
B Hadron Lifetimes at DØ

Claus Peter Buszello
for the DØ Collaboration



Imperial College
London



The DØ Detector

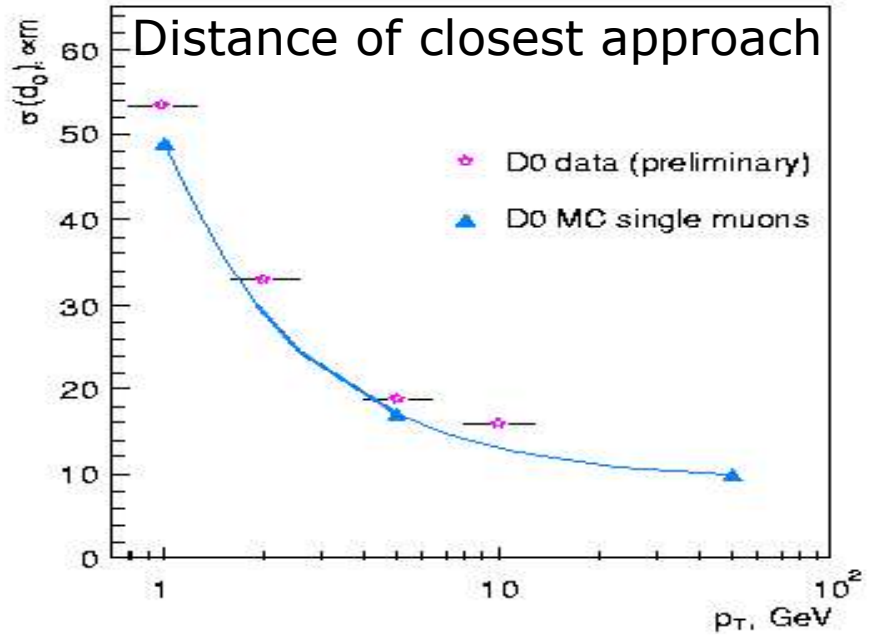
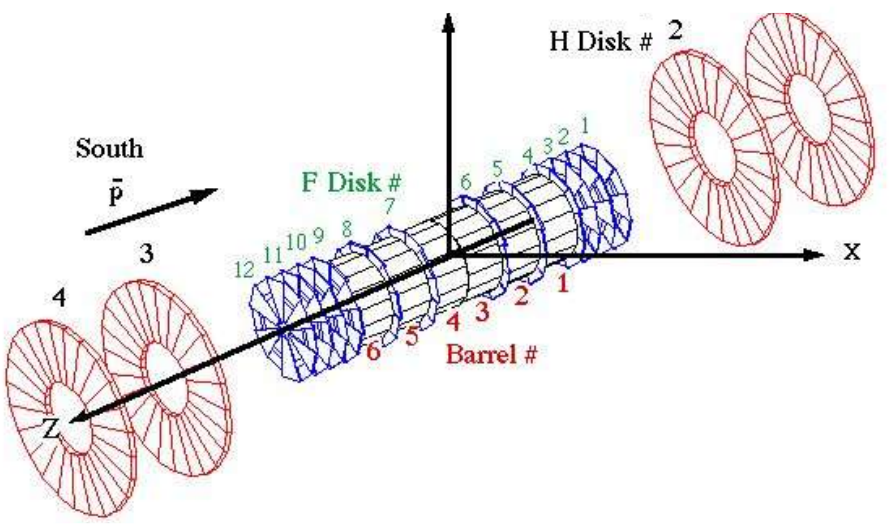
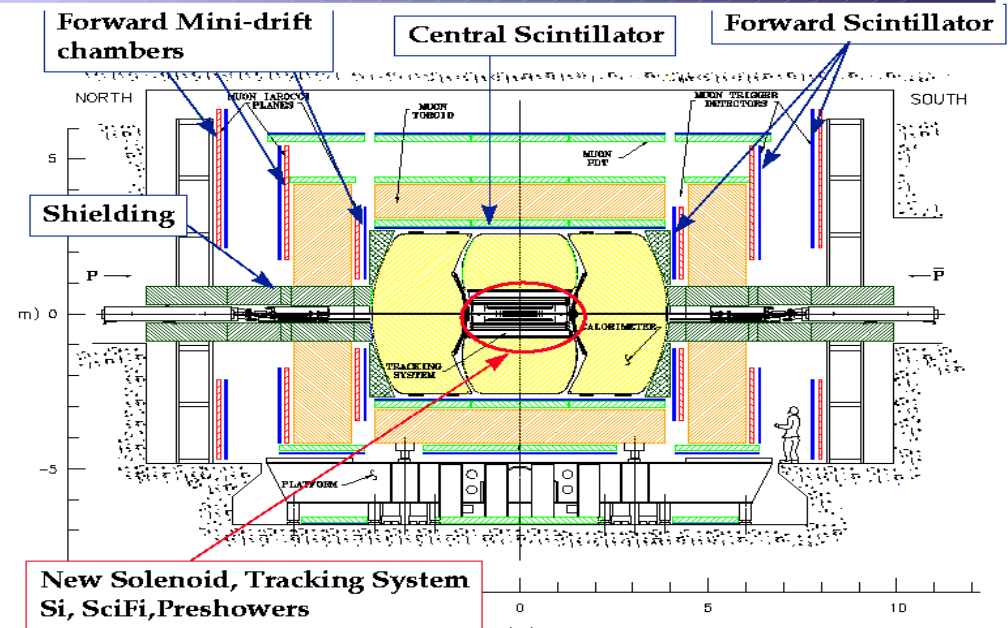
Clean muon ID at $|\eta| < 2$

Compact tracker:

- Central fibre tracker (CFT)
- Silicon microstrip tracker (SMT)

Trigger system:

- Level 1 – Hardware -> 1.5 kHz
- Level 2 – Hardware -> 800 Hz
- Level 3 – Software -> 50 Hz



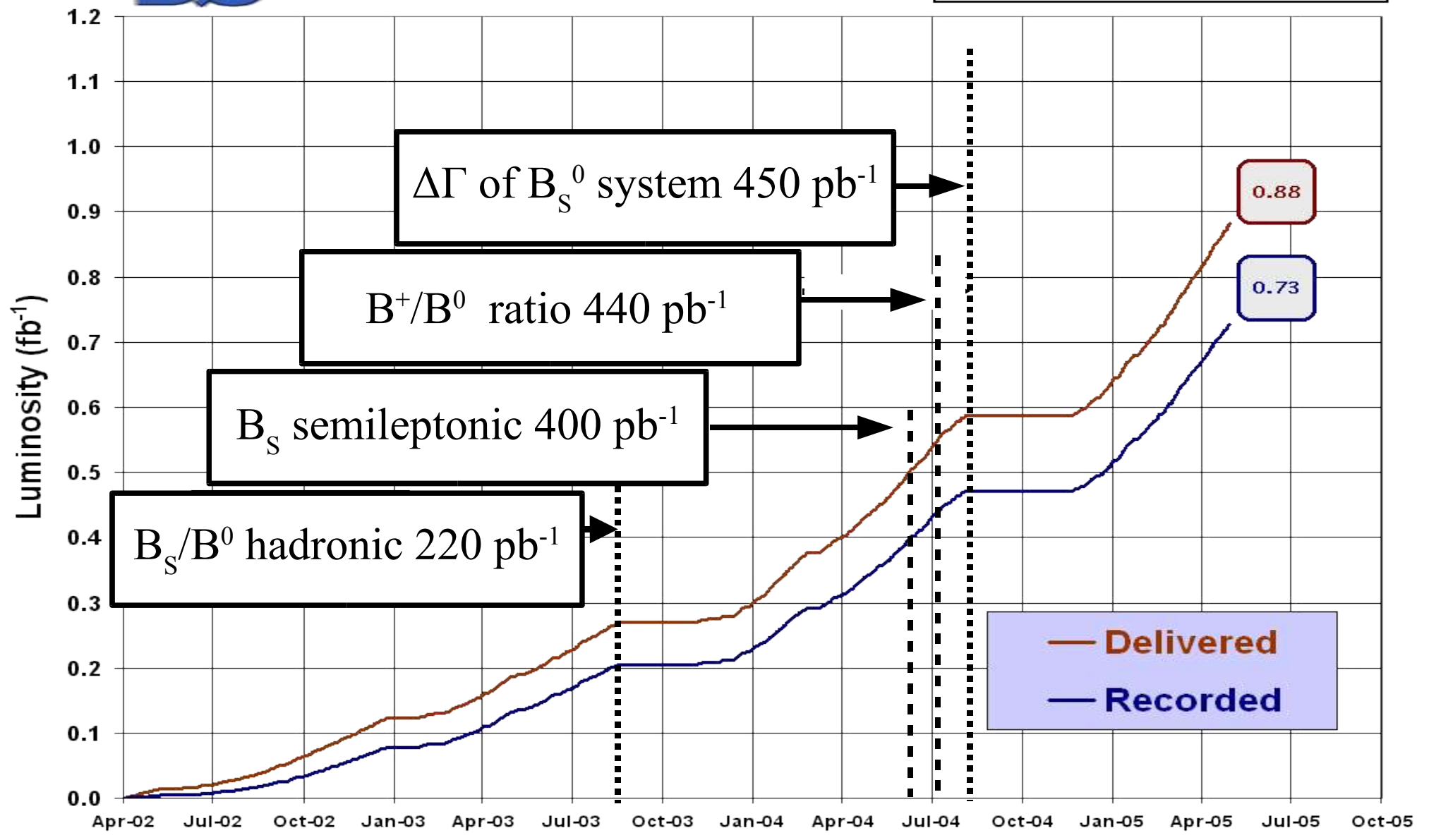


Data Collected



Run II Integrated Luminosity

19 April 2002 - 17 May 2005





Transverse decay length

Far better resolution in XY only:

$$L = c\tau\beta\gamma = c\tau \frac{p}{m} \Rightarrow L_{XY} = c\tau \frac{p_T}{m}$$

Lifetime fits

Simultaneous unbinned likelihood fit to mass and lifetime distributions:

$$L = \prod_i^N [f_{sig} F_{sig}^i + (1 - f_{sig}) F_{bg}^i]$$

Visible proper decay length (VPDL)

If neutrinos present in decay use P_T of visible decay products

K-factors

Use MC to find correction factor for VPDL

$$K = \frac{P_T(D_S \mu)}{P_T(B_S)}$$

Triggers

B-physics events triggered by well understood muon triggers

Typical crosschecks

Divide data into different kinematic regions; MC ensemble tests;
Bias tests by varying measured value in MC input



- 1. B^+ / B^0 lifetime ratio**
- 2. Exclusive hadronic decay modes**
 - $B_s \rightarrow J/\psi \phi$ lifetime
 - $B^0 \rightarrow J/\psi K^{*0}$ lifetime
 - B_s / B^0 lifetime ratio
 - $\Lambda_B \rightarrow J/\psi \Lambda^0$ lifetime and ratio
- 3. B_s semileptonic decay**
 - $B_s \rightarrow D_s^- \mu^+ \nu X$ lifetime
- 4. B_s lifetime difference**
 - $\Delta\Gamma/\Gamma$



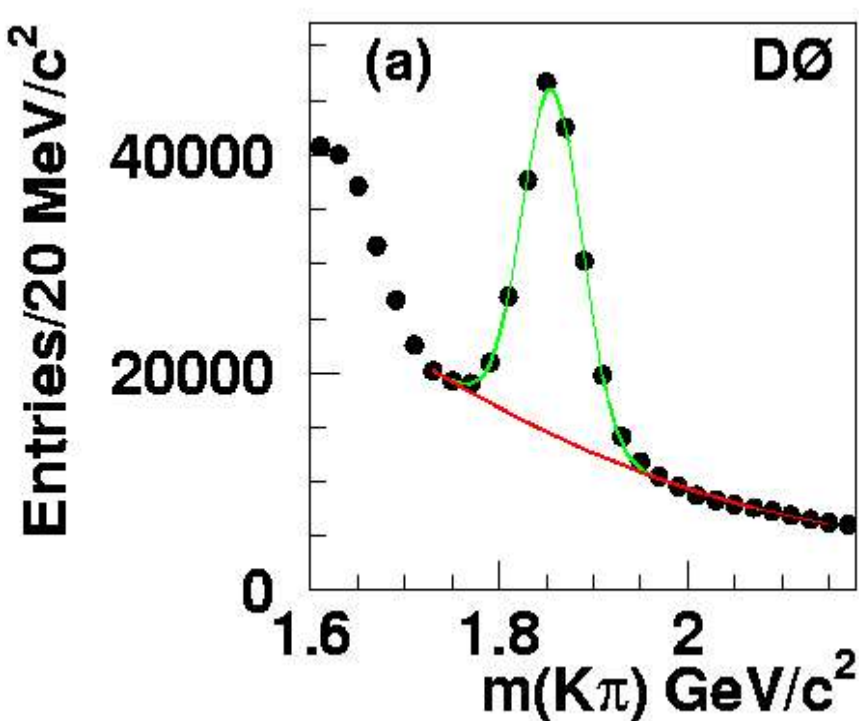
B⁺/B⁰ Lifetime Ratio

→ Ratio is a good precision variable:

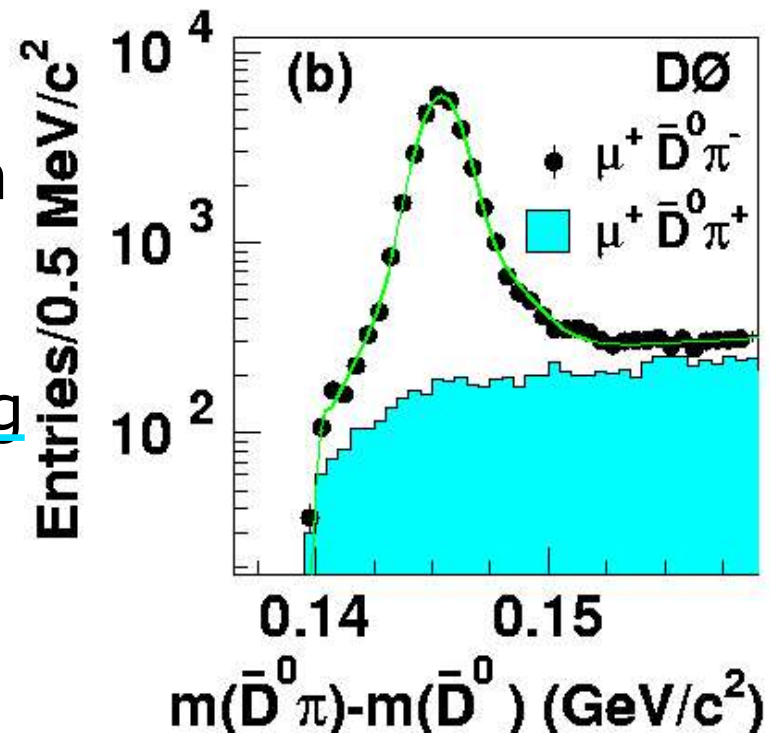
- Precise theoretical prediction from HQE : $\tau(B^+)/\tau(B^0) = 1.06 \pm 0.02$
- Systematics cancel if channels chosen well.

$$B^+ \rightarrow \mu^+ \nu \mathbf{D}^0 X \quad (\mathbf{D}^0 \rightarrow K\pi)$$

$$B^0 \rightarrow \mu^+ \nu D^{*-} X \rightarrow \mu^+ \nu \mathbf{D}^0 \pi^- X$$



find slow pion
 →
 classify into
right or wrong
 signed





B⁺/B⁰ Ratio Results

Unusal approach:

if lifetimes are *equal*, ratio of B⁺ and B⁰ events *constant* in VPDL
=> Fit ratio of number of events:

$$\min \chi^2(\epsilon, k) = \sum_i \frac{(r_i - r_i^e(\epsilon, k))^2}{\sigma^2(r_i)}$$

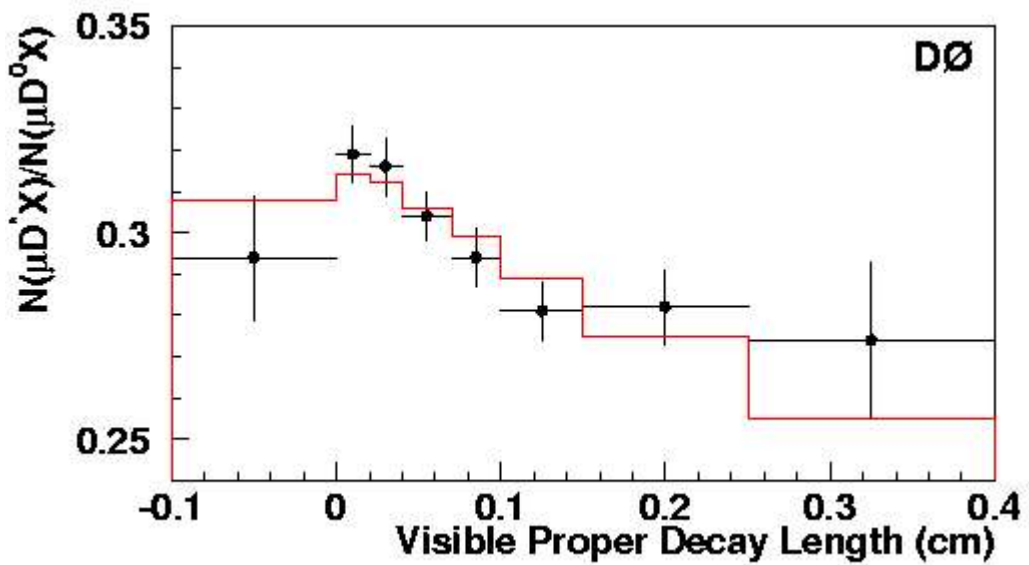
Free parameters:

k := $\tau^+/\tau^0 - 1$

ε : reconstruction efficiency of pion

r_i ratio from data

r_i^e expected ratio (from MC and data)



$\tau^+/\tau^0 = 1.080 \pm 0.016(\text{stat}) \pm 0.014(\text{syst})$
WA: 1.086 ± 0.017

Some main systematics:	
Branching ratio	0.0059
Resolution difference	0.0053
Fitting procedure	0.0086



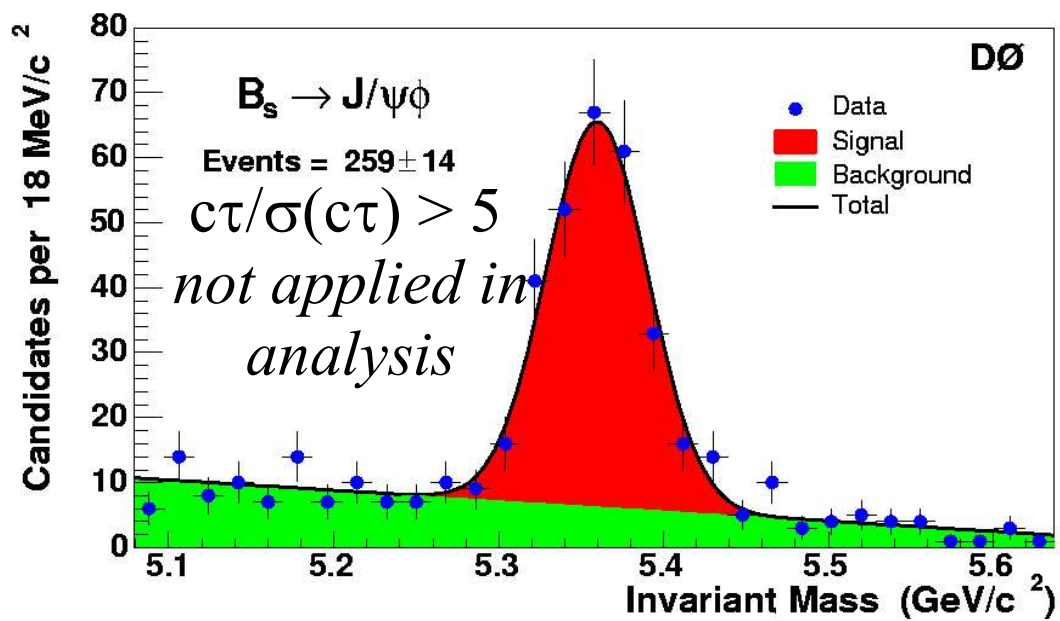
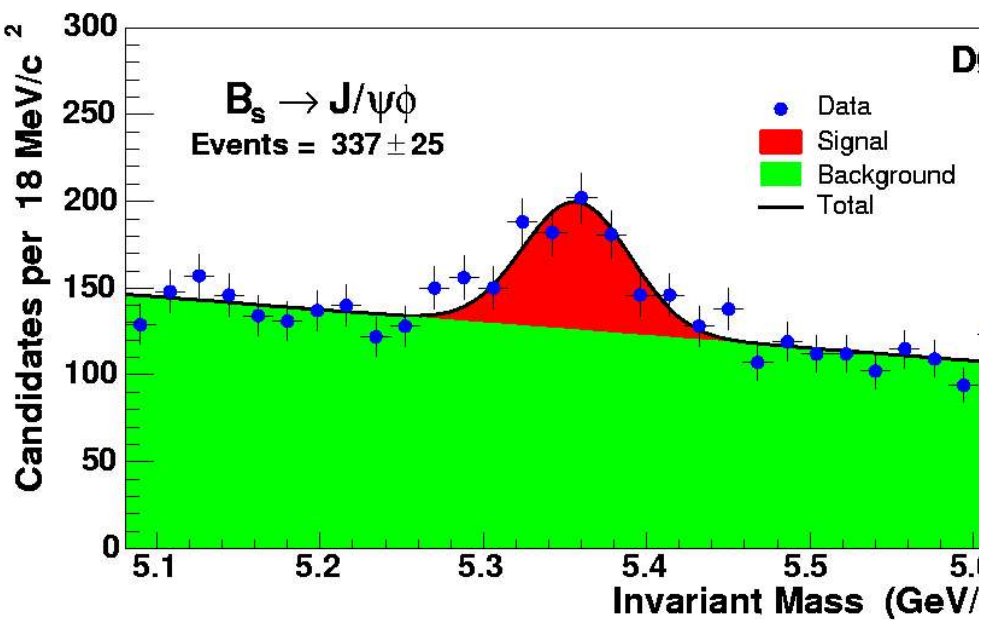
$B_s \rightarrow J/\psi \phi$ Signal

- Ratio of B_s/B^0 predicted to be smaller than B^+/B^0 : $\approx 1\%$
- $B_s \rightarrow J/\psi \phi$ CP even dominated (see $\Delta\Gamma$) and not flavour specific

Use $B_s \rightarrow J/\psi \phi$ ($J/\psi \rightarrow \mu\mu, \phi \rightarrow KK$) with 220 pb^{-1} of data

Besides kinematic cuts...

- Find J/ψ (to two muons)
- Two opposite signed tracks with inv. mass nearest to ϕ -mass
- Fit 4 track secondary vertex constrained by J/ψ mass
- No lifetime cut





$B_s \rightarrow J/\psi \phi$ Fitting Procedure

Unbinned maximum likelihood fit to mass and lifetime distribution

Signal:

Lifetime distribution

exponential-decay convoluted with gaussian

width = $\sigma(\text{PDL})$ (per Event)

global scale factor for $\sigma(\text{PDL})$

Mass distribution

gaussian

Background:

Lifetime distributions

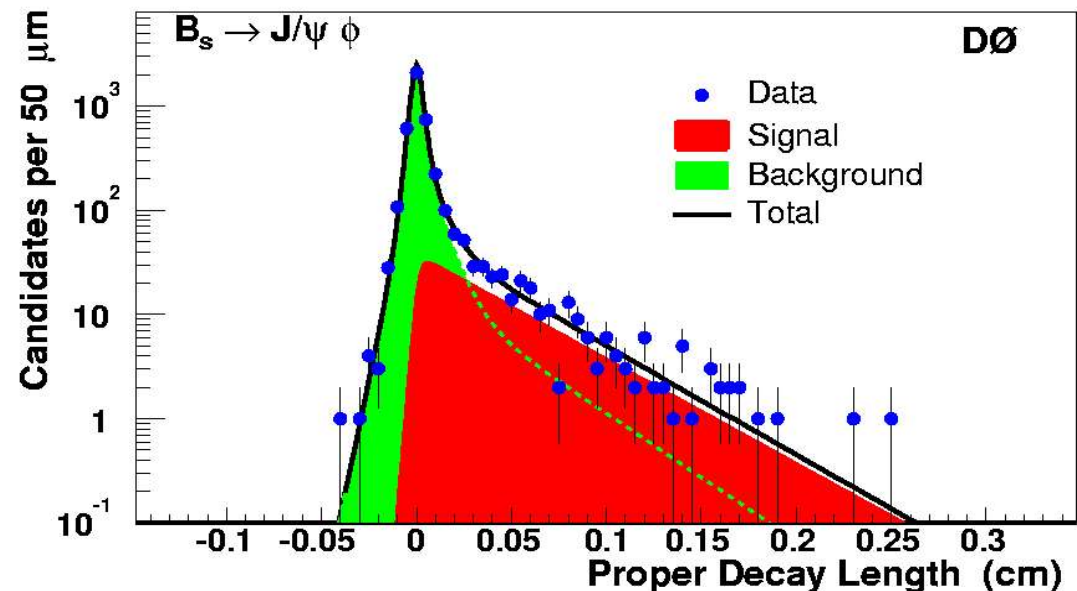
1 gaussian for prompt decay

3 exponential decays

2 short-, 1 longlived

Mass distribution

first order polynomial

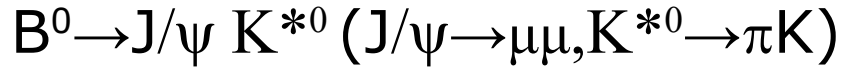


$$\tau(B_s) = 1.444^{+0.098}_{-0.071} \pm 0.020 \text{ ps}$$



$B^0 \rightarrow J/\psi K^{*0}$ Signal

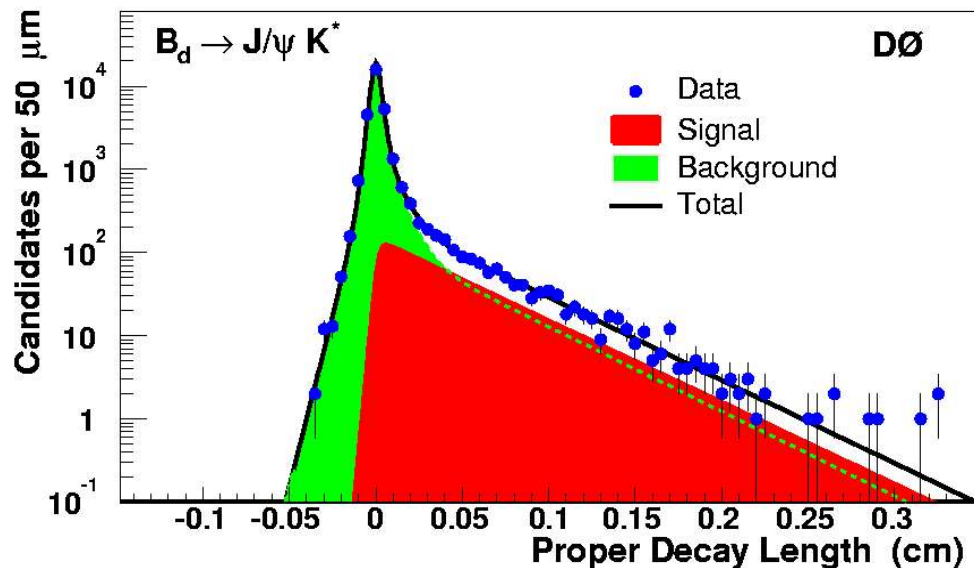
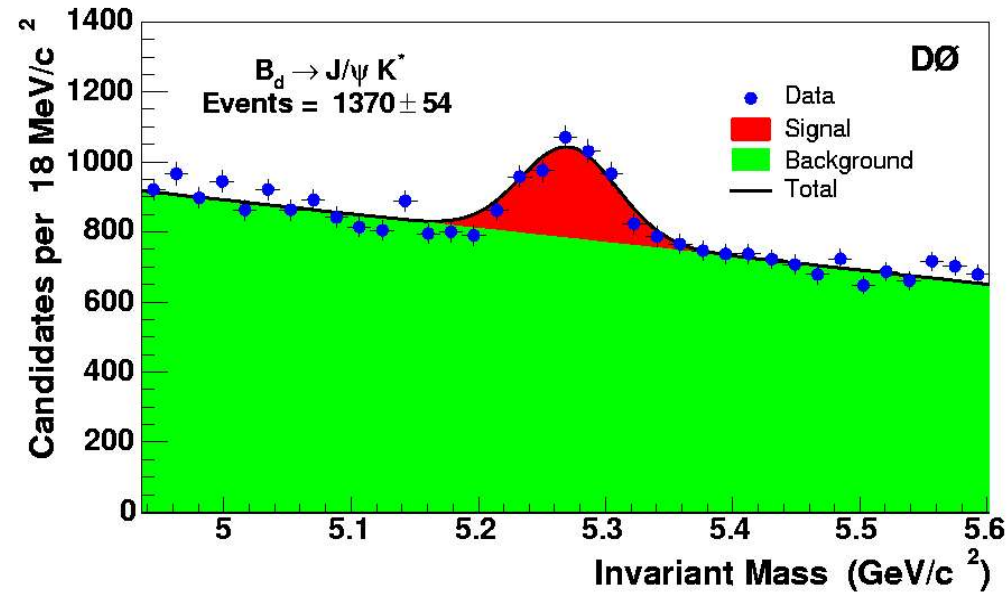
Similar topology:



- similar systematics
- Use identical fitting procedure

Differences:

- lower P_T cut for pion $0.8 \rightarrow 0.5$ GeV
- assume pion and K mass for tracks
- invariant mass closest to $K^{*0}(892)$



$$\tau(B^0) = 1.473^{+0.052}_{-0.050} \pm 0.023 \text{ ps}$$



B⁰/B_s Systematics and Ratio

Source	cτ(B _s) (μm)	cτ(B ⁰) (μm)	τ(B _s)/τ(B ⁰)
Alignment	2	2	0.000
J/ψ Vertex	3	4	0.002
Resolution Model	3	3	0.000
Background	4	5	0.002

$$\tau(B_s) = 1.444^{+0.098}_{-0.071} \pm 0.020 \text{ ps}$$

$$\tau(B^0) = 1.473^{+0.052}_{-0.050} \pm 0.023 \text{ ps}$$

$$\tau(B_s)/\tau(B^0) = 0.980^{+0.076}_{-0.071} \pm 0.003$$



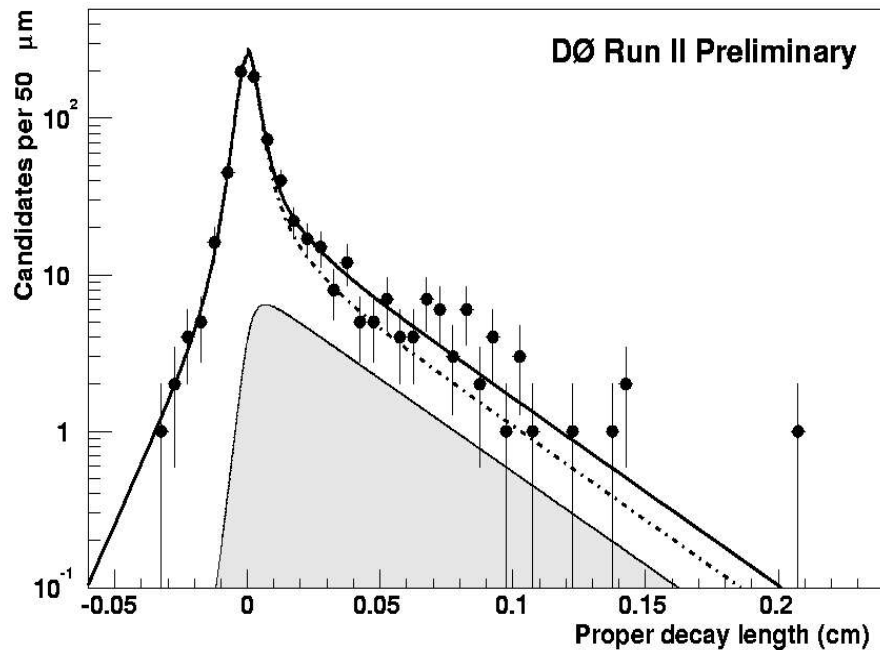
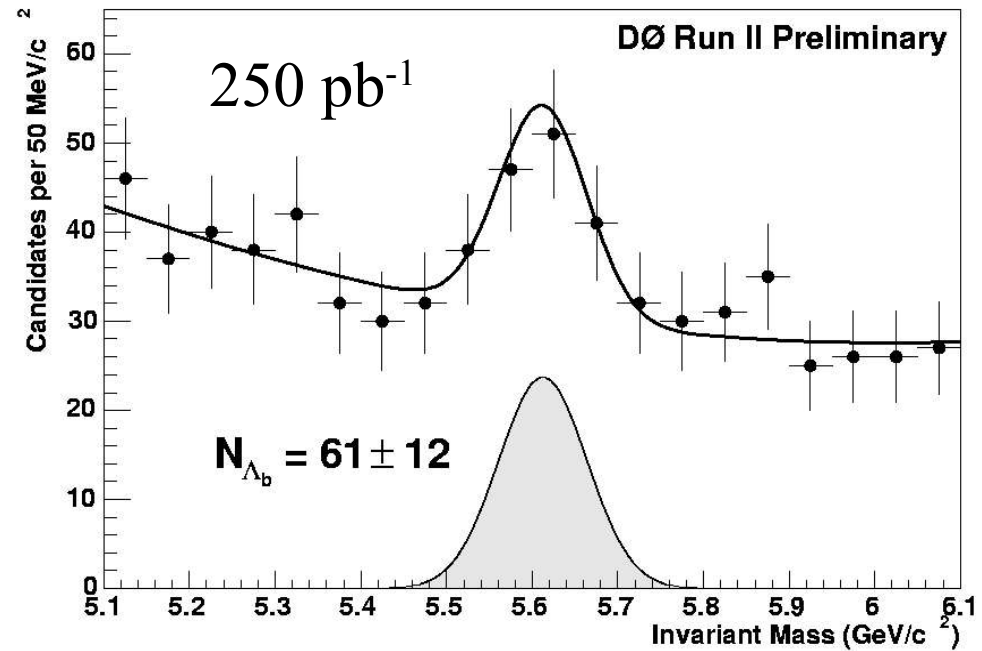
$\Lambda_B \rightarrow J/\psi \Lambda^0$ Lifetime

Again similar topology:

$$\Lambda_B \rightarrow J/\psi \Lambda^0 \quad (J/\psi \rightarrow \mu\mu, \Lambda^0 \rightarrow \pi p)$$

$$\tau(\Lambda_B) = 1.22^{+0.22}_{-0.18} \pm 0.04 \text{ ps}$$

$$\tau(\Lambda_B)/\tau(B^0) = 0.87^{+0.17}_{-0.10} \pm 0.03$$



Source	$c\tau(\Lambda_B)/\mu\text{m}$	ratio
Alignment	5.4	0.002
Resolution model	6.7	0.010
Background model	2.7	0.005
Signal Mass model	0.2	0.000
Background mass	2.5	0.007
Long lived comp.	1.5	0.003
Contamination	8.8	0.023



$B_S \rightarrow D_S^- \mu^+ \nu X$ Signal

- Best single measurement from DØ
- Independent input to $\Delta\Gamma/\Gamma$
- Helps understand decay for Δm_s

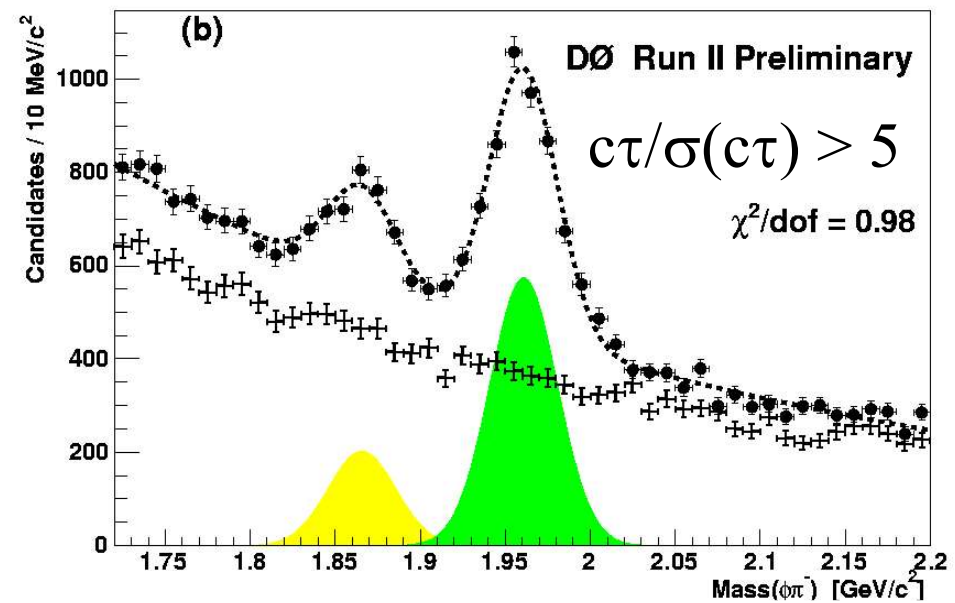
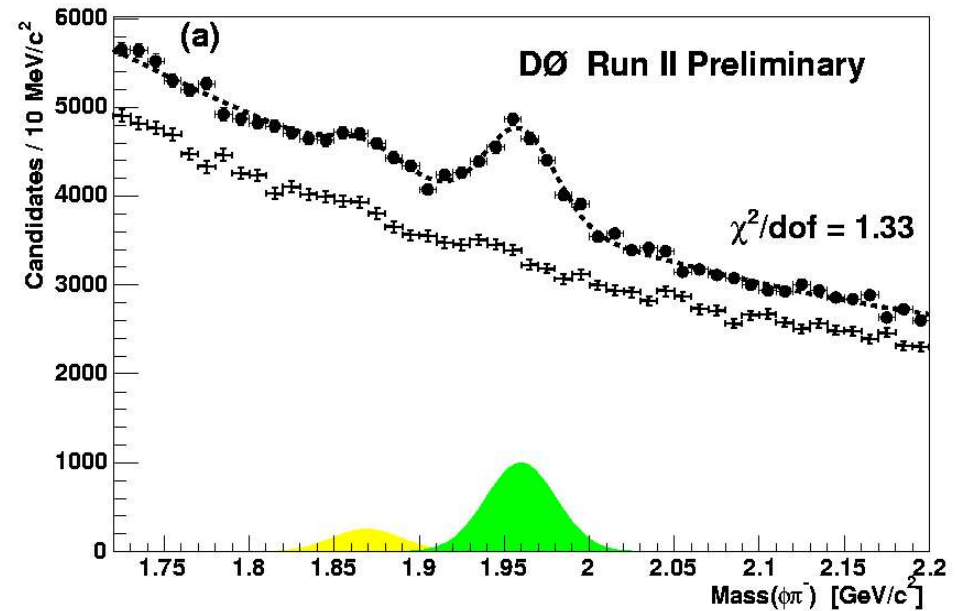
$$B_S \rightarrow D_S^- \mu^+ \nu X$$

$$D_S^- \rightarrow \phi \pi^- \quad \phi \rightarrow K^+ K^-$$

- Reconstructed D^- must have *positive* displacement...
- ...but *no* lifetime cut
- Use correlation in ϕ decay:
Transversity angle Φ between K^- and D^- in ϕ restframe,
 $\cos(\Phi) < 0.4$

B contamination of background

Decay mode	rel. eff.
$B \rightarrow D_S^{(*)-} D^{(*)+} X'$	5.3%
$B \rightarrow D_S^{(*)-} D^{(*)0} X'$	5.3%
$B \rightarrow D_S^{(*)+} D_S^{(*)-} X'$	4.4%

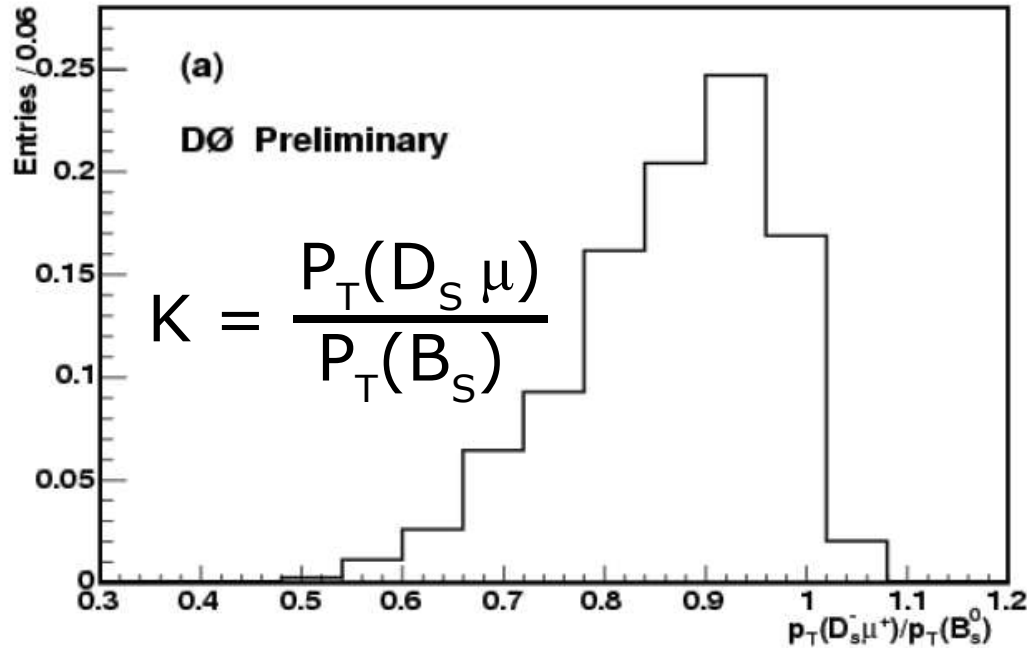




$B_S \rightarrow D_s^- \mu^+ \nu X$

MC Input

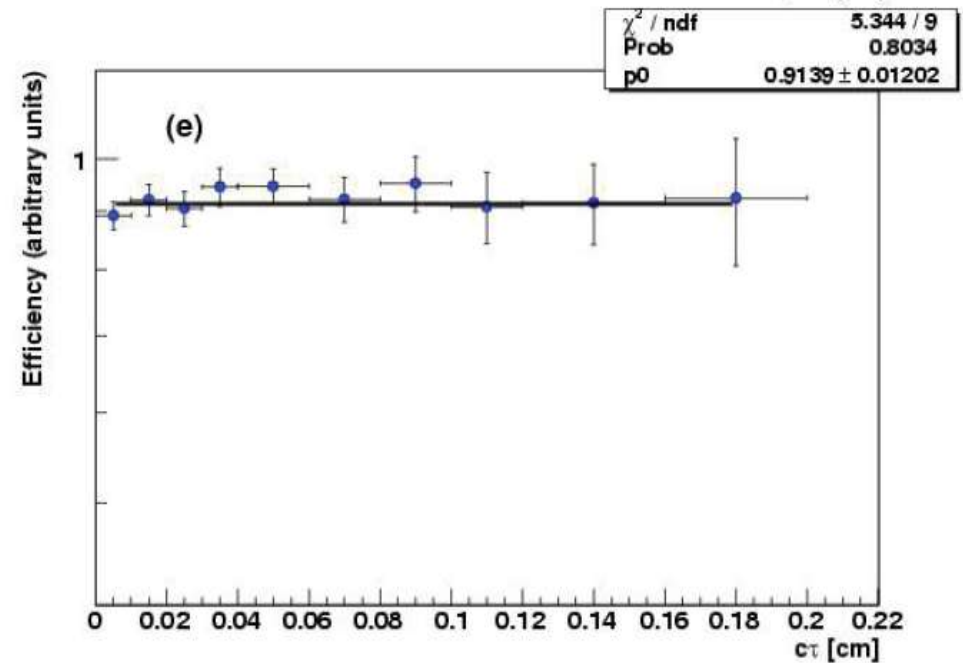
Combined K-factor



$\langle K\text{-factor} \rangle$ for diff. signal ch.

$B_S^0 \rightarrow D_s^- \mu^+ \nu X$	0.8848 ± 0.0024
$B_S^0 \rightarrow D_s^{*-} \mu^+ \nu X$	0.8608 ± 0.0014
$B_S^0 \rightarrow D_{s0}^{*-} \mu^+ \nu X$	0.8471 ± 0.0081
$B_S^0 \rightarrow D_{s1}^{*-} \mu^+ \nu X$	0.8166 ± 0.0055

Efficiency vs $c\tau$





Simultaneous fit to signal and background (i.e. D^- sidebands) lifetime distributions

$$L = \prod_i^{N_s} [f_{sig} F_{sig}^i + (1 - f_{sig}) F_{bg}^i] \prod_j^{N_B} F_{bg}^j$$

$$F_{sig}^i = \int dK H(K) \left[\frac{K}{c\tau} e^{-K\lambda_j/c\tau} \otimes G \right]$$

$$F_{bg}^j = (1 - f_+ - f_{++} - f_-) G$$

$$+ f_+ \frac{e^{-\lambda_j/\lambda^+}}{\lambda^+} \quad (\lambda_j \geq 0)$$

$$+ f_{++} \frac{e^{-\lambda_j/\lambda^{++}}}{\lambda^{++}} \quad (\lambda_j \geq 0)$$

$$+ f_- \frac{e^{-\lambda_j/\lambda^-}}{\lambda^-} \quad (\lambda_j < 0)$$

Signal parameters

- 1 lifetime
- 1 signal fraction

Background parameters

- 3 background fractions
- 3 lifetimes
- 1 width for prompt decay

General parameters

- 1 $c\tau$ resolution scale factor

Total 10 parameters

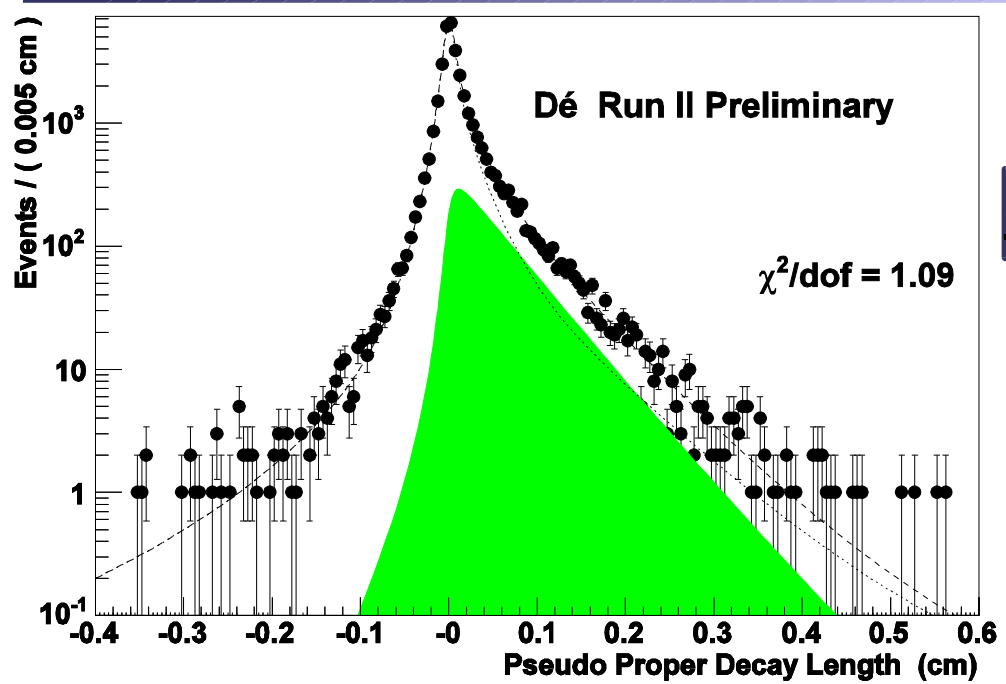


$B_s \rightarrow D_s^- \mu^+ \nu X$ Systematics

Non B_s^0 backgrounds	-4.4/+3.6 μm
K factor determination	$\pm 3.5 \mu\text{m}$
Decay length resolution	$\pm 1.6 \mu\text{m}$
Detector alignment	$\pm 5.0 \mu\text{m}$
Cut selection bias	+ 3.6 μm
K factor convolution	- 2.2 μm
Background evaluation	$\pm 15.0 \mu\text{m}$ Work in Progress
from left and right sideband longlived contributions	
Total (added in quadrature)	$\pm 17.0 \mu\text{m}$



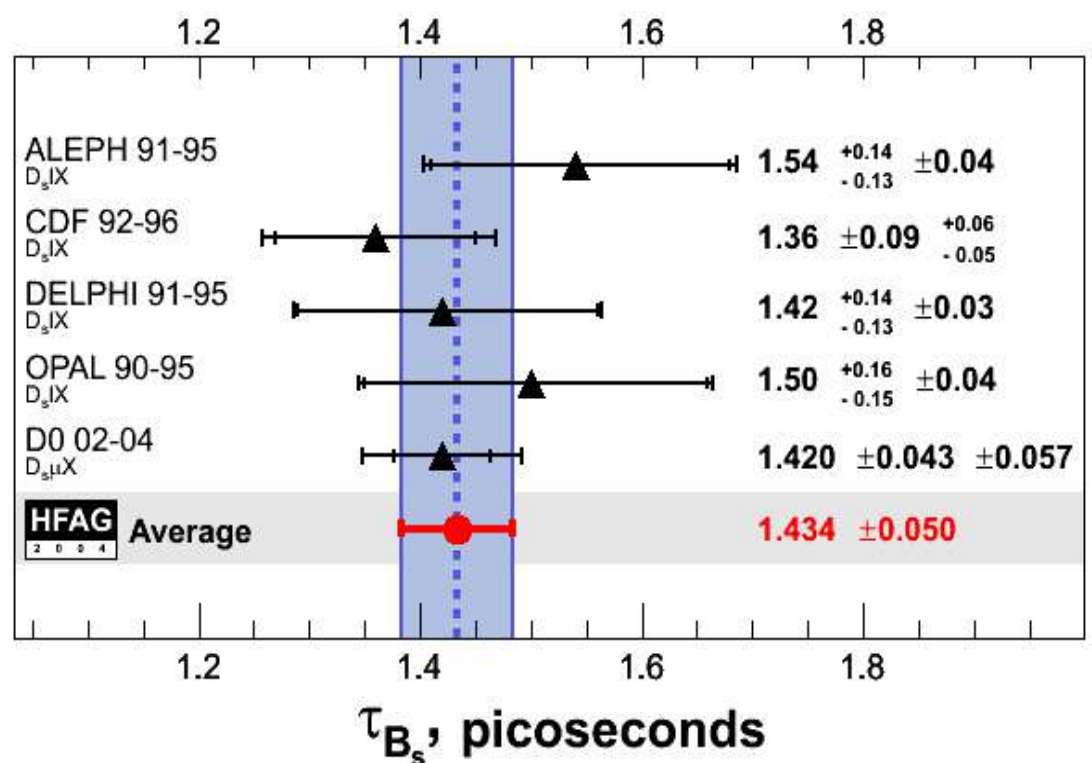
$B_S \rightarrow D_s^- \mu^+ \nu X$ Results



$\tau = 1.420 \pm 0.043(\text{stat}) \pm 0.057(\text{syst}) \text{ps}$

Preliminary

Previous World Average:
 $1.461 \pm 0.057 \text{ ps}$
 New:
 $1.434 \pm 0.050 \text{ ps}$





CP eigenstates:

$$|B_s^{\text{even}}\rangle = 1/\sqrt{2}(|B_s^0\rangle - |\bar{B}_s^0\rangle)$$

$$|B_s^{\text{odd}}\rangle = 1/\sqrt{2}(|B_s^0\rangle + |\bar{B}_s^0\rangle)$$

Mass eigenstates:

$$|B_L\rangle = (p|B_s^0\rangle + q|\bar{B}_s^0\rangle)$$

$$|B_H\rangle = (p|B_s^0\rangle - q|\bar{B}_s^0\rangle)$$

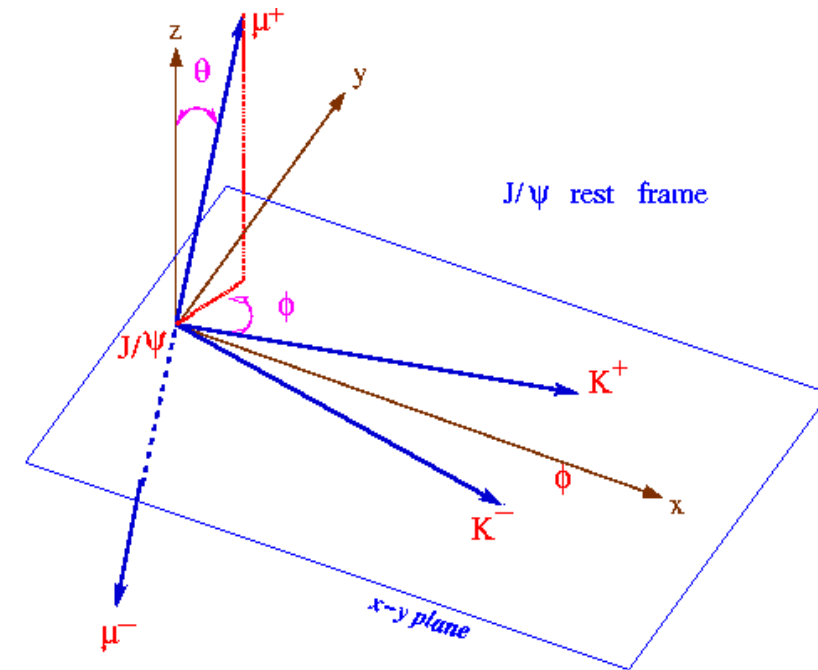
- $B_s \rightarrow J/\psi \phi$ not flavour specific
final state for both CP eigenstates
with different lifetimes $\Rightarrow \Delta\Gamma$
- Semileptonic decays are flavour specific ($|\bar{B}_s^0\rangle$ or $|B_s^0\rangle$)
- Negligible CP violation in SM
 \Rightarrow CP states = Mass states

$B_s \rightarrow J/\psi \phi$,

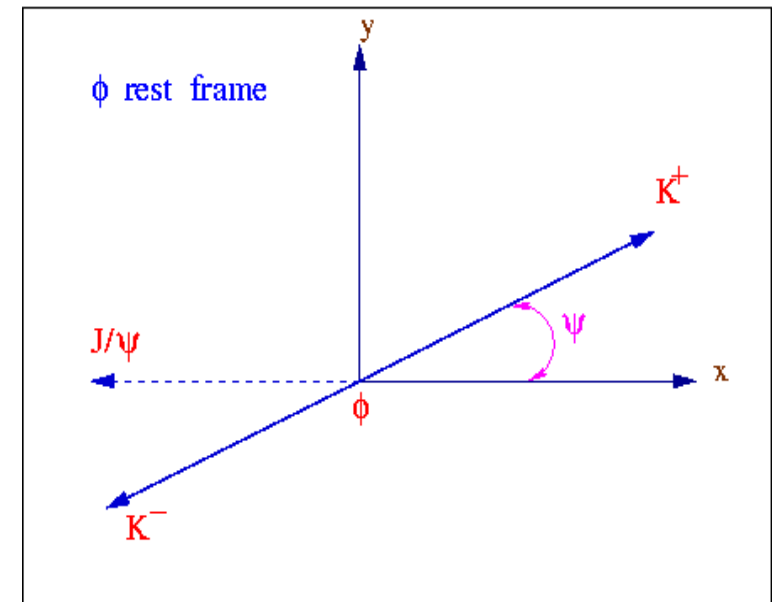
Pseudoscalar \rightarrow Vector Vector decay

Both CP-even and CP-odd present,
but well separated in transversity

Transversity angle: $\cos(\theta)$



- Measure **two distinct lifetimes** (equivalently: $\Delta\Gamma/\Gamma$ and τ) by fitting time evolution and transversity distr. In untagged $B_s \rightarrow J/\psi \phi$ decays.
- If **CP is conserved**, they can be interpreted as the lifetimes of the two B_s mass eigenstates.





$\Delta\Gamma/\Gamma$: Parameterisation

Three amplitudes: $A_0, A_{\parallel}, A_{\perp}$

CP even: linear combination of A_0, A_{\parallel}

CP odd: A_{\perp}

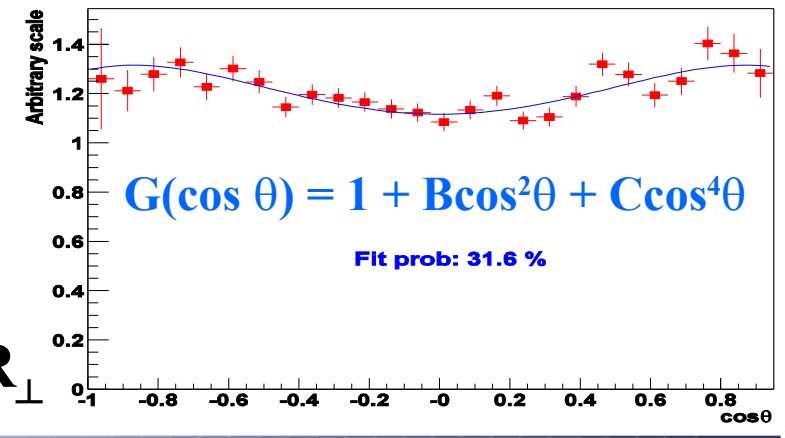
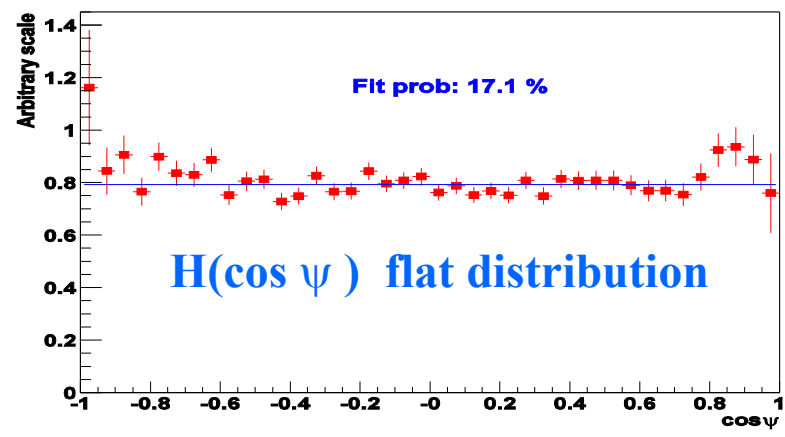
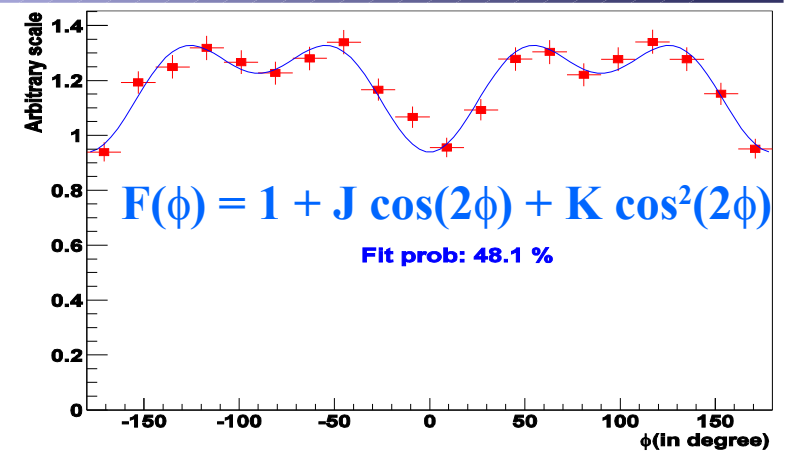
Define: $R_{\perp} := |A_{\perp}(0)|^2$

$$\frac{d^4\Gamma \rightarrow J/\psi(1^+1^-)\phi(K^+K^-)}{d\cos\theta d\phi d\psi dt} = L(\cos\theta, \phi, \psi, t, A_0, A_{\parallel}, A_{\perp}) \cdot F(\phi) \cdot G(\cos\theta) \cdot H(\cos\psi)$$

Insert $F(), H()$ and integrate over ψ and ϕ

\Rightarrow

$$\frac{d^2\Gamma \rightarrow J/\psi(1^+1^-)\phi(K^+K^-)}{d\cos\theta dt} = L(\cos\theta, t, \underbrace{|A_{\perp}|^2}_{R_{\perp}}, \underbrace{|A_{\parallel}|^2 - |A_0|^2}_{0.355 \pm 0.066 \text{ (from CDF)}}, \underbrace{|A_{\parallel}|^2 + |A_0|^2}_{= 1 - |A_{\perp}(0)|^2 = 1 - R_{\perp}}) \cdot G(\cos\theta)$$





Simultaneous fit to mass, proper decay length and transversity

Signal Parameters

1	f_{sig}	signal fraction
2	m_S, σ	signal mass, width
1	R_{\perp}	CP-odd fraction at $t=0$
1	$c\tau = c/\bar{\Gamma}$,	$\bar{\Gamma} = (\Gamma_L + \Gamma_H)/2$
1	$\Delta\Gamma/\bar{\Gamma}$	

Background Parameters

2	slope in mass (1 prompt, 1 long-lived)
6	ct shape
4	transversity (2 prompt + 2 long-lived)

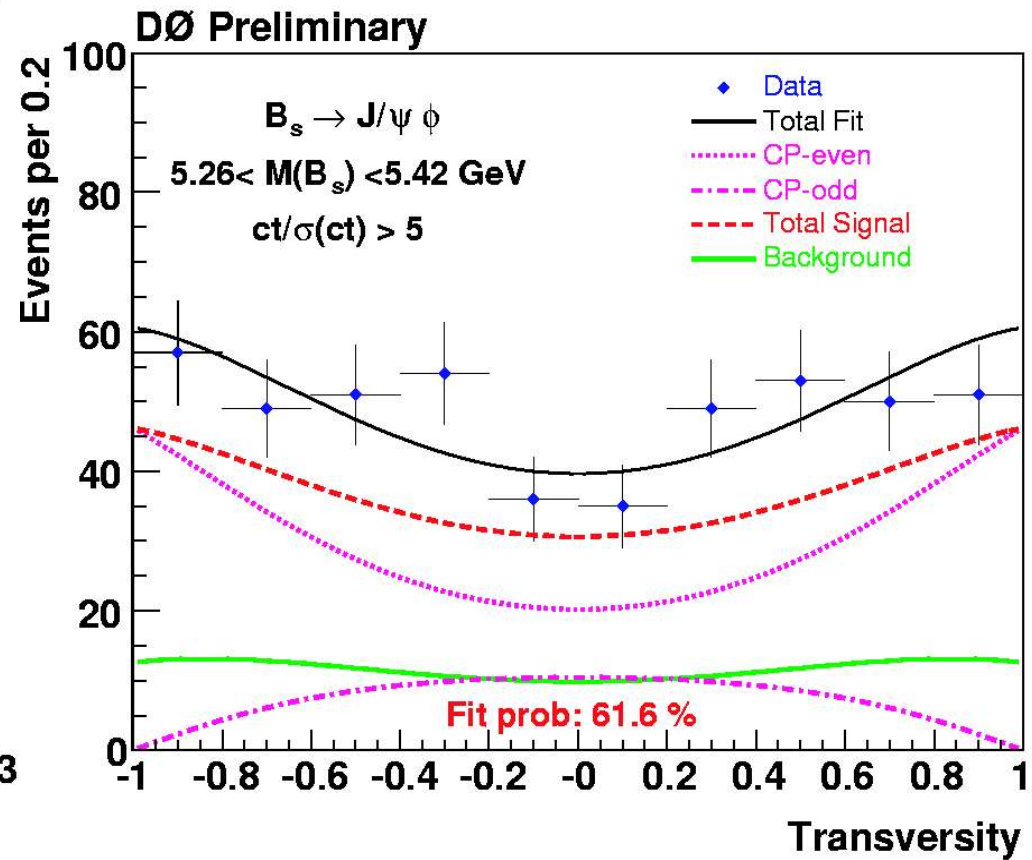
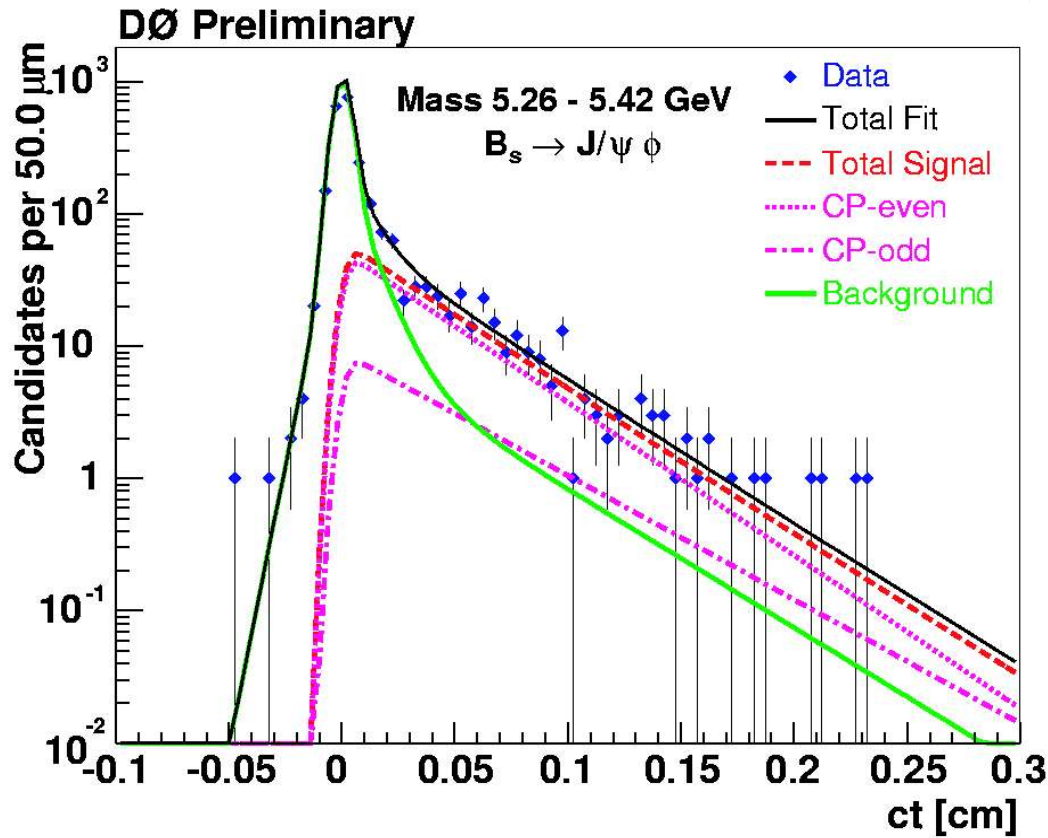
General Parameter

1	$\sigma(\text{ct})$ scale
---	---------------------------

Total: **19 parameters**



$\Delta\Gamma/\Gamma$: Results



$$\tau(B_s^0) = 1.39^{+0.13}_{-0.14} \pm 0.08 \text{ ps}$$

$$\frac{\Delta\Gamma}{\Gamma} = 0.21^{+0.27}_{-0.40} \pm 0.20$$

$$R_{\perp} = 0.17 \pm 0.10 \pm 0.02$$



$\Delta\Gamma/\Gamma$: Systematics

Source	$c\tau$ (in μm)	R_{\perp}	$\Delta\Gamma / \bar{\Gamma}$	
Signal ε vs $\cos\theta$	± 0.6	± 0.005	± 0.001	MC
Signal ε vs ϕ, ψ angles including: $(A_0 ^2 - A_{\parallel} ^2)$	± 0.2	± 0.02	± 0.001	MC + CDF
Signal mass model	± 0.4	± 0.006	± 0.016	data
Procedure bias	± 2	± 0.01	± 0.025	MC
Detector alignment	± 2	--	--	data
Bkg lifetime model	0.5	0.005	0.016	data



$\Delta\Gamma/\Gamma$: Comparisons

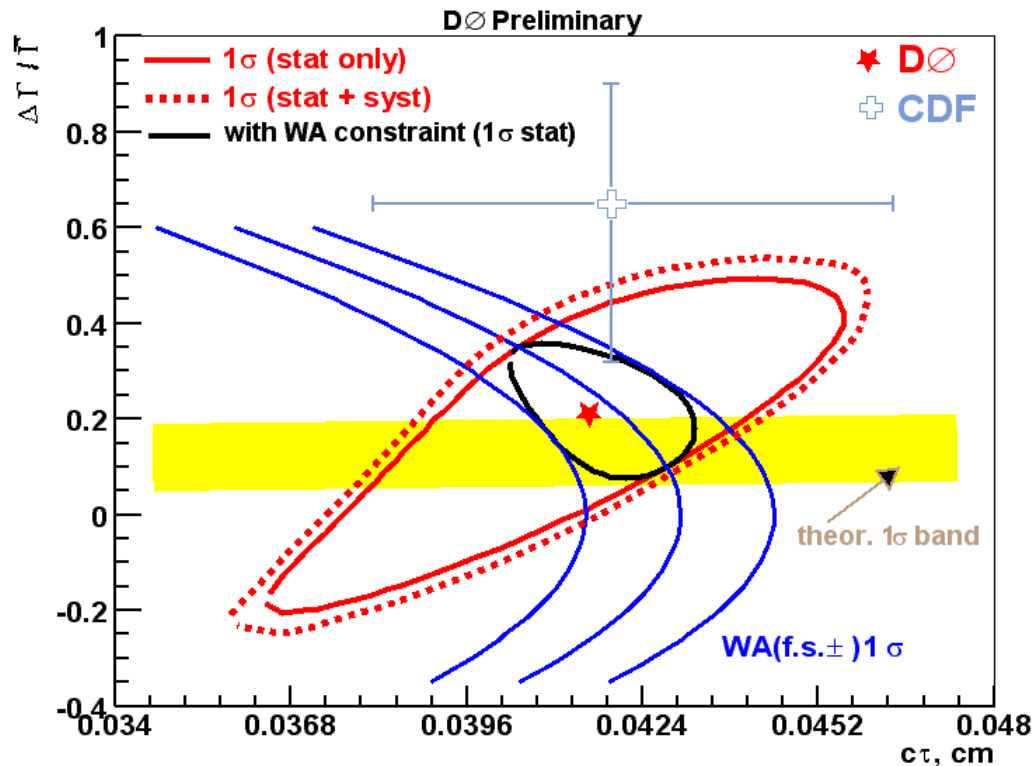
- Consistent with $\Delta\Gamma/\Gamma$ CDF result
- Agrees well with theoretical prediction 0.12 ± 0.05
- The WA flavor specific lifetime provides independent relation of $\Delta\Gamma$ and Γ

$$\Gamma_{fs} = \bar{\Gamma} \left(\frac{1 - (\Delta\Gamma/2\bar{\Gamma})^2}{1 + (\Delta\Gamma/2\bar{\Gamma})^2} \right)$$

$$\tau_{fs} = 1.43 \pm 0.05 \text{ ps}$$

$$\Rightarrow \frac{\Delta\Gamma}{\Gamma} = 0.23^{+0.16}_{-0.17}$$

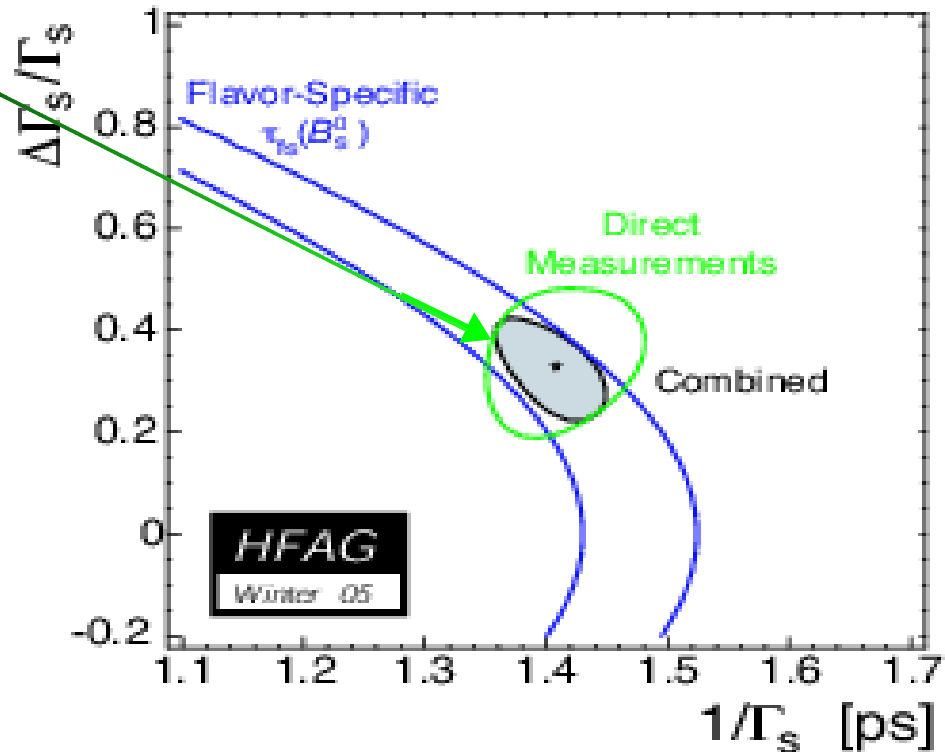
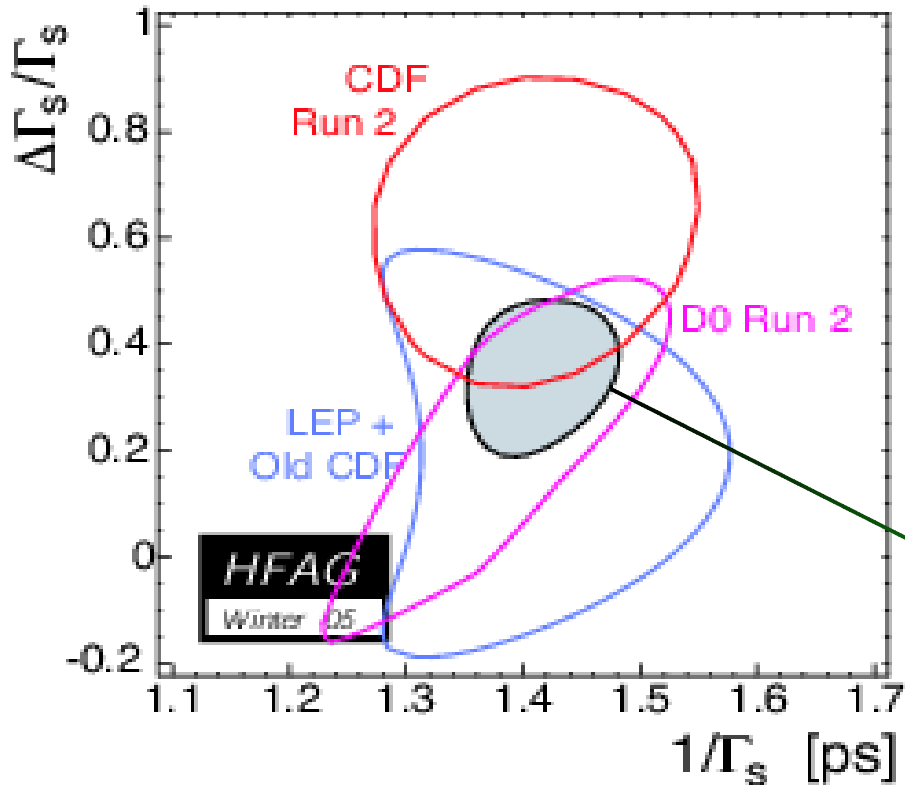
=>significant improvement to $\Delta\Gamma$





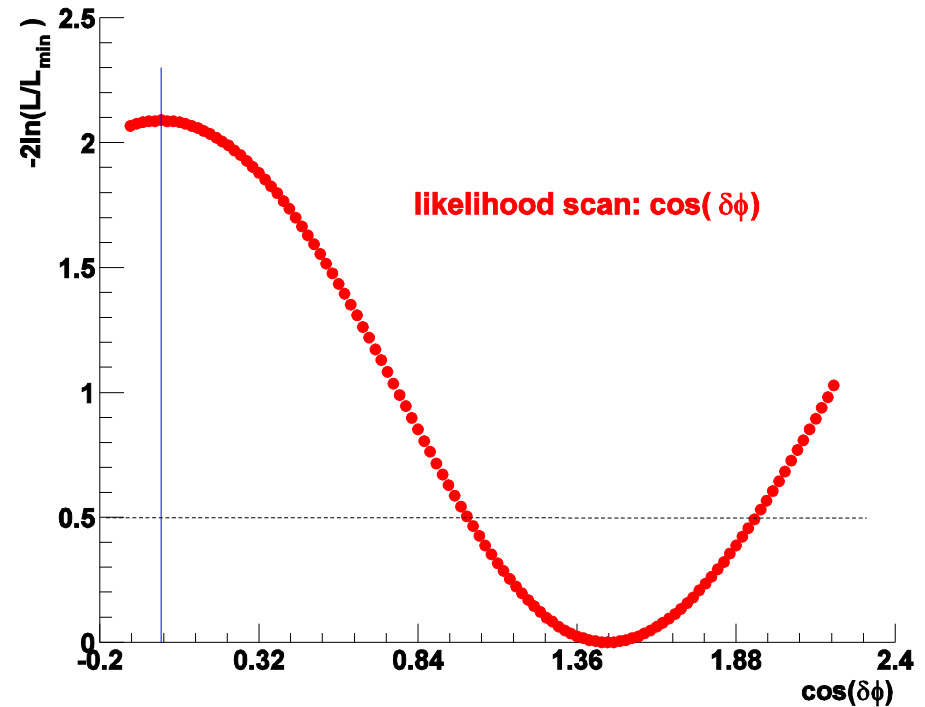
$\Delta\Gamma/\Gamma$: Averages

Averages of b-hadron
Properties as of Winter 2005
Heavy Flavor Averaging Group
(HFAG)
hep-ex/0505100





- Introducing CP violating phase as free parameter
- Interpret measured $\Delta\Gamma/\Gamma$ as $(\Delta\Gamma/\Gamma)_{SM} \cos^2(\delta\phi)$
(I. Dunietz, R. Fleischer, U.Nierste hep-ph/0012219)
 1. we measured $\Delta\Gamma/\Gamma = (\Delta\Gamma/\Gamma)_{SM} \cos^2(\delta\phi)$ and τ
 2. flavour specific lifetime constrains $\Delta\Gamma/\Gamma$ further.
 3. SM predicts (A. Lenz, hep-ph/0412007) $(\Delta\Gamma/\Gamma)_{SM} = 0.12 \pm 0.05$



$$|\cos(\delta\phi)| = 1.46^{+0.73}_{-0.69}$$



Summary

DØ produces a wealth of B physics results!
All results are competitive and test theory in a meaningful way

	measured	predicted	publ./prel.
B^+/B^0 ratio	$1.080_{\pm 0.016} \pm 0.014$	1.06 ± 0.02	published
Λ_B lifetime	$1.22_{-0.18}^{+0.22} \pm 0.04$ ps		published
Λ_B/B^0 ratio	$0.87_{-0.10}^{+0.17} \pm 0.03$	0.9-1.0	published
B_S/B^0 ratio	$0.980_{-0.071}^{+0.076} \pm 0.003$	$\approx 1\%$	published
$B_S \rightarrow D_S^- \mu^+ \nu X$	$1.420_{\pm 0.043} \pm 0.057$ ps		preliminary
$\Delta\Gamma/\Gamma$	$0.21_{-0.40}^{+0.24} \pm 0.20$	0.12 ± 0.05	preliminary