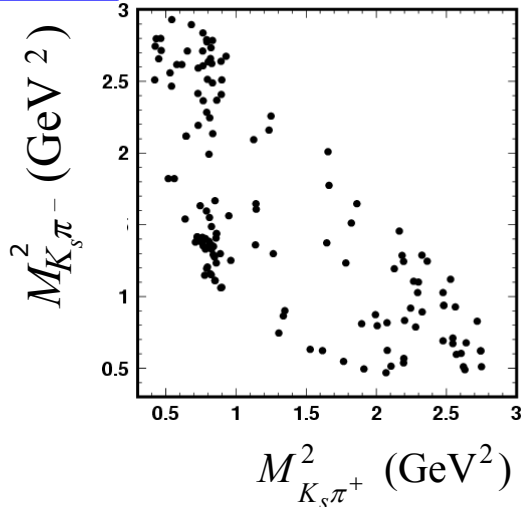
$$f(m_-^2, m_+^2) = \sum_r a_r e^{i\delta_r} A_r(m_-^2, m_+^2) + a_{nr} e^{i\delta_{nr}}$$

# $B^\pm \rightarrow DK^\pm, D \rightarrow K_S \pi^+ \pi^-$ Dalitz plots



139 events

137 events



Fit these  $D^0$  Dalitz plots using unbinned maximum likelihood

Free parameters:  $r_B, \phi_3, \delta$

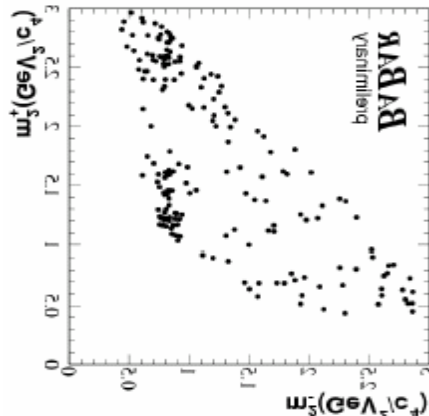
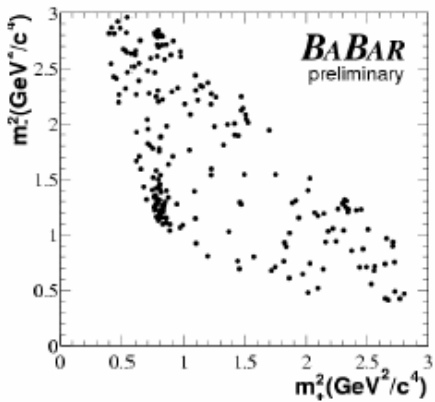
2-fold ambiguity:

$\phi_3, \delta, \cup \phi_3+180^\circ, \delta+180^\circ$



$D^0$  from  $B^+ \rightarrow D^0 K^+$

$D^0$  from  $B^- \rightarrow D^0 K^-$   
( $\pi^+$  and  $\pi^-$  interchanged)





hep-ex/0411049

$D^0 K$

CPV signif. 94%

$D^0 K$

$$\begin{aligned} \varphi_3 &= [64 \pm 19 \pm 13(\text{sys}) \pm 11(\text{model})]^\circ \\ r_B &= 0.21 \pm 0.08 \pm 0.03(\text{sys}) \pm 0.04(\text{model}) \\ \delta_B &= [157 \pm 19 \pm 11(\text{sys}) \pm 21(\text{model})]^\circ \end{aligned}$$

$$\begin{aligned} r_B &= 0.118 \pm 0.079 \pm 0.034(\text{sys})_{-0.034}^{+0.036}(\text{model}) \\ \delta_B &= [104 \pm 45_{-21}^{+17}(\text{sys})_{-24}^{+16}(\text{model})]^\circ \end{aligned}$$

$D^{*0} K$

CPV signif. 38%

$D^{*0} K$

$$\begin{aligned} \varphi_3 &= [75 \pm 57 \pm 12(\text{sys}) \pm 11(\text{model})]^\circ \\ r_B &= 0.12_{-0.11}^{+0.16} \pm 0.02(\text{sys}) \pm 0.04(\text{model}) \\ \delta_B &= [321 \pm 57 \pm 11(\text{sys}) \pm 21(\text{model})]^\circ \end{aligned}$$

$$\begin{aligned} r_B^* &= 0.169 \pm 0.096_{-0.026}^{+0.030}(\text{sys})_{-0.026}^{+0.029}(\text{model}) \\ \delta_B^* &= [296 \pm 41_{-12}^{+14}(\text{sys}) \pm 15(\text{model})]^\circ \end{aligned}$$

hep-ex/0504013

$D^0 K^*$

CPV signif. 63%

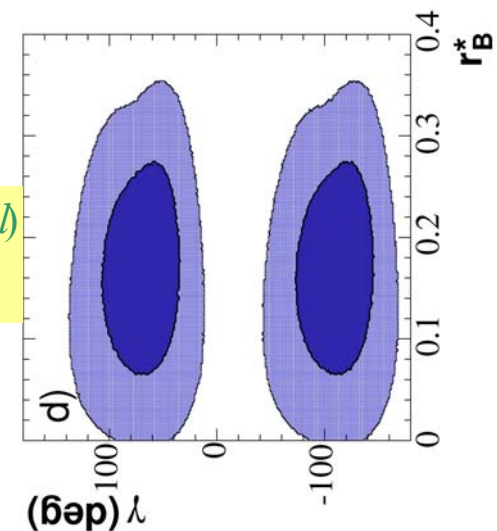
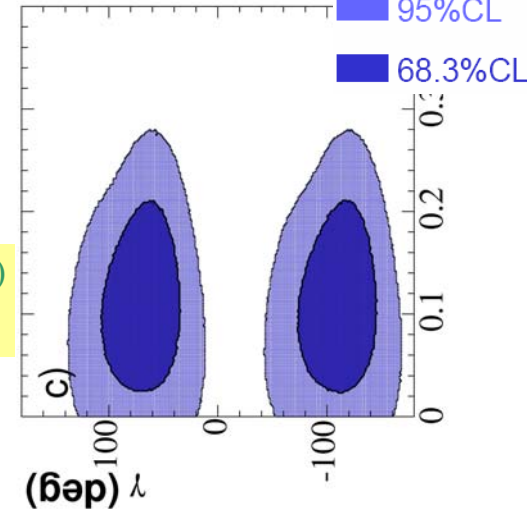
$$\begin{aligned} \varphi_3 &= [112 \pm 35 \pm 8(\text{sys}) \pm 21(\text{model}) \pm 8(nr)]^\circ \\ r_B &= 0.25_{-0.18}^{+0.17} \pm 0.09(\text{sys}) \pm 0.04(\text{model}) \pm 0.08(nr) \\ \delta_B &= [353 \pm 35 \pm 8(\text{sys}) \pm 21(\text{model}) \pm 49(nr)]^\circ \end{aligned}$$

$$\gamma = [70 \pm 31_{-10}^{+12}(\text{sys})_{-11}^{+14}(\text{model})]^\circ [12^\circ, 137^\circ]$$

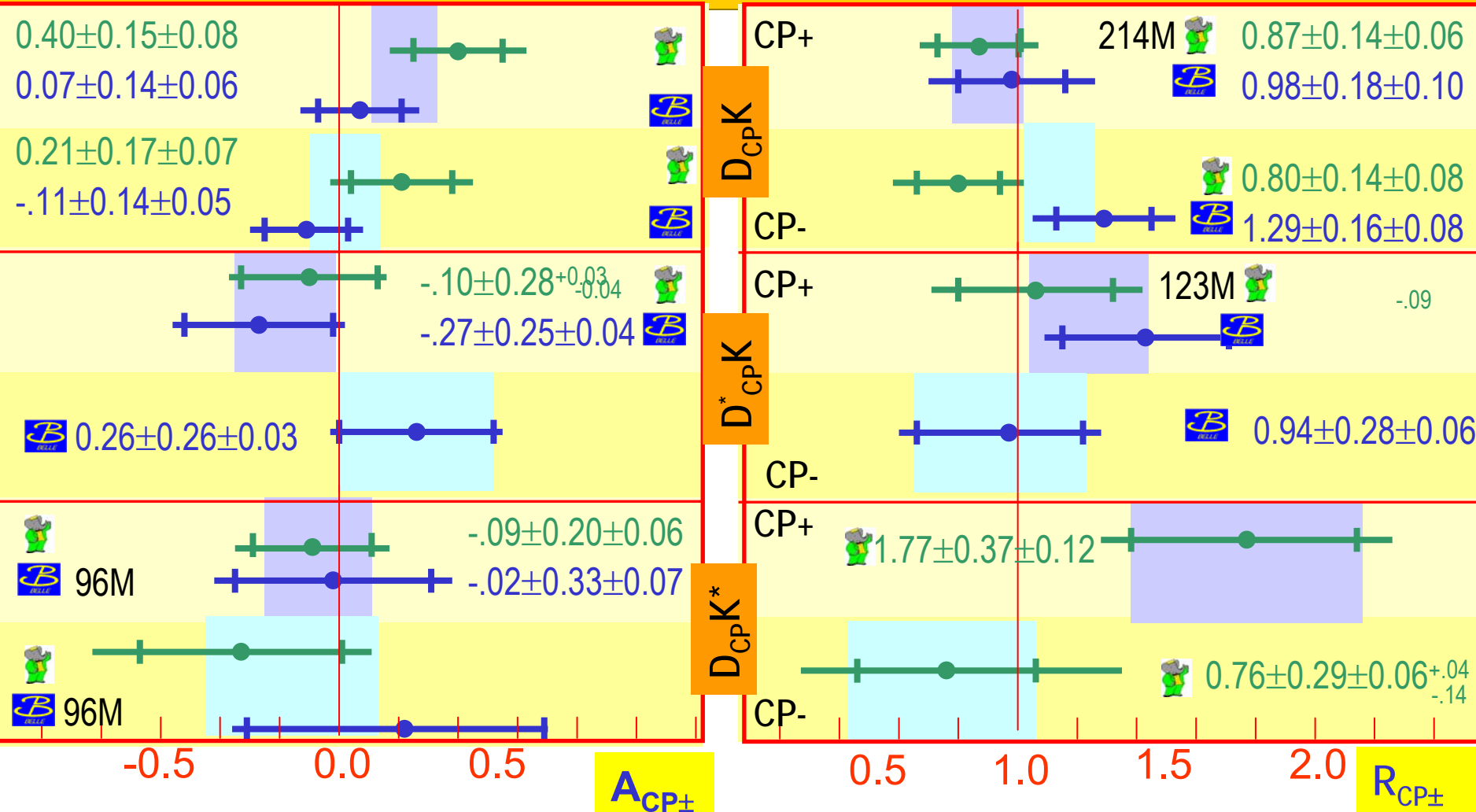
hep-ex/0504039

95%CL

68.3%CL



# GLW-results



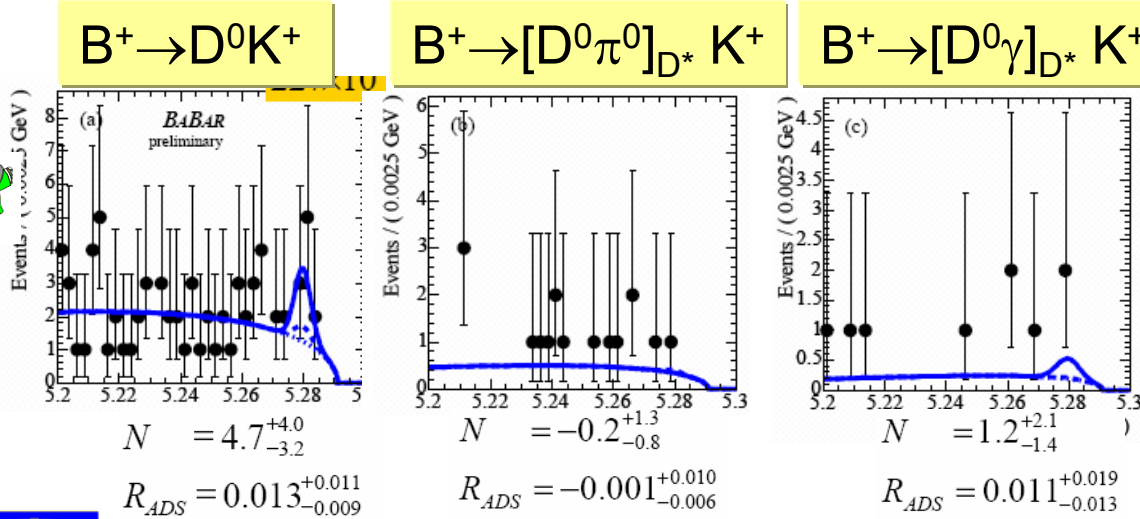
$$\sin^2(\Phi_3) \leq R_{CP\pm}$$

$$0.5 \cdot (R_{CP+} + R_{CP-}) = 1 + r_B^2$$

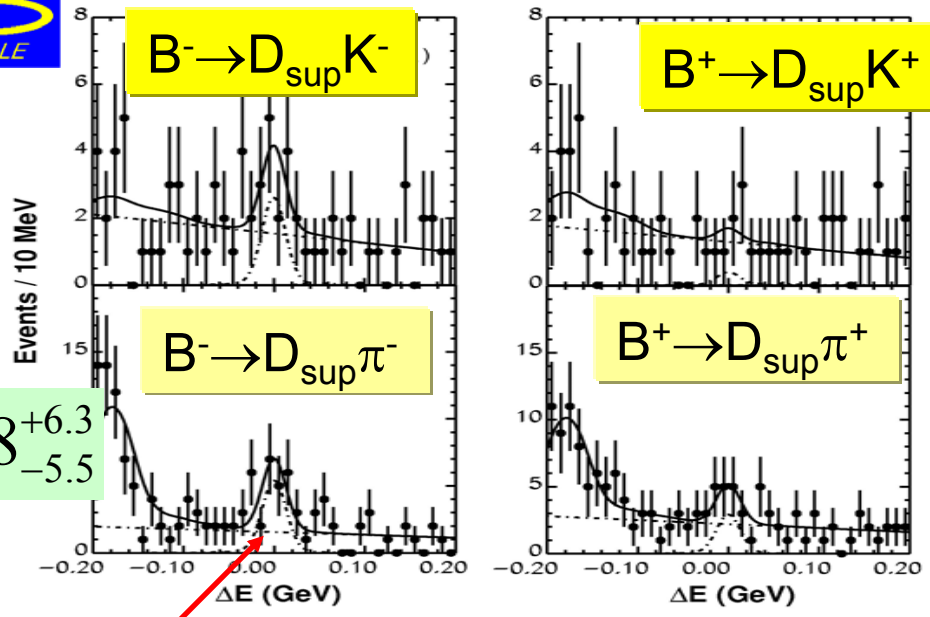
Loose bounds on  $r_B$

# $B^- \rightarrow D^{(*)0}_{ADS} [K^+ \pi^-] K^-$

hep-ex/0408028



$r_B < 0.23$   $DK$   
 (90%CL)  
 $r_B < 0.16$   $D^*K$



hep-ex/0412025

$R_{DK} = 2.3^{+1.6}_{-1.4} \pm 0.1(sys) \times 10^{-2}$   
 $A_{DK} = .88^{+0.77}_{-0.62} \pm 0.1(sys)$

$R_{D\pi} = 3.5^{+1.0}_{-0.9} \pm 0.2(sys) \times 10^{-3}$   
 $A_{D\pi} = .30^{+0.29}_{-0.25} \pm 0.06(sys)$

$r_B < 0.27$  (90%CL)

First observation

# Constraints on $\phi_3(\gamma)$ from $B \rightarrow DK$



Dalitz analysis

$$\phi_3 = [68_{-15}^{+14} \pm 13(\text{sys}) \pm 11(\text{model})]^\circ$$

$$[22^\circ, 113^\circ]$$

$$r_B(D^0 K) = 0.21 \pm 0.08 \pm 0.03 \pm 0.04$$

$$r_B(D^{*0} K) = 0.12_{-0.11}^{+0.16} \pm 0.02 \pm 0.04$$

$$r_B(D^0 K^*) = 0.24_{-0.18}^{+0.17} \pm 0.09 \pm 0.04 \pm 0.08$$



Dalitz analysis

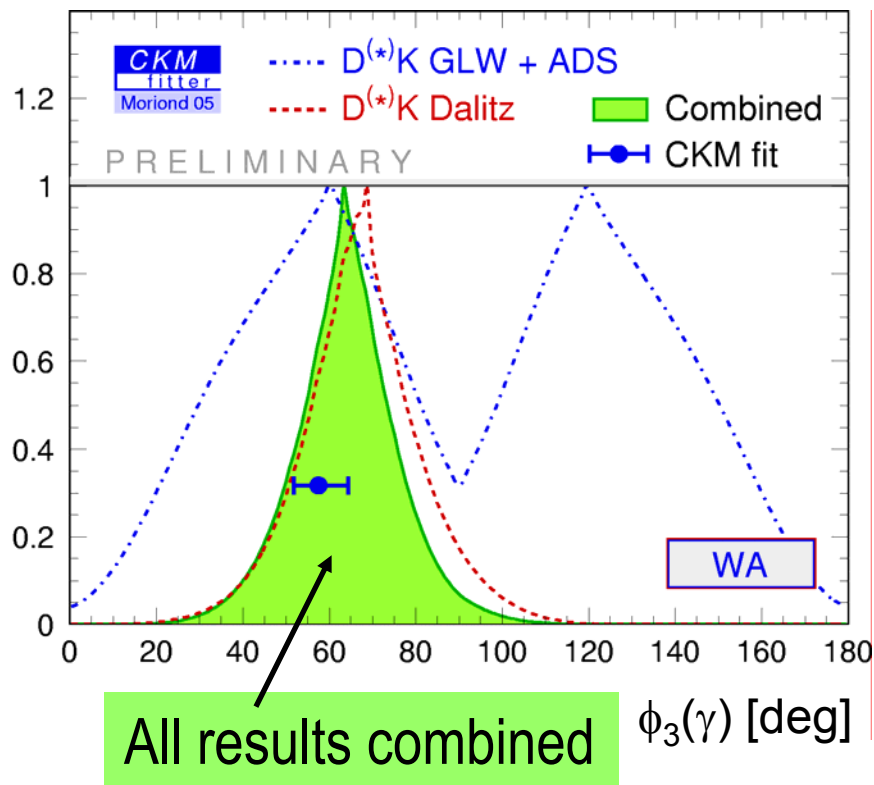
$$\gamma = [70 \pm 31_{-10}^{+12} (\text{sys})_{-11}^{+14} (\text{model})]^\circ$$

$$[12^\circ, 137^\circ]$$

$$r_B(D^0 K) = 0.118_{-0.096}^{+0.079} \pm 0.034_{-0.034}^{+0.036}$$

$$r_B(D^{*0} K) = 0.169 \pm 0.096_{-0.028}^{+0.03} \pm 0.029_{-0.026}$$

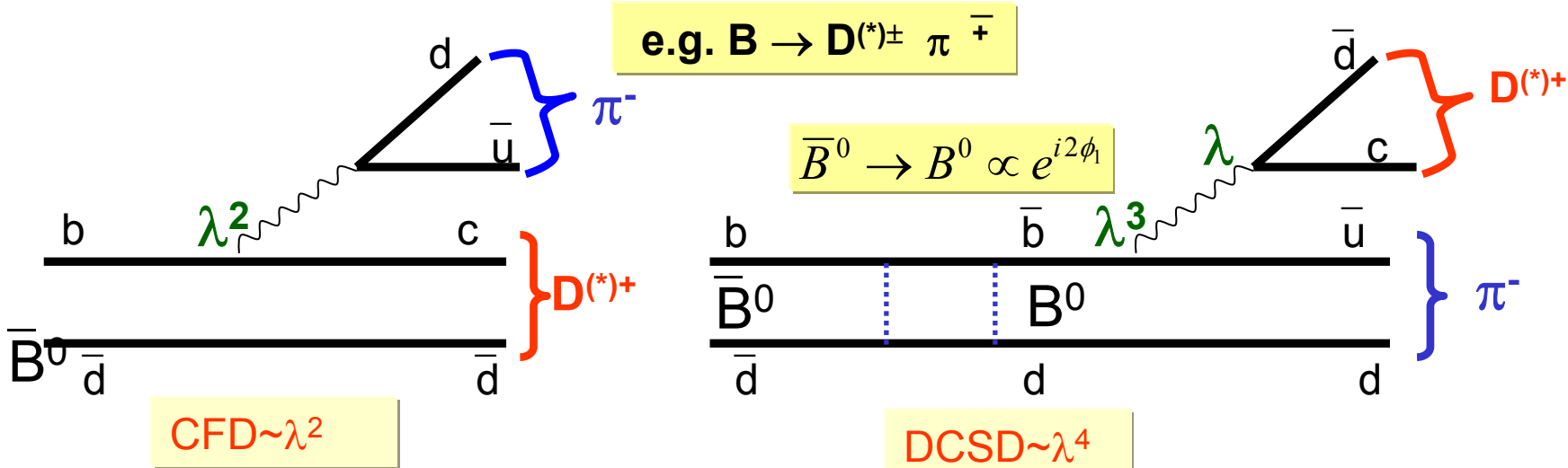
CKM fitter Moriond'05



# Measurements of $\sin(2\beta+\gamma)/(2\phi_1+\phi_3)$

I. Dunietz, Phys.Lett. B 427, 179(1998)

Use *interference*  $b \rightarrow c \bar{u} d \oplus b \rightarrow u \bar{c} d$  instead of  $b \rightarrow c \bar{u} s \oplus b \rightarrow u \bar{c} s$



$$P(B^0 \rightarrow D^{*\mp} \pi^\pm, \Delta t) \propto 1 \pm C \cos(\Delta m \Delta t) - S^\mp \sin(\Delta m \Delta t)$$

$$P(\bar{B}^0 \rightarrow D^{*\mp} \pi^\pm, \Delta t) \propto 1 \mp C \cos(\Delta m \Delta t) + S^\mp \sin(\Delta m \Delta t)$$

$$C = (1 - R_{D^* \pi}^2) / (1 + R_{D^* \pi}^2) \approx 1$$

$$S^\pm = -2R_{D^* \pi} \sin(2\phi_1 + \phi_3 \pm \delta_{D^* \pi})$$

$$R_{D^* \pi} = \frac{|suppressed|}{|favoured|} \approx 0.02$$

$$a_\pi^* \equiv -\frac{S^+ + S^-}{2} \approx 2R_{D^* \pi} \sin(2\phi_1 + \phi_3) \cos \delta$$

$$c_\pi^* \equiv -\frac{S^+ - S^-}{2} \approx 2R_{D^* \pi} \cos(2\phi_1 + \phi_3) \sin \delta$$

*Very small asymmetry offset by copious statistics*

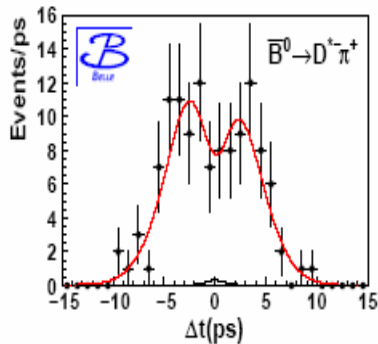
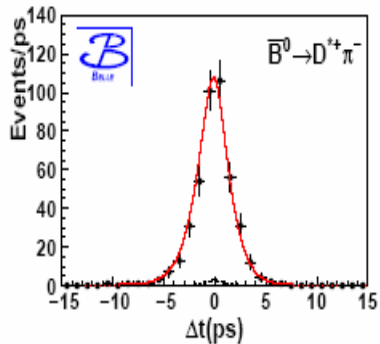
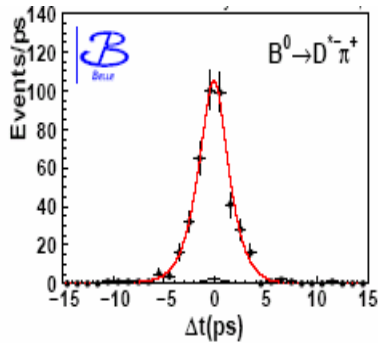
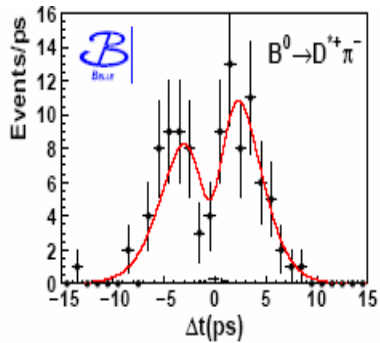


# $B^0 \rightarrow D^{(*)-} \pi^+$ time dependent decay rates

152M  $\bar{B}B$   
hep-ex/0308048

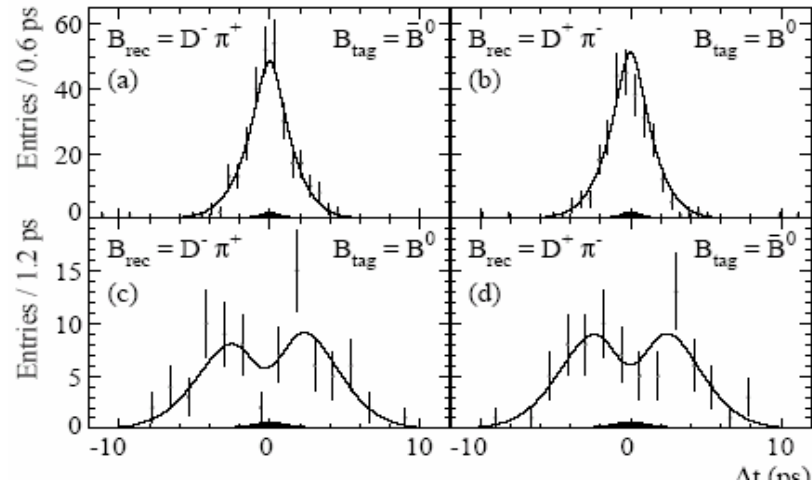
*exclusive reconstruction*

110M  $BB$   
hep-ex/0408059



$D^* \pi$  7763 events, purity 96%

$D \pi$  9351 events, purity 91%



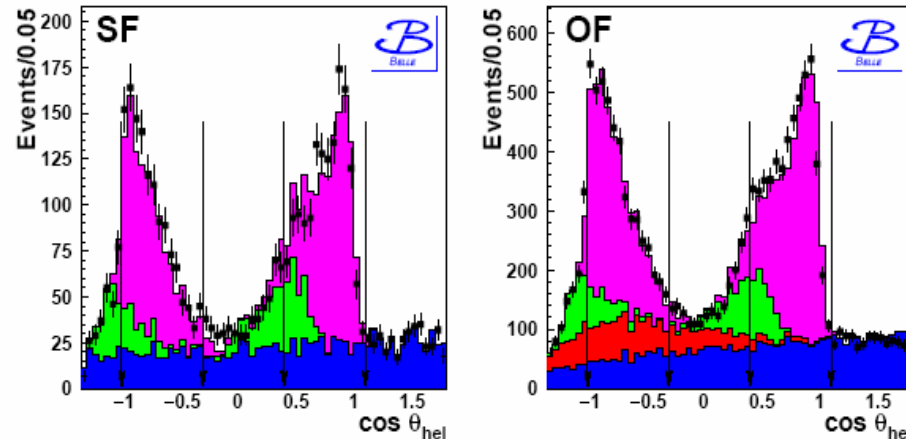
$D^\pm \pi^\mp$ (all tag)	$7611 \pm 97$	91%
$D^{*\pm} \pi^\mp$ (all tag)	$7068 \pm 89$	95%
$D^\pm \rho^\mp$ (all tag)	$4400 \pm 79$	88%

# $B^0 \rightarrow D^{*-} \pi^+$ partial reconstruction

$B^+ \rightarrow D^* \pi^+$  partial reconstruction :

- The decay products of the  $D$  are not reconstructed, but the topology of the prompt (“fast”) pion and that from  $D^{*+} \rightarrow D \pi^+$  decay (“slow”) and 2-body kinematics allow to separate signal from background.
- The presence of a high momentum lepton in the event suppress continuum background.

*Increase efficiency ,  
worse purity*



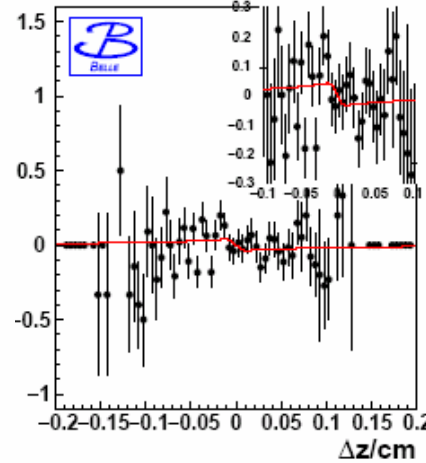
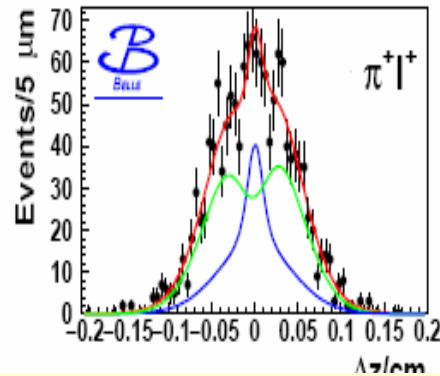
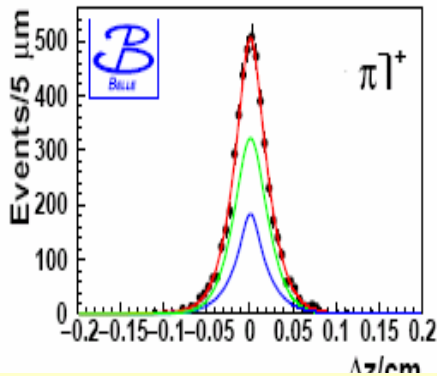
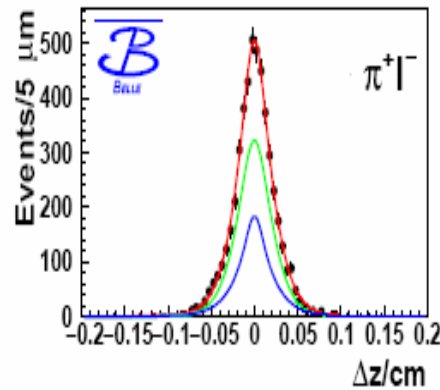
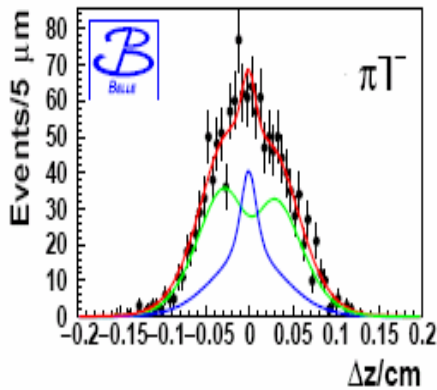
Mode	Data	Signal	$D^* \rho$	Corr. bkg	Uncorr. bkg	S/N
SF ( $\pi_f^\pm \ell_{tag}^\pm$ )	2823	1908	311	—	637	67%
OF ( $\pi_f^\pm \ell_{tag}^\mp$ )	10078	6414	777	928	1836	64%

*helicity angle calculated with  $\pi_{slow}$*

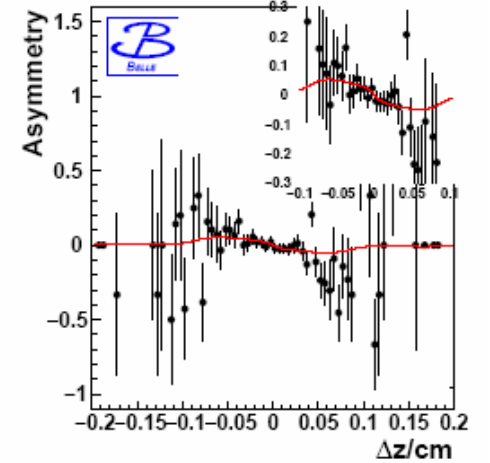
152M  $\bar{B}B$

*partial reconstruction*

*Lepton tag*



$$A^{SF} = \frac{N_{\pi^-\ell^-} - N_{\pi^+\ell^+}}{N_{\pi^-\ell^-} + N_{\pi^+\ell^+}}$$



$$A^{OF} = \frac{N_{\pi^+\ell^-} - N_{\pi^-\ell^+}}{N_{\pi^+\ell^-} + N_{\pi^-\ell^+}}$$

2823 (67%) Same Flavour (mixed)

10078 (64%) Opposite Flavour (unmixed)

$$S^+ = +0.035 \pm 0.041 \pm 0.018$$

$$S^- = +0.025 \pm 0.041 \pm 0.018$$



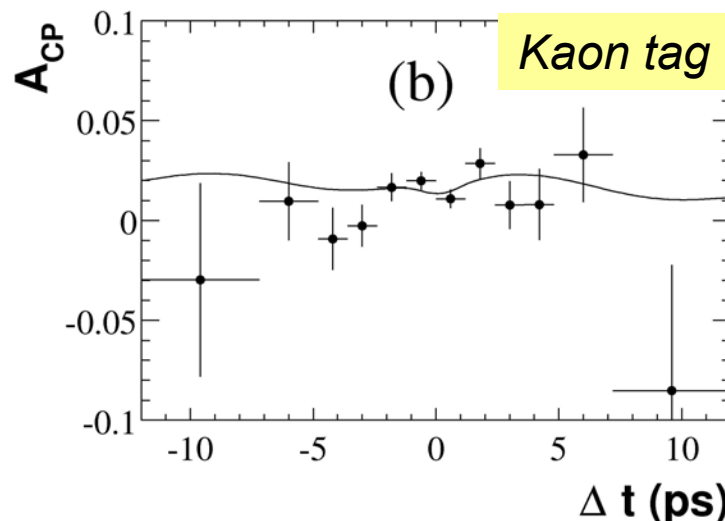
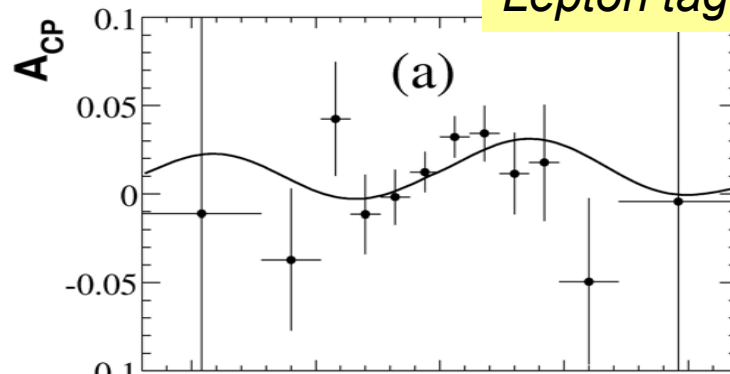
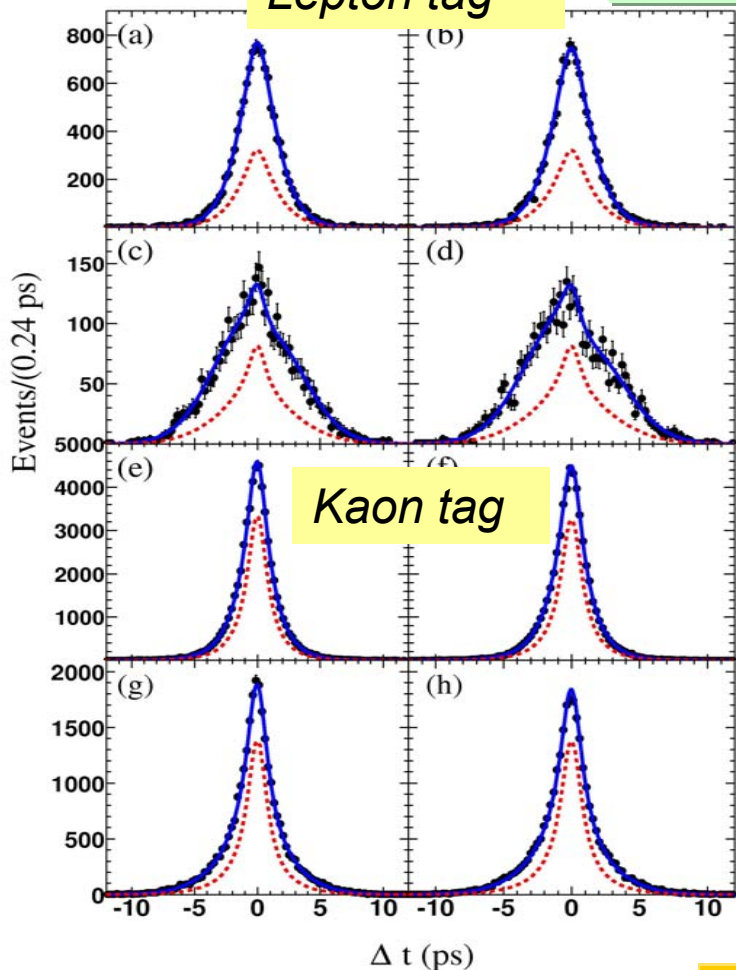
# $B^0 \rightarrow D^{(*)-} \pi^+$

232M  $\bar{B}B$

*partial reconstruction*

Lepton tag

Lepton tag

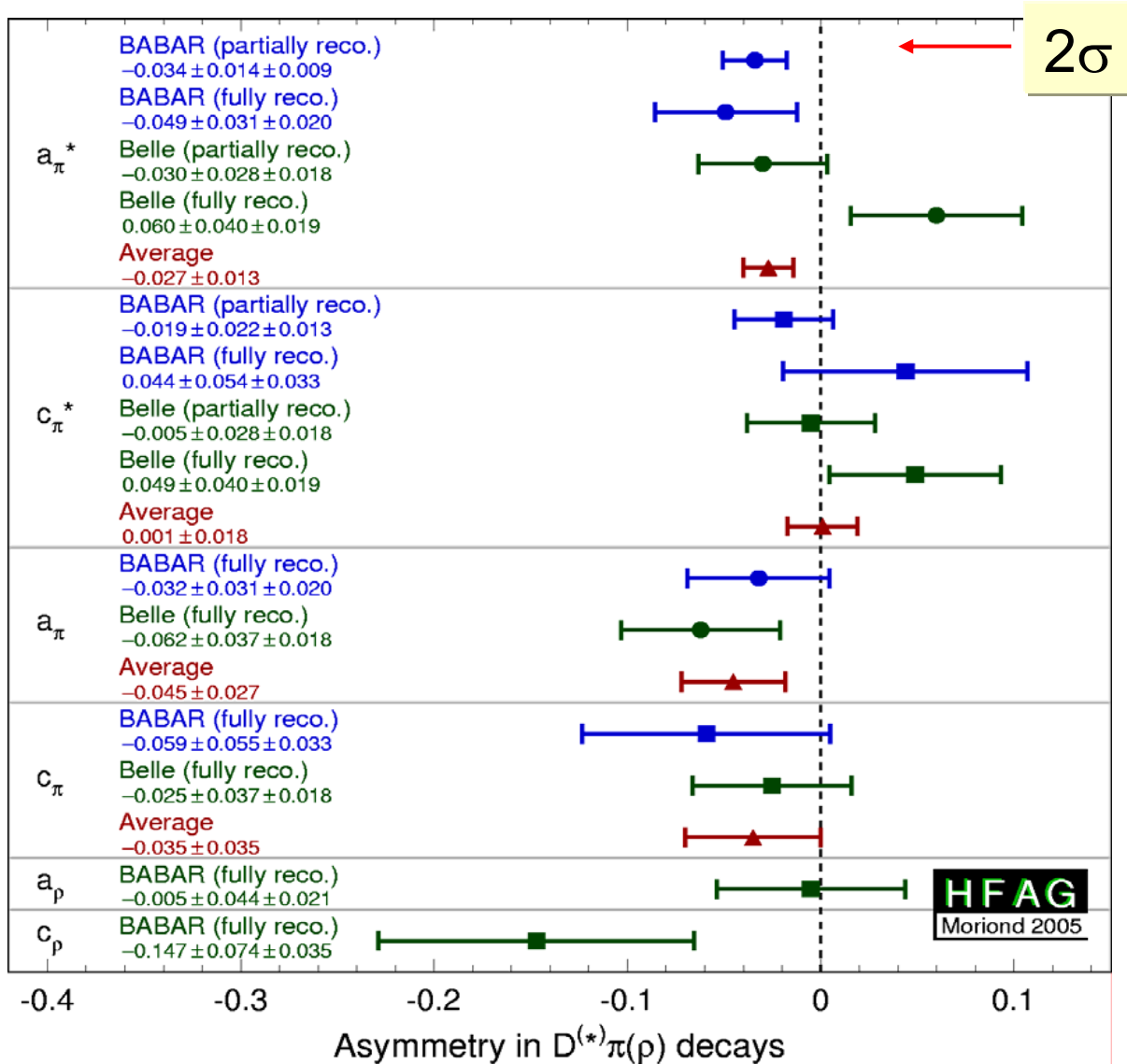


18705 (54%), lepton tag

70584 (31%), Kaon tag

$$2r \sin(2\beta + \gamma) \cos\delta = -0.034 \pm 0.014 \pm 0.009$$

# Asymmetry parameters in $B \rightarrow D^{(*)}\pi(\rho)$



Other modes can be used,  
 e.g.:  $B^0 \rightarrow D^{*\mp} a_1^{\pm}$   
 $B^0 \rightarrow D^{**\mp} \pi^{\pm}$

# Summary and outlook

➤ **Summary:** direct measurements of the 3 angles of the Unitarity Triangle from B-factories;  $\phi_2/\alpha$  and  $\phi_3/\gamma$  consistent with the CKM fits

➤ **Outlook:**

- Other relevant decay modes for  $\phi_3/\gamma$  and  $2\phi_1 + \phi_3/2\beta + \gamma$  have been observed
- More data



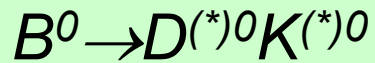
**Good prospects for Super B-factory ...**

# *Backup slides*

# outlook

## ➤ Outlook:

- Other relevant decay modes for  $\phi_3/\gamma$  and  $2\phi_1+\phi_3/2\beta+\gamma$  e.g.:



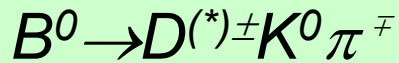
both amplitudes are color suppressed, expect  $r \sim 0.4$



$$Br(B^0 \rightarrow \bar{D}^0 K^{*0}) = (3.08 \pm 0.56 \pm 0.31(\text{sys})) \times 10^{-5}$$

$$Br(B^0 \rightarrow \bar{D}^0 K^0) = (3.72 \pm 0.65 \pm 0.37(\text{sys})) \times 10^{-5}$$

Consistent with old results:  
PRL 90, 141802 (2003)



both amplitudes are color allowed

Time dep. Dalitz plot analysis

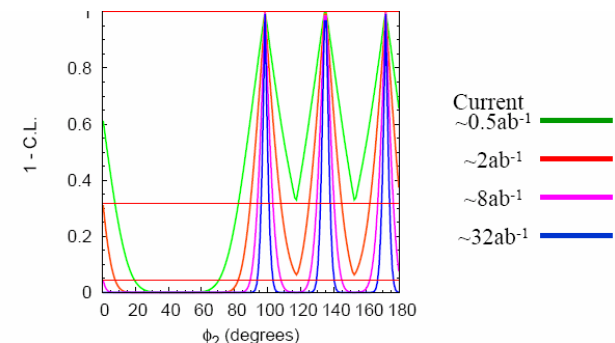
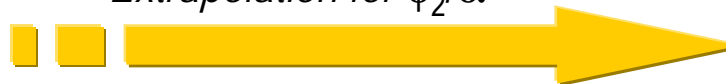


▪ N

$$B(B^0 \rightarrow D^\mp K^0 \pi^\pm) = (4.9 \pm 0.7_{\text{stat}} \pm 0.5_{\text{syst}}) \times 10^{-4}$$

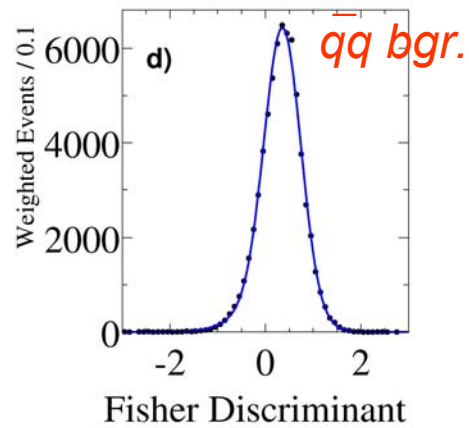
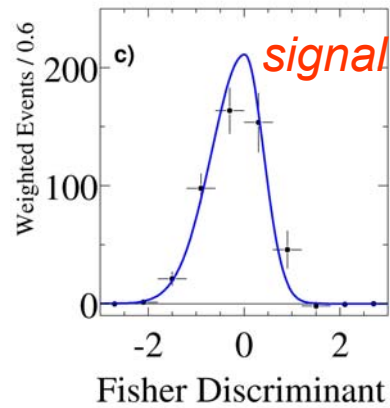
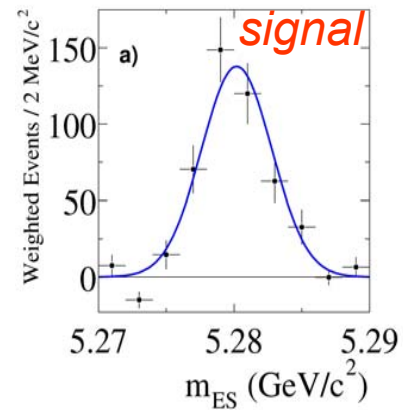
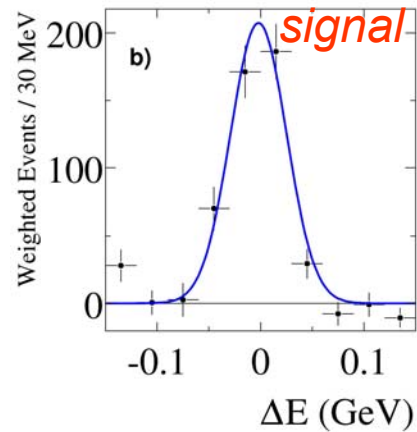
$$B(B^0 \rightarrow D^{*\mp} K^0 \pi^\pm) = (3.0 \pm 0.7_{\text{stat}} \pm 0.3_{\text{syst}}) \times 10^{-4}$$

Extrapolation for  $\phi_2/\alpha$





## Event weighted distributions



$$L_i = (1 - f_{ol}) \int d\Delta t' \{ f_{\pi\pi} P_{\pi\pi} + f_{K\pi} P_{K\pi} \} R_{sig}(\Delta t - \Delta t') + f_{\bar{q}q} P_{\bar{q}q} R_{\bar{q}q}(\Delta t - \Delta t') \} + f_{ol} P_{ol}(\Delta t)$$

Unbinned maximum likelihood fit

$$L_{tot} = \prod L_i(\Delta t, q)$$

$\pi\pi$

$$P_{\pi\pi}(\Delta t, q; A_{\pi\pi}, S_{\pi\pi}) = \frac{\exp(-|\Delta t|/\tau_{B^0})}{4\tau_{B^0}} \{ 1 - q\Delta w + q(1-2w)[A_{\pi\pi} \cos \Delta m \Delta t + S_{\pi\pi} \sin \Delta m \Delta t] \}$$

from data

2 fit parameters

$K\pi$

$P_{K\pi}(\Delta t, q)$ :

$$S_{K\pi} = 0, A_{K\pi} = A_{K\pi}^{eff} = \frac{A_{K\pi}^{CP} + A_\varepsilon}{1 + A_{K\pi}^{CP} A_\varepsilon},$$

$$A_\varepsilon = \frac{p(K^- \rightarrow \pi^-) \varepsilon_{\pi^+} - p(K^+ \rightarrow \pi^+) \varepsilon_{\pi^-}}{p(K^- \rightarrow \pi^-) \varepsilon_{\pi^+} + p(K^+ \rightarrow \pi^+) \varepsilon_{\pi^-}} \text{HFAG'04}$$

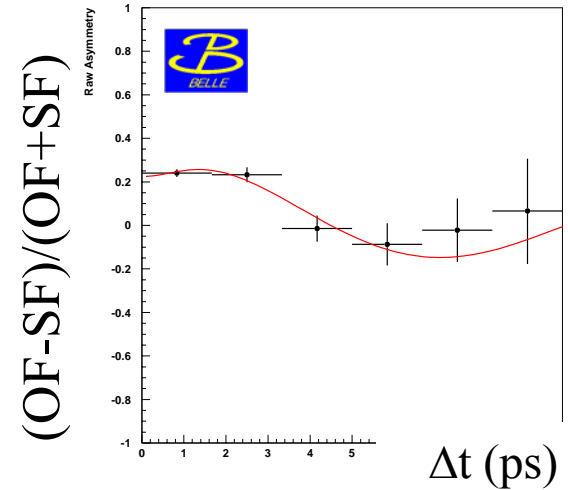
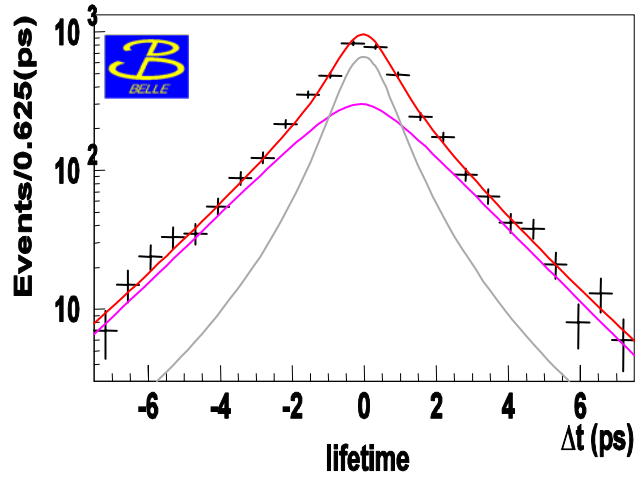
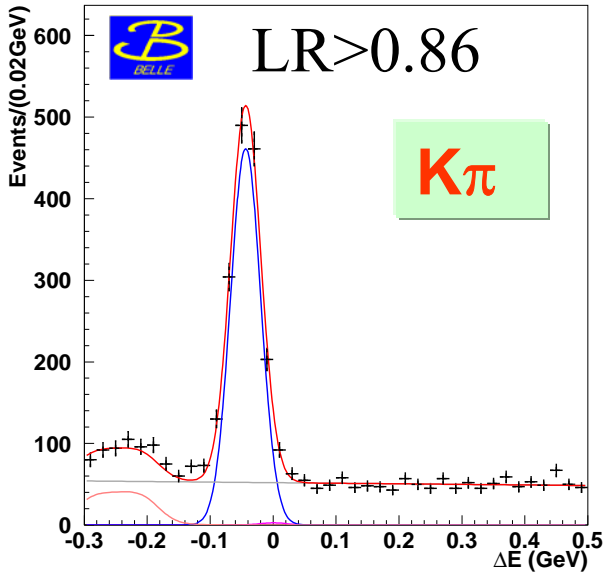
$$A_{K\pi}^{CP} = -0.109 \pm 0.019$$

$\bar{q}q$

$P_{\bar{q}q}(\Delta t, q)$ :

from sideband

# Validity checks



similar topology to  $B^0 \rightarrow \pi^+ \pi^-$

$B$  BELLE  $\tau_{B^0} = 1.52 \pm 0.04 \text{ ps}$

$\Delta m = 0.46 \pm 0.03 \text{ ps}^{-1}$

$B$  BELLE  $\tau_{B^0} = 1.50 \pm 0.07 \text{ ps}$

$\pi\pi$  sample



$\tau_{B^0} = 1.60 \pm 0.04 \text{ ps}, \Delta m_d = 0.523 \pm 0.028 \text{ ps}^{-1}$

WA

$\tau_{B^0} = 1.536 \pm 0.014 \text{ ps}, \Delta m_d = 0.502 \pm 0.007 \text{ ps}^{-1}$

.... many other checks

# SYSTEMATICS



	$S_{\pi\pi}$	$C_{\pi\pi}$
<b>B-flavor identification</b>	<b><math>\pm 0.005</math></b>	<b><math>\pm 0.015</math></b>
$\tau_{B0}$ and $\Delta m_d$	<b><math>\pm 0.001</math></b>	<b><math>\pm 0.004</math></b>
<b>PDF parameters</b>	<b><math>\pm 0.017</math></b>	<b><math>\pm 0.018</math></b>
<b>Potential bias</b>	<b><math>\pm 0.013</math></b>	<b><math>\pm 0.007</math></b>
<b>SVT alignment</b>	<b><math>\pm 0.010</math></b>	<b><math>\pm 0.002</math></b>
<b>Beam spot</b>	<b><math>\pm 0.010</math></b>	<b><math>\pm 0.010</math></b>
<b>Tag-side interference</b>	<b><math>\pm 0.008</math></b>	<b><math>\pm 0.023</math></b>
<b>total</b>	<b><math>\pm 0.027</math></b>	<b><math>\pm 0.035</math></b>

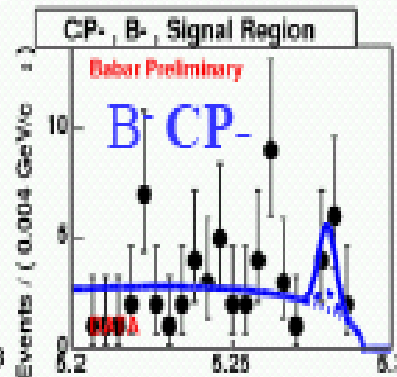
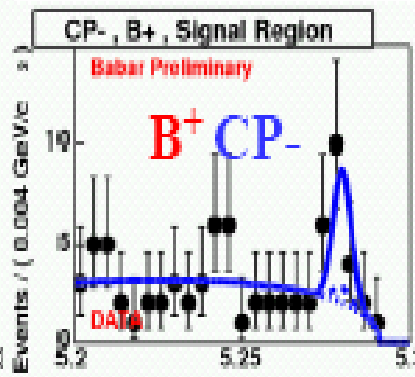
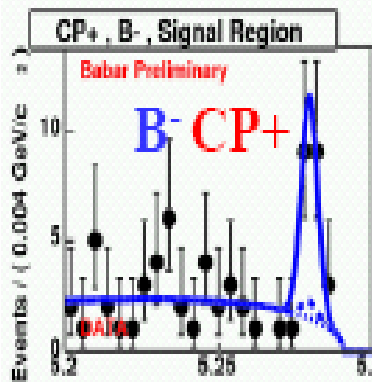
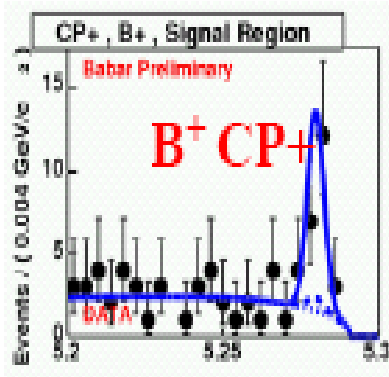


	$S_{\pi\pi}$	$A_{\pi\pi}$
<b>wrong tag</b>	<b><math>\pm 0.01</math></b>	<b><math>\pm 0.01</math></b>
<b>physics param.</b>	<b><math>&lt; 0.01</math></b>	<b><math>\pm 0.01</math></b>
<b>resolution func</b>	<b><math>\pm 0.04</math></b>	<b><math>\pm 0.01</math></b>
<b>bkg Dt shape</b>	<b><math>&lt; 0.01</math></b>	<b><math>&lt; 0.01</math></b>
<b>event fraction</b>	<b><math>\pm 0.02</math></b>	<b><math>\pm 0.04</math></b>
<b>fit bias</b>	<b><math>\pm 0.01</math></b>	<b><math>\pm 0.01</math></b>
<b>vertexing</b>	<b><math>\pm 0.04</math></b>	<b><math>+0.03</math> <math>-0.01</math></b>
<b>tag side interfere</b>	<b><math>\pm 0.01</math></b>	<b><math>+0.02</math> <math>-0.04</math></b>
<b>total</b>	<b><math>\pm 0.06</math></b>	<b><math>\pm 0.06</math></b>



$D_{CP}^0 K^{*-} (K^{*-} \rightarrow K_S \pi^-)$

$K_S \phi, K_S \omega, K_S \pi^0$



$CP+ = 34.4 \pm 6.9$

$N_{BB} = 227 \cdot 10^6$

$CP- = 15.1 \pm 5.8$

$B^\pm \rightarrow D_{CP} K^{*\pm}$

$R_{CP+} = 1.73 \pm 0.36(stat.) \pm 0.12(syst.)$

$R_{CP-} = 0.76 \pm 0.29(stat.) \pm 0.06(syst.)^{+0.04}_{-0.14}$

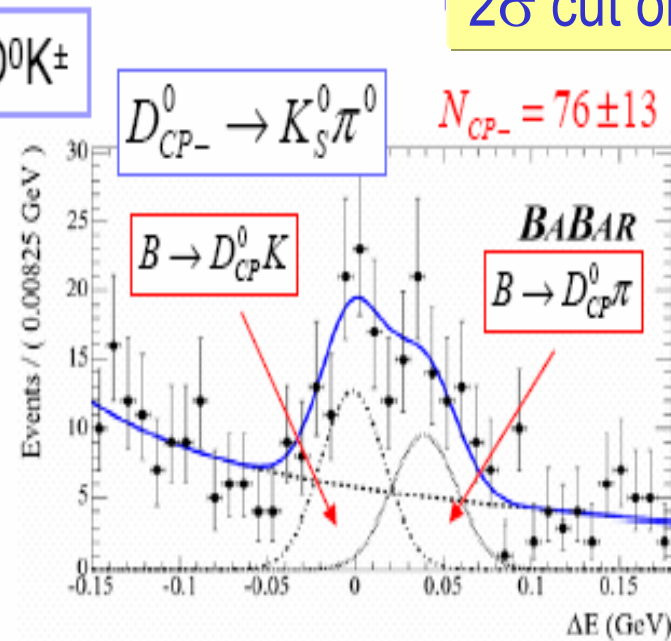
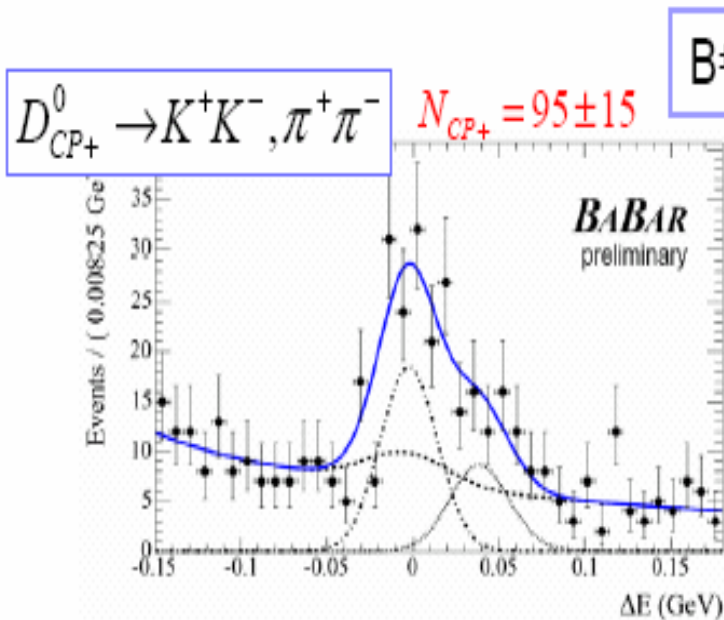
$A_{CP+} = -0.09 \pm 0.20(stat.) \pm 0.06(syst.)$

$A_{CP-} = -0.33 \pm 0.34(stat.) \pm 0.10(syst.)$

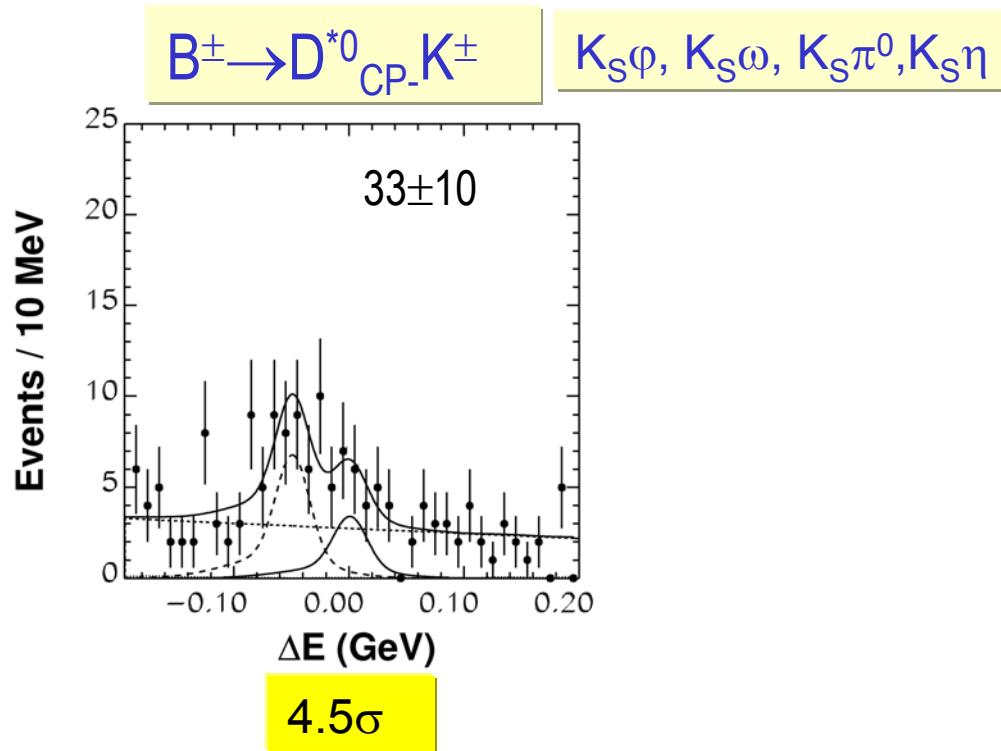
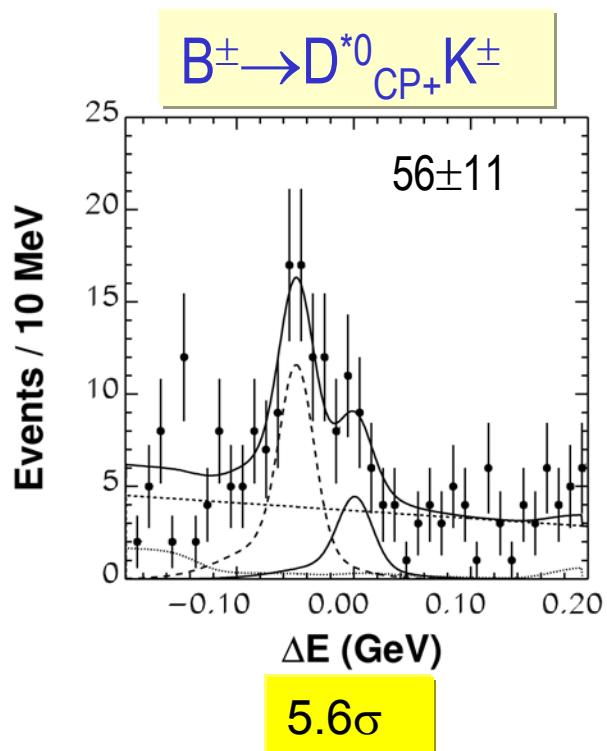
$(+0.15 \pm 0.1)(A_{CP-} - A_{CP+})$



$2\sigma$  cut on  $\theta_c$



$B^\pm \rightarrow D_{CP} K^\pm$ 214M	$R_{CP+} = 0.87 \pm 0.14(stat.) \pm 0.06(syst.)$	$R_{CP-} = 0.80 \pm 0.14(stat.) \pm 0.08(syst.)$
	$A_{CP+} = 0.40 \pm 0.15(stat.) \pm 0.08(syst.)$	$A_{CP-} = 0.21 \pm 0.17(stat.) \pm 0.07(syst.)$



$$B^\pm \rightarrow D_{CP}^{*0} K^\pm$$

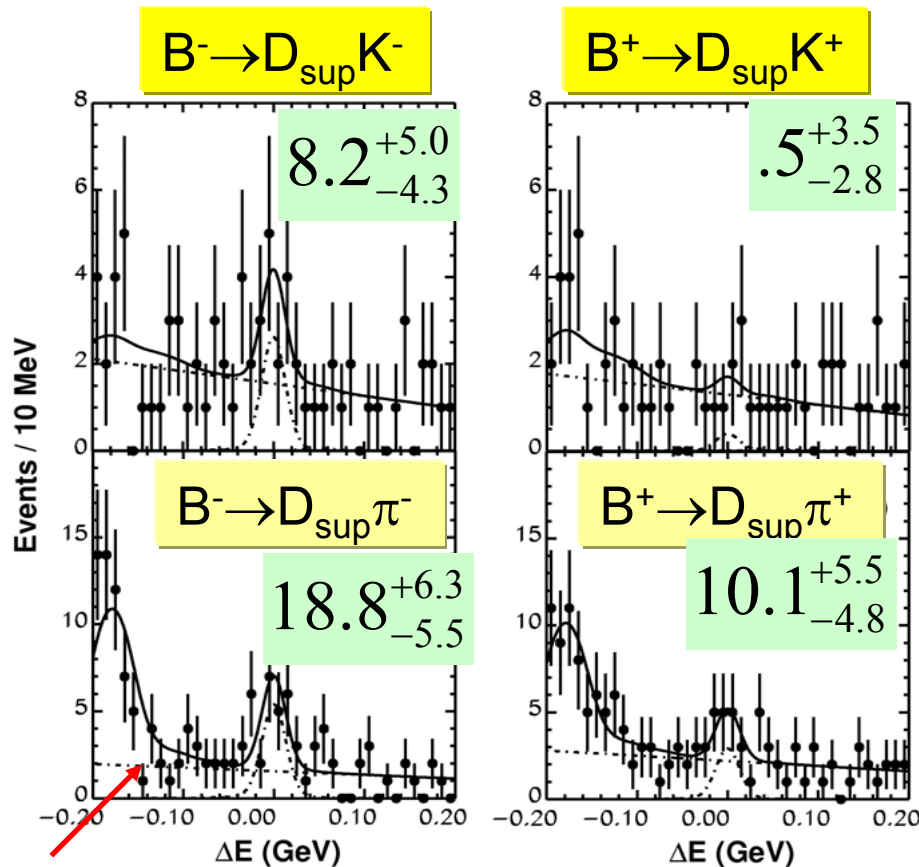
$$D^{*0} \rightarrow D_{CP} \pi^0$$

$$R_{CP+} = 1.43 \pm 0.28(\text{stat.}) \pm 0.06(\text{syst.})$$

$$R_{CP-} = 0.94 \pm 0.28(\text{stat.}) \pm 0.06(\text{syst.})$$

$$A_{CP+} = -0.27 \pm 0.25(\text{stat.}) \pm 0.04(\text{syst.})$$

$$A_{CP-} = 0.26 \pm 0.26(\text{stat.}) \pm 0.03(\text{syst.})$$



$$A_{DK} = .88^{+0.77}_{-0.62} \pm 0.1(\text{sys})$$

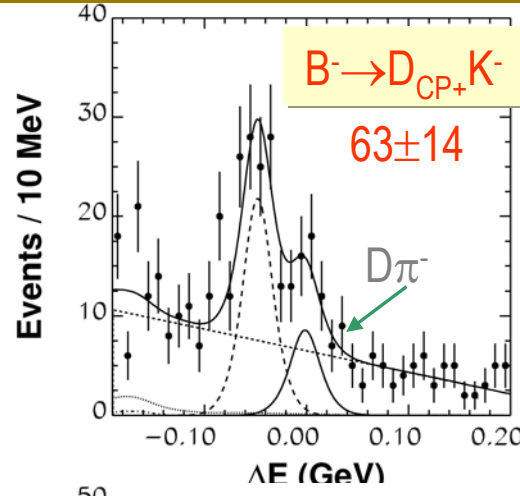
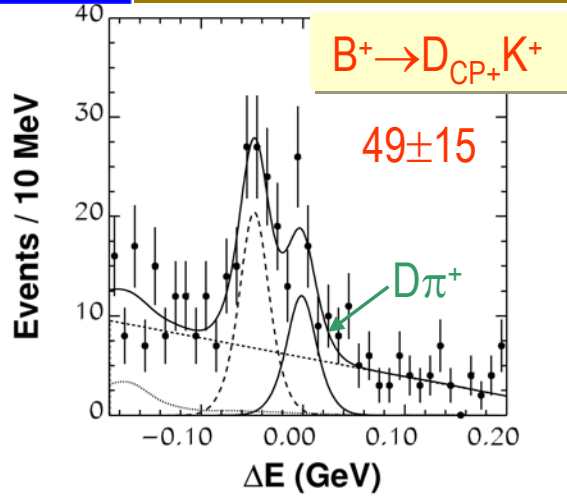
$$R_{DK} = 2.3^{+1.6}_{-1.4} \pm 0.1(\text{sys}) \times 10^{-2}$$

$$A_{D\pi} = .30^{+0.29}_{-0.25} \pm 0.06(\text{sys})$$

$$R_{D\pi} = 3.5^{+1.0}_{-0.9} \pm 0.2(\text{sys}) \times 10^{-3}$$

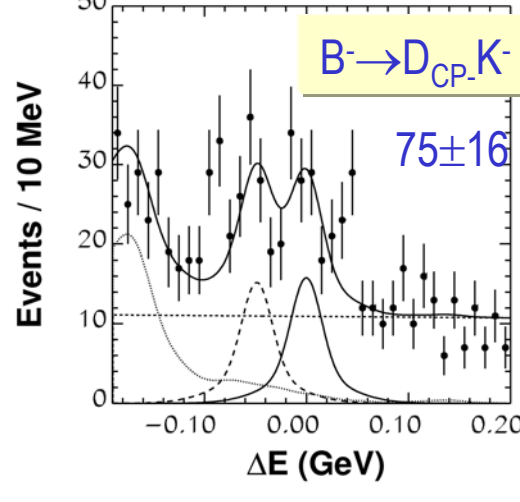
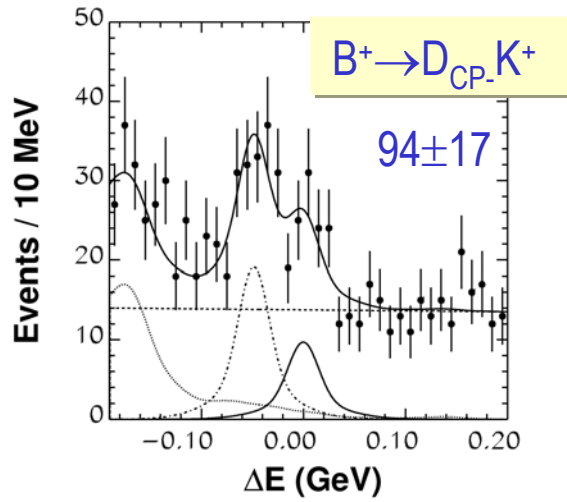
*First observation*

$$r_B < 0.27 \text{ (90\%CL)}$$

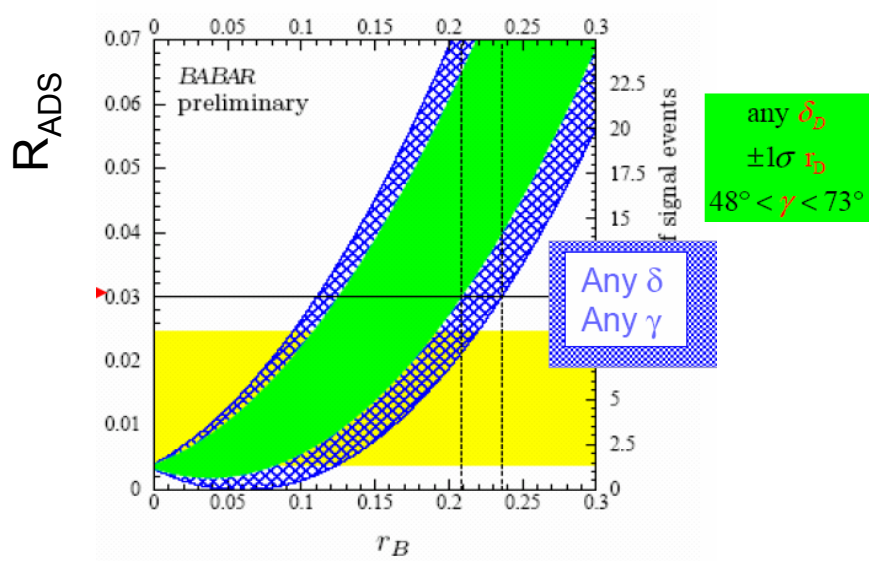


$B^\pm \rightarrow D_{CP} K^\pm$

$R_{CP^+} = 0.98 \pm 0.18(stat.) \pm 0.10(syst.)$   
 $A_{CP^+} = 0.07 \pm 0.14(stat.) \pm 0.06(syst.)$

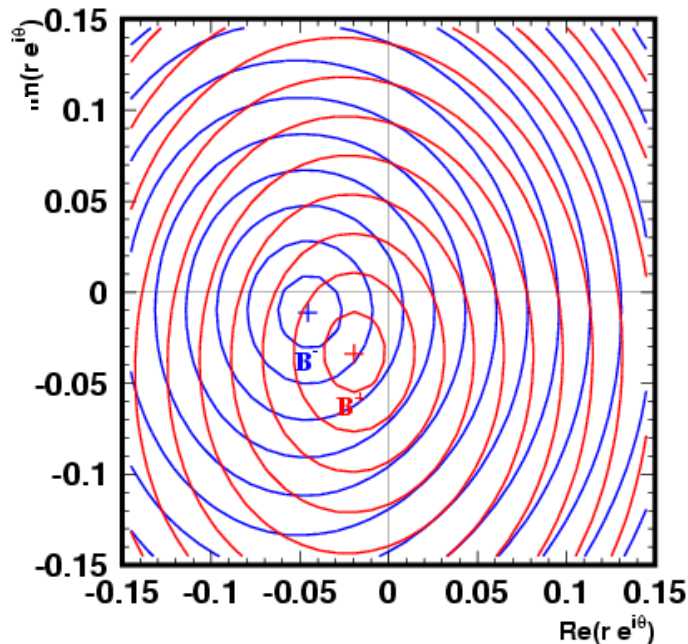


$R_{CP^-} = 1.29 \pm 0.16(stat.) \pm 0.08(syst.)$   
 $A_{CP^-} = -0.11 \pm 0.14(stat.) \pm 0.05(syst.)$



# Test sample fit

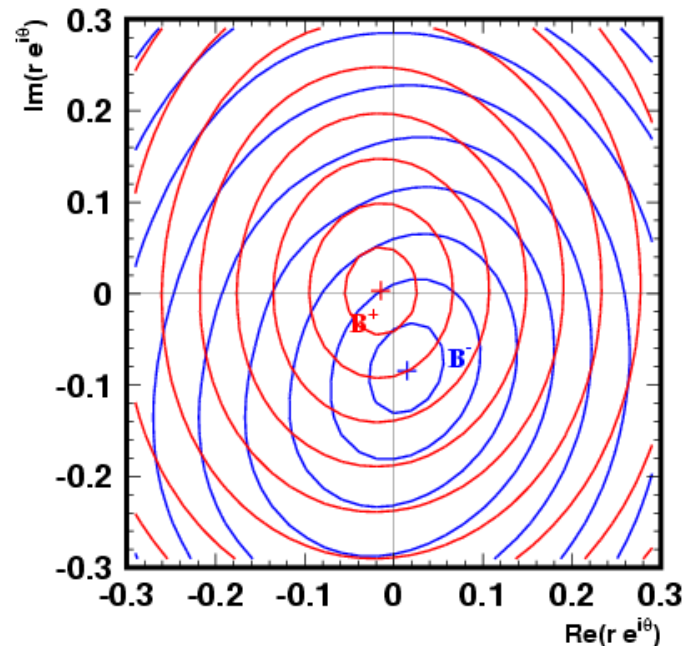
$B^+ \rightarrow D^0 \pi^+$  (3425 events)



$$r_+ = 0.039 \pm 0.021, \theta_+ = 240 \pm 28^\circ$$

$$r_- = 0.047 \pm 0.018, \theta_- = 193 \pm 24^\circ$$

$B^+ \rightarrow D^{*0} \pi^+$  (642 events)



$$r_+ = 0.015 \pm 0.042, \theta_+ = 169 \pm 186^\circ$$

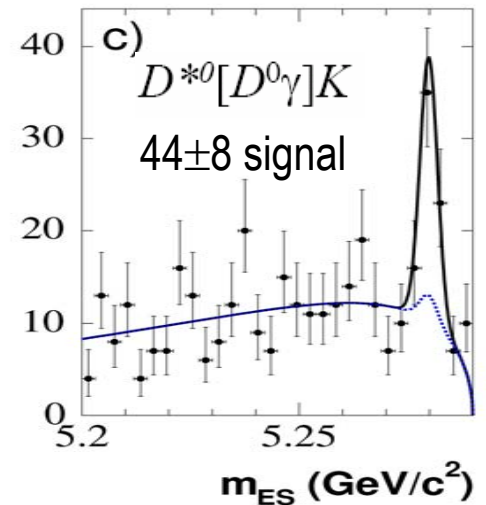
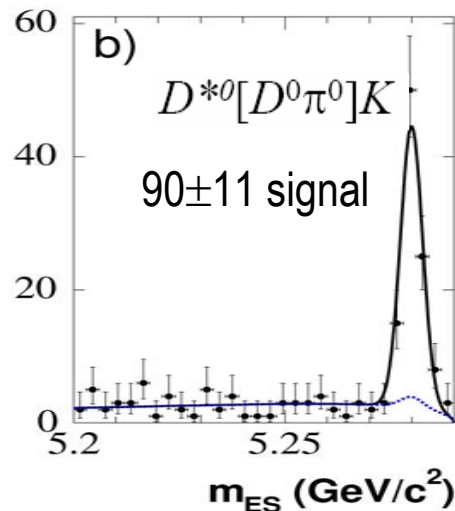
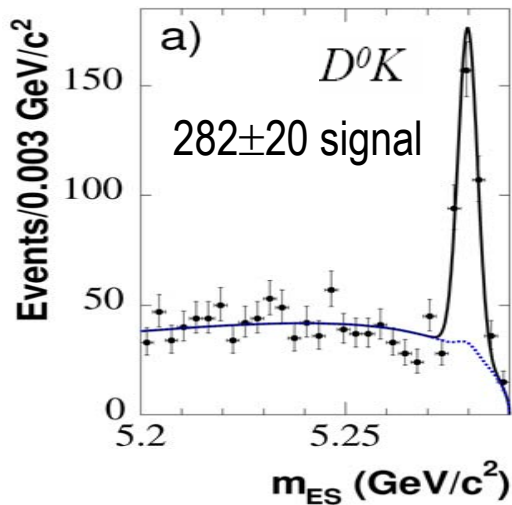
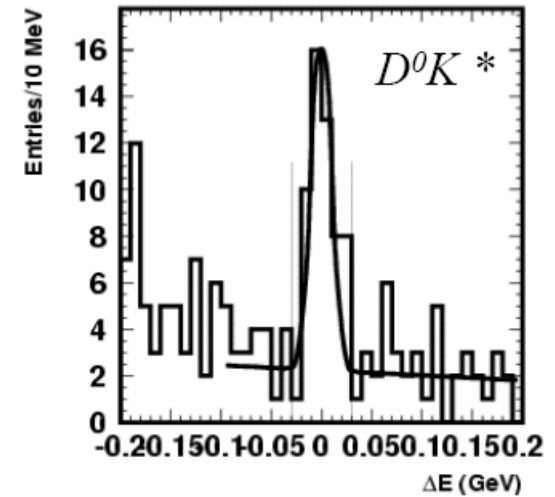
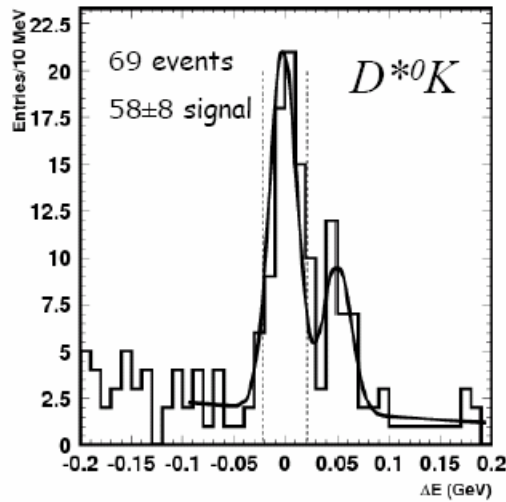
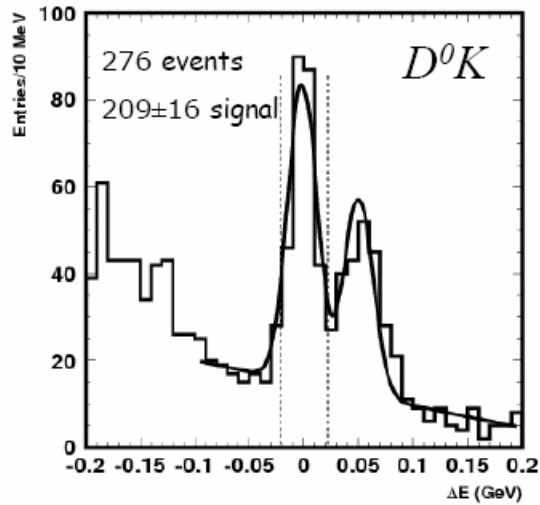
$$r_- = 0.086 \pm 0.049, \theta_- = 280 \pm 30^\circ$$

Expect  $r \sim 0.01-0.02$

$$x_+ = r_B \cos(\delta + \gamma) \quad x_- = r_B \cos(\delta - \gamma)$$

$$y_+ = r_B \sin(\delta + \gamma) \quad y_- = r_B \sin(\delta - \gamma)$$

# $B^\pm \rightarrow D^{(*)0} K^{(*)\pm}, D^0 \rightarrow K_S \pi^+ \pi^-$ signals

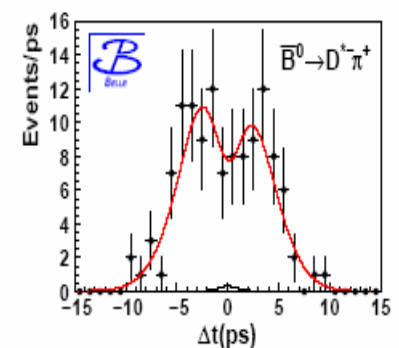
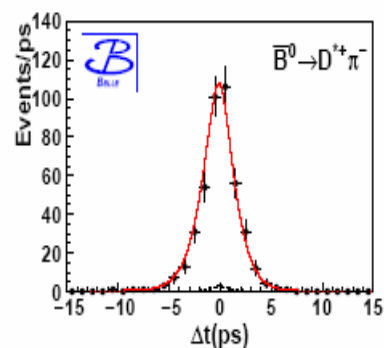
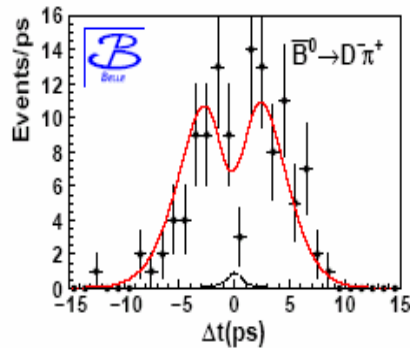
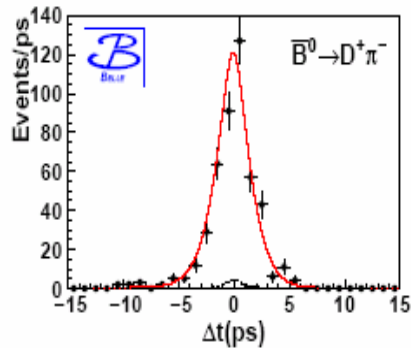
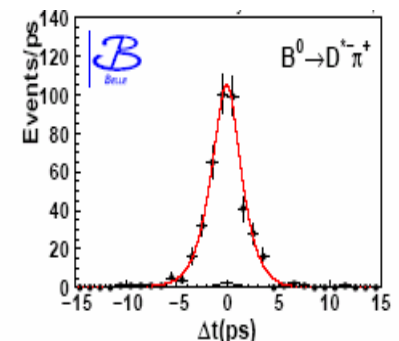
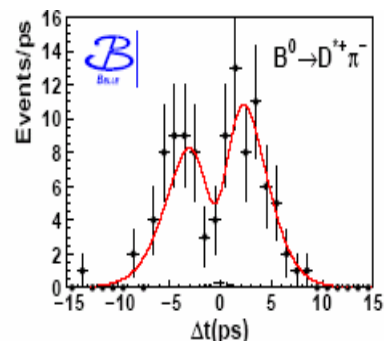
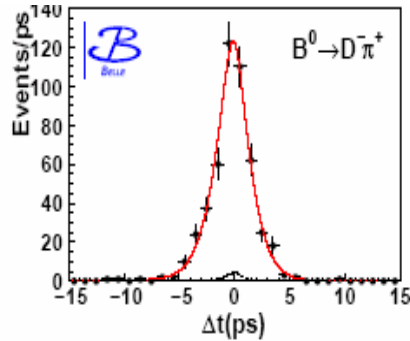
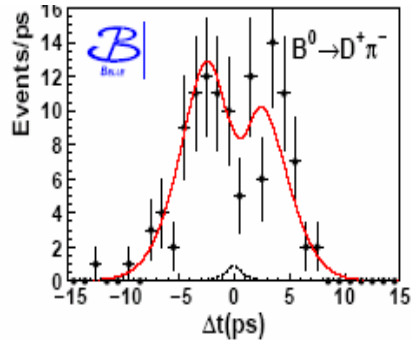


152M  $\bar{B}B$

$D\pi$

*exclusive reconstruction*

$D^*\pi$



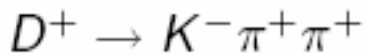
$$S^+ = +0.087 \pm 0.054 \pm 0.018$$

$$S^- = +0.037 \pm 0.052 \pm 0.018$$

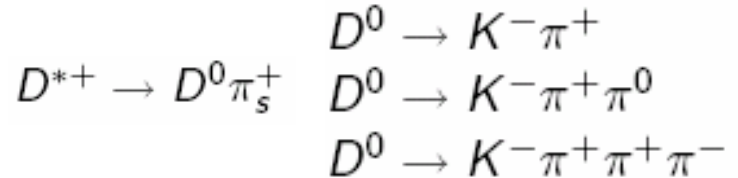
$$S^+ = -0.109 \pm 0.057 \pm 0.019$$

$$S^- = -0.011 \pm 0.057 \pm 0.019$$

9351 events, purity 91%



7763 events, purity 96%





# Babar $B^0 \rightarrow D^{(*)-} \pi^+ / \rho^+$ results hep-ex/0408059

110M  $\bar{B}B$

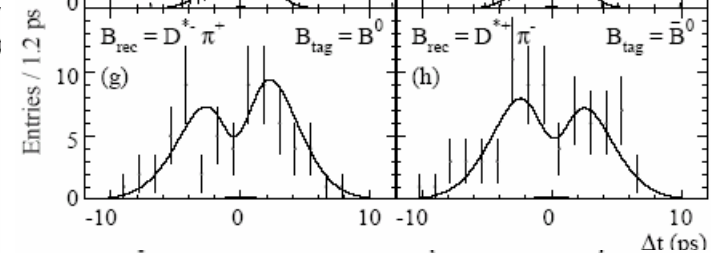
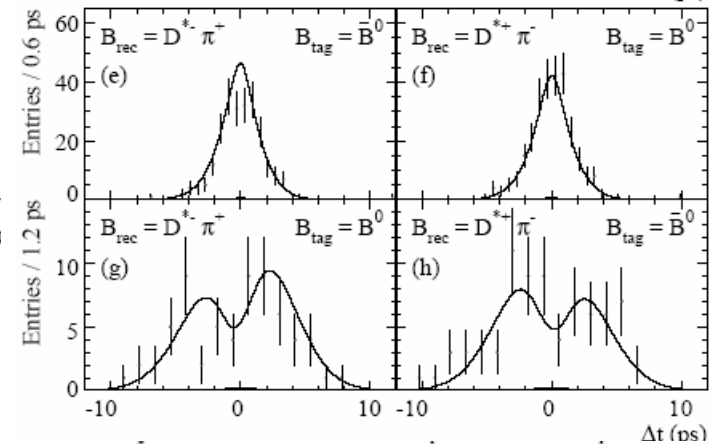
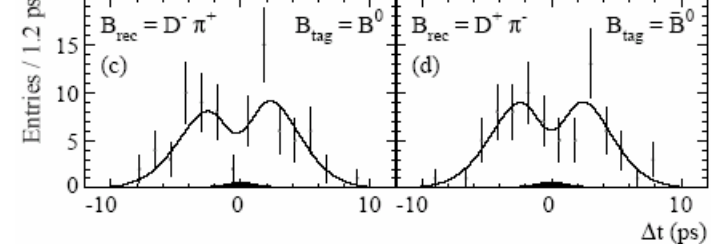
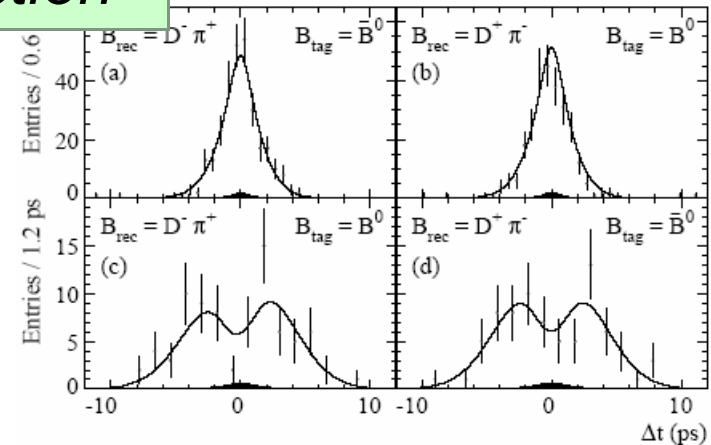
*exclusive reconstruction*

*abc parametrization*

$$\begin{aligned}
 a &= 2r \sin(2\beta + \gamma) \cos \delta \\
 b &= 2r' \sin(2\beta + \gamma) \cos \delta' \\
 c &= 2 \cos(2\beta + \gamma) (r \sin \delta - r' \sin \delta')
 \end{aligned}$$

*Simultaneous fit to all decay modes and tagging categories*

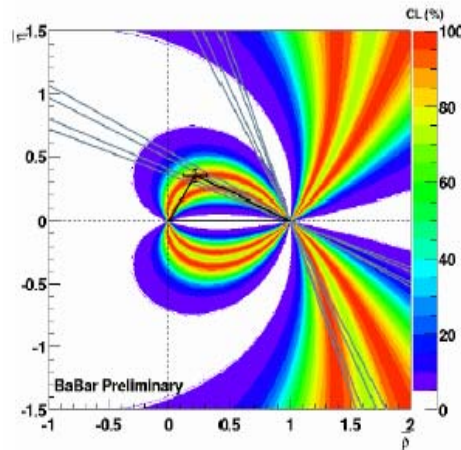
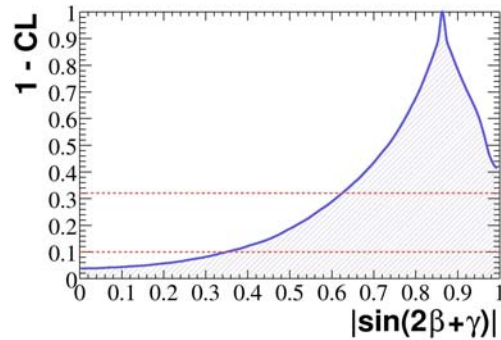
$$\begin{aligned}
 2r^{D\pi} \sin(2\beta + \gamma) \cos \delta^{D\pi} &= -0.032 \pm 0.031 \pm 0.020 \\
 2r^{D\pi} \cos(2\beta + \gamma) \sin \delta^{D\pi} &= -0.059 \pm 0.055 \pm 0.033 \\
 2r^{D^*\pi} \sin(2\beta + \gamma) \cos \delta^{D^*\pi} &= -0.049 \pm 0.031 \pm 0.020 \\
 2r^{D^*\pi} \cos(2\beta + \gamma) \sin \delta^{D^*\pi} &= +0.044 \pm 0.054 \pm 0.033 \\
 2r^{D\rho} \sin(2\beta + \gamma) \cos \delta^{D\rho} &= -0.005 \pm 0.044 \pm 0.021 \\
 2r^{D\rho} \cos(2\beta + \gamma) \sin \delta^{D\rho} &= -0.147 \pm 0.074 \pm 0.035
 \end{aligned}$$



$D^\pm \pi^\mp$ (all tag)	$7611 \pm 97$	91%
$D^{*\pm} \pi^\mp$ (all tag)	$7068 \pm 89$	95%
$D^\pm \rho^\mp$ (all tag)	$4400 \pm 79$	88%

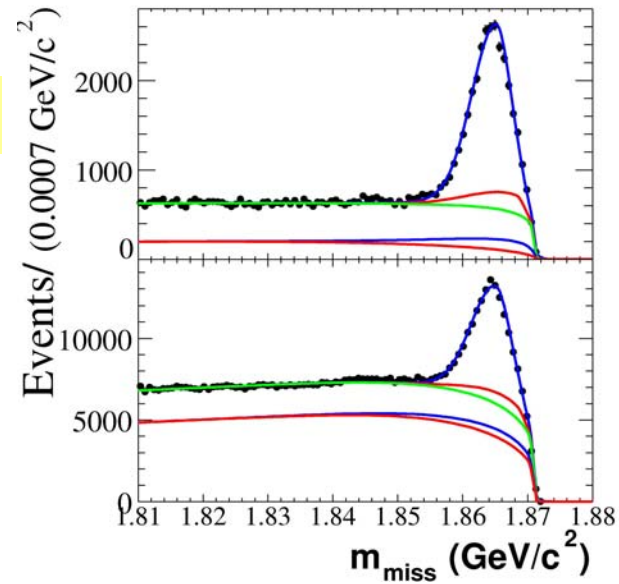
*SU(3) flavor symmetry:*

$$r_{D^* \pi} = \sqrt{\frac{Br(B^0 \rightarrow D_s^{*+} \pi^-)}{Br(B^0 \rightarrow D^{*-} \pi^+)}} \frac{f_{D^*}}{f_{D_s^*}} \tan \theta_C = 0.015^{+0.004}_{-0.006}$$



Lepton tag

Kaon tag



— Continuum  
— peaking BB  
— Combinatoric BB  
—  $D^*\rho$