

Rare K Decays

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Thanks to many: D. Jaffe, T. Komatsubara, D. Bryman

Historical Perspective

Kaon decays have a parallel history along with the development of the standard model.

Phase	Observation	BR sens	Physics
Early	Long life	1	Strangeness
	Decays of K^+ , K_L , K_S	0.1	Parity violation
1960s	Semileptonic	$> 10^{-3}$	Meson Dynamics
	Hadronic	$> 10^{-3}$	CP violation
1970-80s	FCNC	$> 10^{-7}$	GIM, Standard Model
1985-present	ϵ'/ϵ		Direct CP
	radiative decays	$\sim 10^{-8}$	Low Energy QCD
	Forbidden Searches	$\sim 10^{-11}$	Limits on Non-SM
Future	Precision	$\sim 10^{-13}$	SM or New

Progress has been in phases partly driven by accelerator and detector technology. New phase is about to begin.

Focus of this talk:

- $K_L/K_S \rightarrow \pi^0 l^+ l^-$ [$l = e, \mu$]
- $K^+ \rightarrow \pi^+ \nu \bar{\nu}$, $K_L \rightarrow \pi^0 \nu \bar{\nu}$

Measuring $K_L^0 \rightarrow \pi^0 \ell^+ \ell^-$

$$\mathcal{B}(K_L^0 \rightarrow \pi^0 \ell^+ \ell^-) = (C_{mix} \pm C_{int} \frac{Im\lambda_t}{10^{-4}} + C_{dir} (\frac{Im\lambda_t}{10^{-4}})^2 + C_{CPC}) \times 10^{-12}$$

$\ell\ell$	C_{mix}	C_{int}	C_{dir}	C_{CPC}	$\mathcal{B}(K_L^0 \rightarrow \pi^0 \ell^+ \ell^-)$	$\mathcal{B}(K_L^0 \rightarrow \gamma\gamma\ell\ell)$
e^+e^-	$15.7 a_S ^2$	$6.2 a_S $	2.4	0	$(3.7_{-0.9}^{+1.1}) \times 10^{-11}$ (+) $(1.7_{-0.6}^{+0.7}) \times 10^{-11}$ (-)	6×10^{-7} 10^{-10} with cuts
$\mu^+\mu^-$	$3.7 a_S ^2$	$1.6 a_S $	1.0	5.2	$(1.5 \pm 0.3) \times 10^{-11}$ (+) $(1.0 \pm 0.2) \times 10^{-11}$ (-)	1×10^{-8} ?

$\mathcal{B}(K_L^0 \rightarrow \pi^0 e^+ e^-)$ measurement: Effective \mathcal{B} of main background to ee mode can be reduced with cuts, optimistically assuming signal/background of 1/2.5, implies a $\sim 10\%$ measurement of \mathcal{B} would require 350 $\pi^0 ee$ events or 7×10^{15} K_L with a 1% acceptance (including the decay probability). This would take a year at J-PARC (2×10^{14} p/spill) with 10^9 K_L /3.4s.

Additional possibilities to extract more information from these decays using Dalitz plot information, μ polarization and/or K_L - K_S interference.

Ref: Isidori, Smith, Unterdorfer EPJ **C36** (2004) 15, $|a_S| = 1.2 \pm 0.2$,

uncertainties in C coefficients omitted from table. $B(K_S \rightarrow \pi^0 e^+ e^-) \simeq 5.2 \times 10^{-9} a_S^2$,
 $B(K_S \rightarrow \pi^0 \mu^+ \mu^-) \simeq 1.2 \times 10^{-9} a_S^2$.

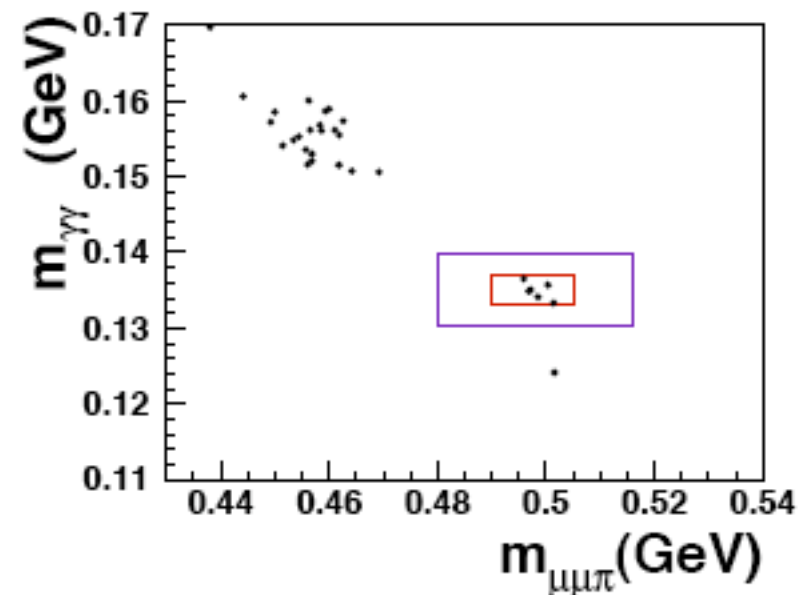
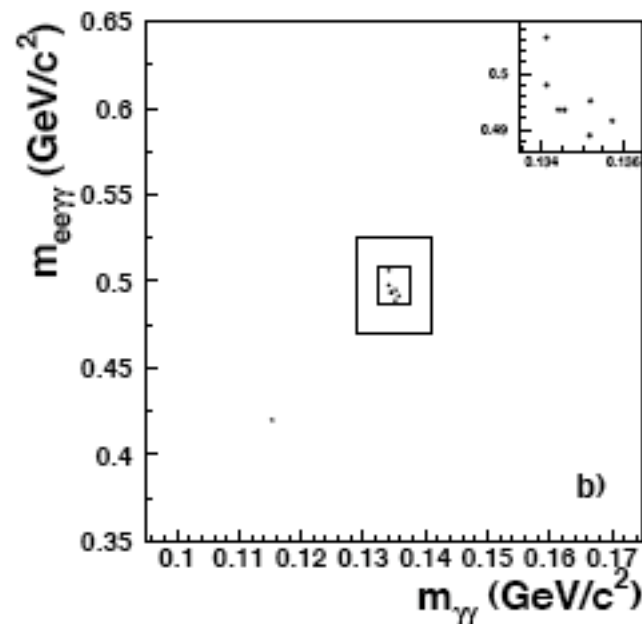
First Observations of $K_S^0 \rightarrow \pi^0 \ell^+ \ell^-$ by NA48/1

$K_S^0 \rightarrow \pi^0 e^+ e^-$

PL B576 (2003) 43

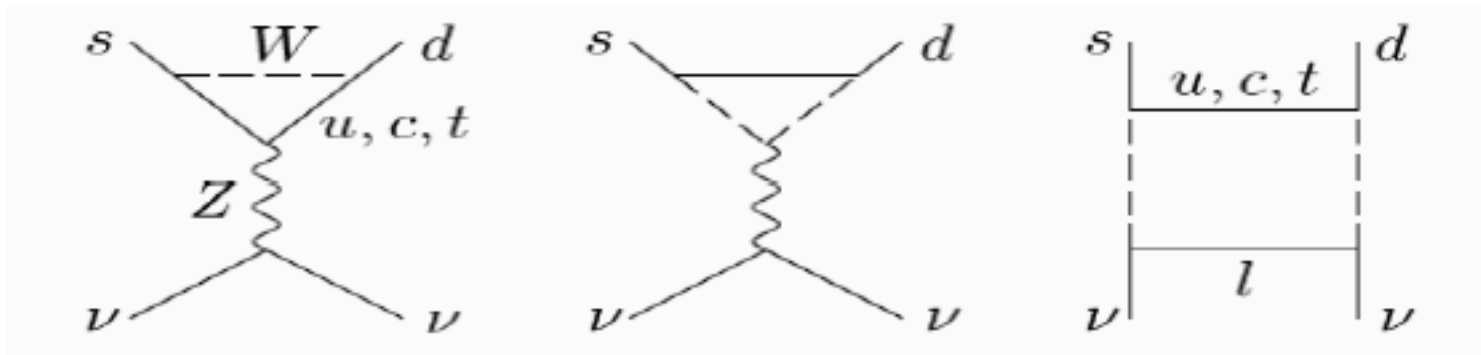
$K_S^0 \rightarrow \pi^0 \mu^+ \mu^-$

PL B599 (2004) 197



Data	Bgd	observed	BR (vector matrix element, no form factor)
$K_S^0 \rightarrow \pi^0 e^+ e^-$	$0.15^{+0.10}_{-0.04}$	7	$5.8^{+2.8}_{-2.3}(stat) \pm 0.8(syst) \times 10^{-9}$
$K_S^0 \rightarrow \pi^0 \mu^+ \mu^-$	$0.22^{+0.18}_{-0.11}$	6	$2.9^{+1.5}_{-1.2}(stat) \pm 0.2(syst) \times 10^{-9}$

$K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$ in the SM



Standard Model (*Buras*):

$$\text{Im } \lambda_t = \text{Im } V_{ts}^* V_{td} = \eta A^2 \lambda^5$$

$$\text{B}(K_L^0 \rightarrow \pi^0 \nu \bar{\nu}) = 1.8 \times 10^{-10} \left(\frac{\text{Im } \lambda_t}{\lambda^5} X(x_t) \right)^2$$

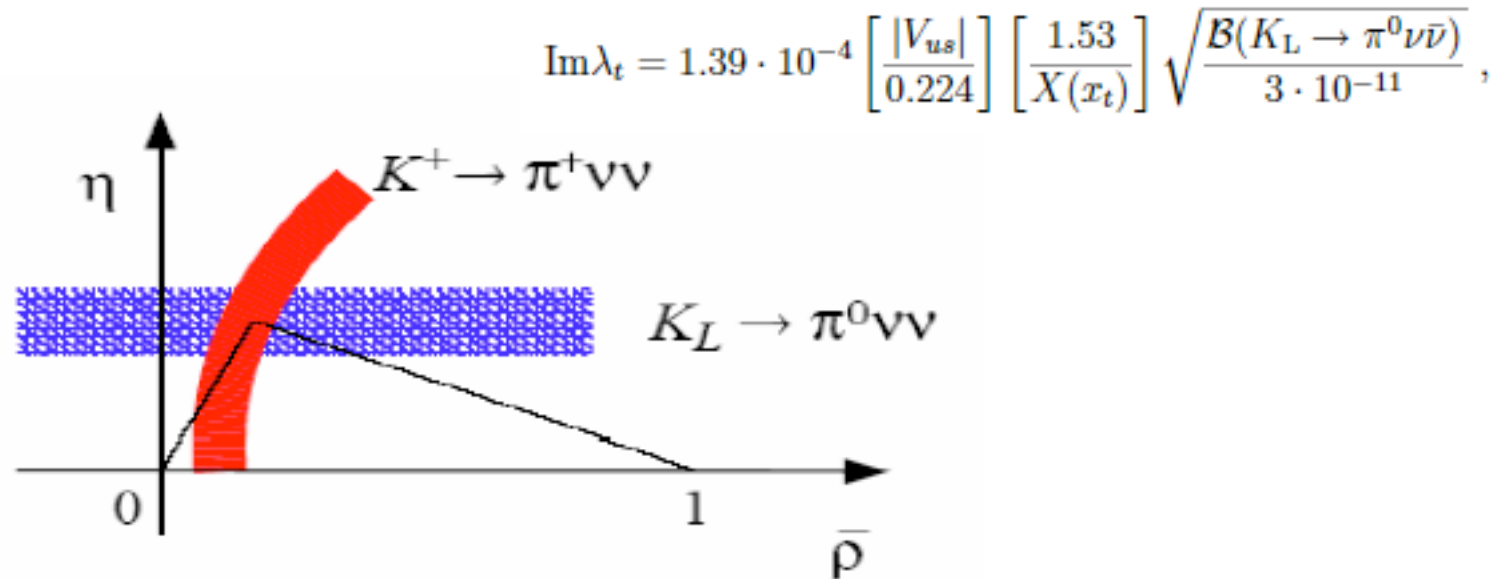
$$\sim 4.1 \times 10^{-10} A^4 \eta^2 = 3.0 \pm 0.6 \times 10^{-11}$$

$$\text{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \sim 1.0 \times 10^{-10} A^4 \left[\eta^2 + (\rho_0 - \rho)^2 \right] = 7.8 \pm 1.2 \times 10^{-11}$$

Errors from CKM parameter uncertainties
 Intrinsic errors $\sim 7\%$ for K^+ , $\sim 2\%$ for K_L

$$\text{Golden Relation: } \sin(2\beta)_{\psi K_S} = \sin(2\beta)_{K \rightarrow \pi \nu \bar{\nu}}$$

Powerful tool to falsify SM or distinguish new physics scenarios



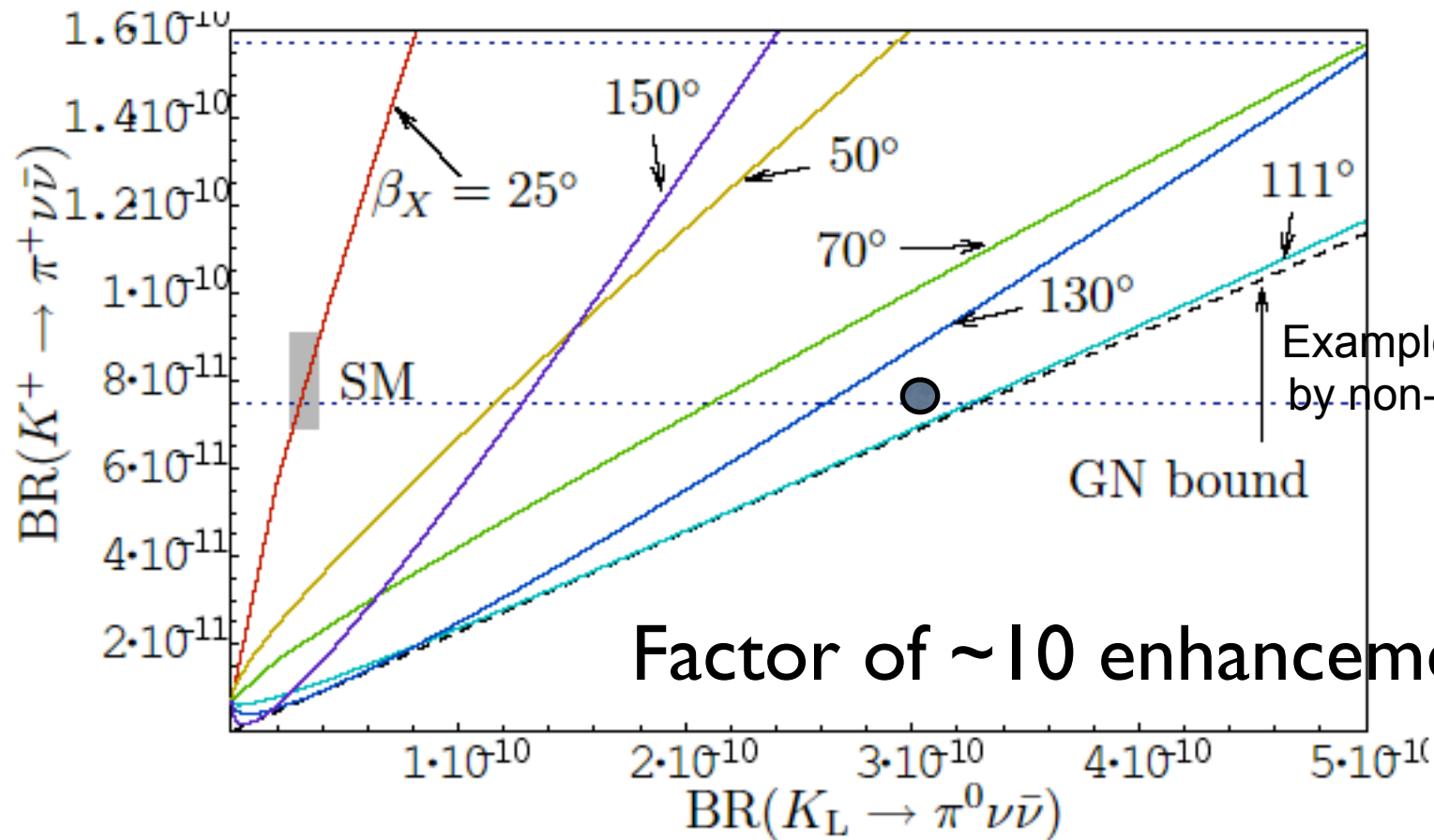
Buras, Isidori, D'Ambrosio, et al.

- $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$ (and $K^+ \rightarrow \pi^+ \nu \bar{\nu}$) – highly suppressed in SM and most of its extensions → opportunity for new physics.
- Most precisely calculated FCNC processes involving quarks in SM and in its extensions.
- Unique, clean access to the CP-violating and flavor breaking structure of new physics -- access to short distance effects.
- Even if SM holds at high precision, access to very high mass scales - complementary to highest energy colliders.

New CP-violating Phase θ_X : $\beta_X = \beta - \theta_X$

$$\frac{B(K_L \rightarrow \pi^0 \nu \bar{\nu})}{B(K_L \rightarrow \pi^0 \nu \bar{\nu})_{SM}} = \left| \frac{X}{X_{SM}} \right|^2 \left[\frac{\sin(\beta - \theta_X)}{\sin(\beta)} \right]^2, \quad X = |X|e^{i\theta_X}$$

$B(K^+ \rightarrow \pi^+ \nu \bar{\nu})$ vs. $B(K_L^0 \rightarrow \pi^0 \nu \bar{\nu})$



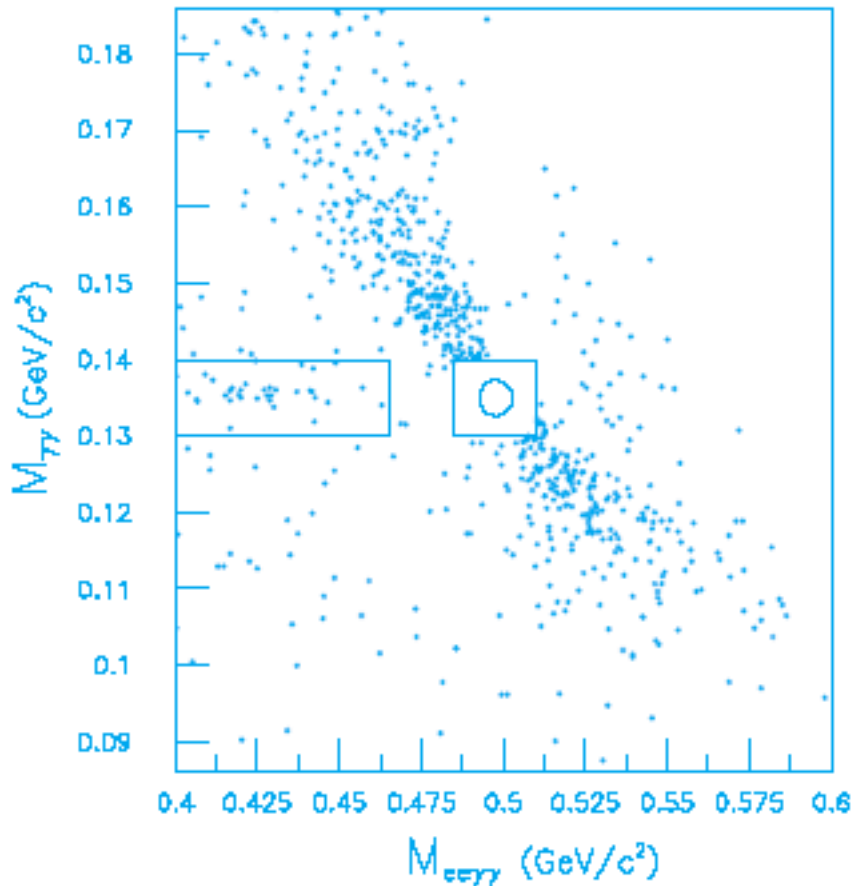
New physics example: Minimum Flavor Violation

Status of experiments

KEK	PS (12GeV)	E246 [✓]	K ⁺ at rest
		E391a	K _L
J-PARC	PS (50GeV)	Lol's*	K _L K ⁺ at rest
BNL	AGS (25GeV)	E787 [✓] / E949	K ⁺ at rest
		E865 [✓]	K ⁺ in flight
		KOPIO*	K _L
CERN	SPS (400GeV)	NA48/1 [✓]	K _S
		NA48/3*	K ⁺ in flight
FNAL	Tevatron (800GeV)	KTEV [✓]	K _L
	Main Injector(120GeV)	CKM-P940*	K ⁺ in flight

✓ data taking completed

* future program: construction not started

$$K_L^0 \rightarrow \pi^0 e^+ e^- \text{ by KTEV}$$


Make fit to extract signal/bck
and make optimized phase space
cuts

$$f(m_{ee\gamma\gamma}, m_{\gamma\gamma}) = A_0 + A_{\gamma\gamma} m_{\gamma\gamma} + A_{ee\gamma\gamma} m_{ee\gamma\gamma} + A_g g(m_{ee\gamma\gamma}, m_{\gamma\gamma})$$

A radiative Dalitz decay:

$$K_L^0 \rightarrow e^+ e^- \gamma \gamma, 5.8 \times 10^{-7}$$

(when $M_{\gamma\gamma} = m_{\pi^0}$)

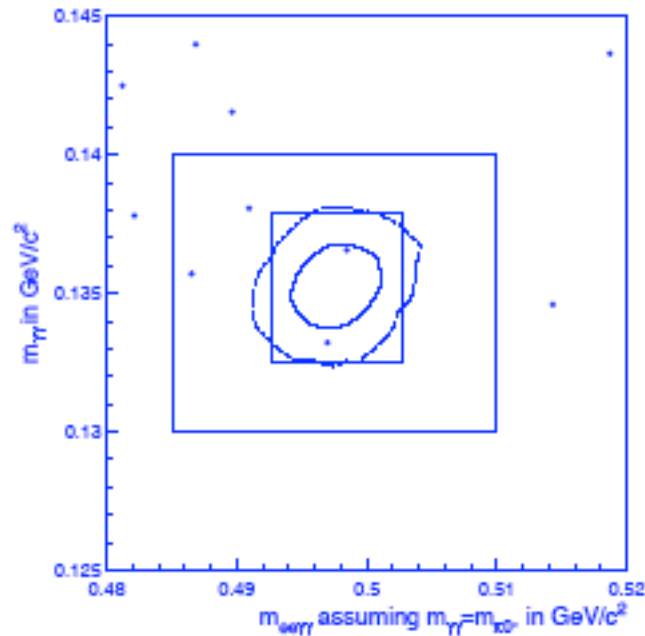
is the limiting background
(pointed out by Greenlee,
1990).

⇒ phase space fiducial cuts

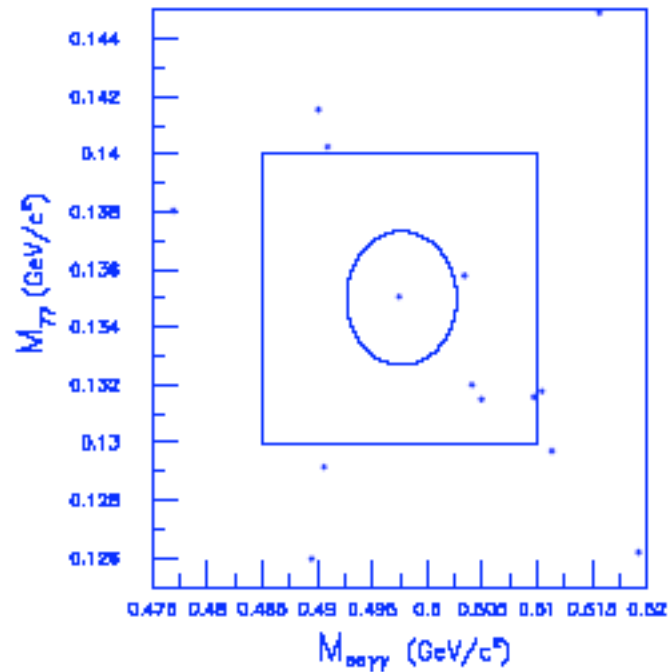
< ~ 1/4 signal loss >

There are several distinctive regions in the $m_{\gamma\gamma}$ vs. $m_{ee\gamma\gamma}$ plane. In order to minimize human bias in the determination of the selection criteria, a blind analysis was performed. The box was the region covered up until cuts were finalized, and spans $130 < m_{\gamma\gamma} < 140 \text{ MeV}/c^2$ and $485 < m_{ee\gamma\gamma} < 510 \text{ MeV}/c^2$. The ellipse in the box is the signal region, which spans $\sim 2\sigma$ in the $K_L \rightarrow \pi^0 e^+ e^-$ signal Monte Carlo $m_{ee\gamma\gamma}$ and $m_{\gamma\gamma}$ distributions. In the $m_{ee\gamma\gamma}$ direction, the ellipse is $\pm 5.02 \text{ MeV}/c^2$ wide, and in the $m_{\gamma\gamma}$ direction it is $\pm 2.32 \text{ MeV}/c^2$ wide. The rectangular “strip” to the left of the box is dominated by backgrounds from $K_L \rightarrow \pi_D^0 \pi_D^0$ and $K_L \rightarrow \pi^0 \pi_D^0 \pi_D^0$ decays with accidental π^0 s. Missing particles in these decays cause the reconstructed mass $m_{ee\gamma\gamma}$ to be low.

KTEV 1997 dataset
PRL 86 (2001) 397



KTEV 1999 dataset
PRL 93 (2004) 021805



Data	Bgd	observed	BR
1997	1.06 ± 0.41	2	$< 5.1 \times 10^{-10}$
1999	0.99 ± 0.35	1	$< 3.5 \times 10^{-10}$
Combined			$< 2.8 \times 10^{-10}$
SM prediction			$(2 \pm 1) \times 10^{-11}$

$$K_L^0 \rightarrow \pi^0 \mu^+ \mu^- \text{ by KTEV}$$

KTEV 1997 dataset
PRL 84 (2000) 5279

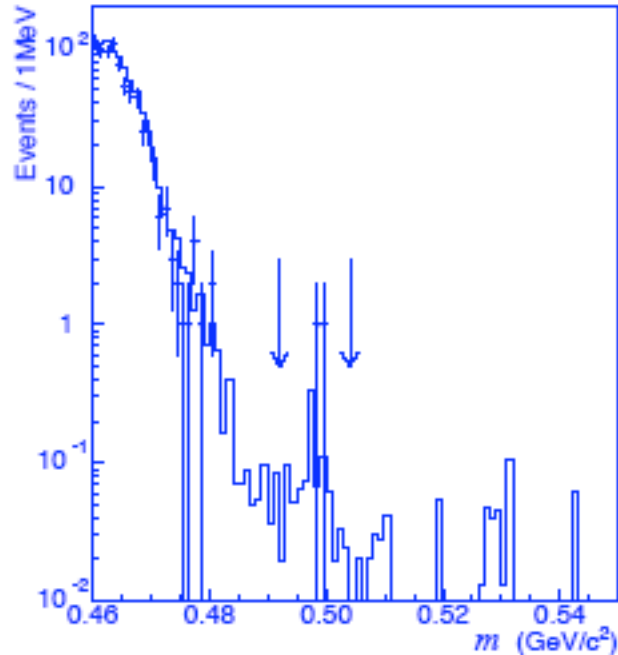


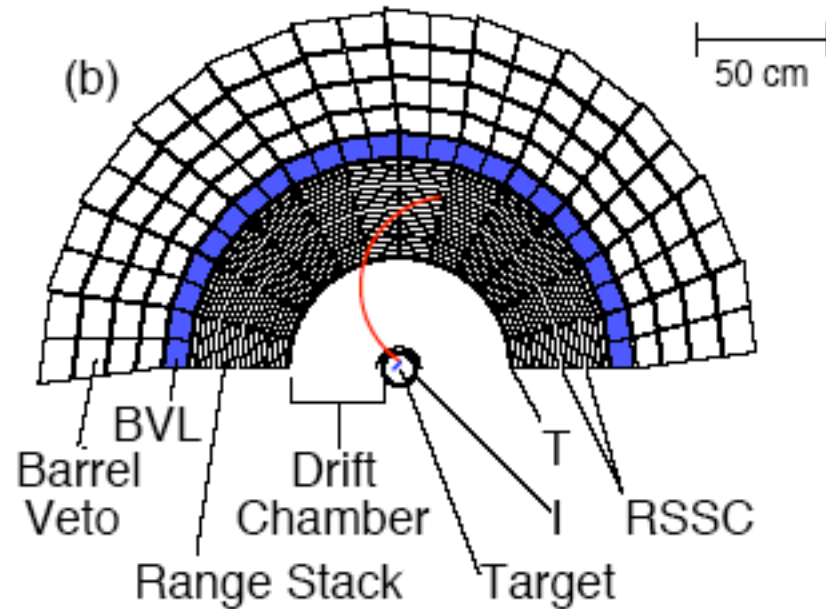
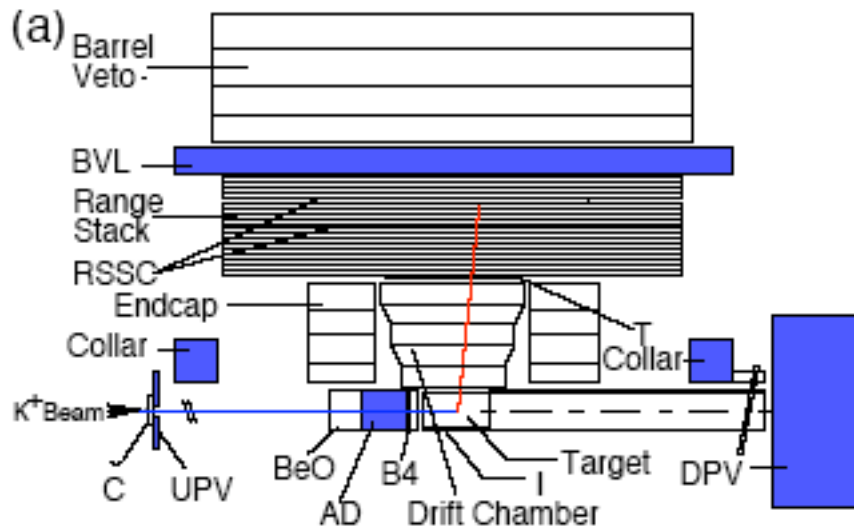
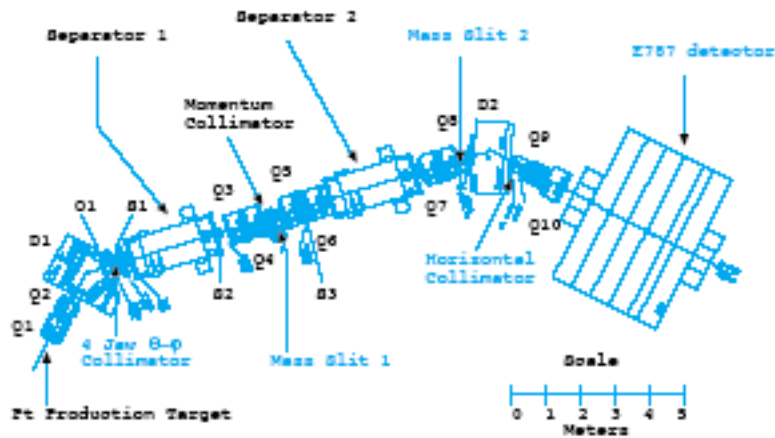
TABLE I. Summary of expected backgrounds in the signal region. “Acc.” refers to particles from other sources which were accidentally time-coincident with the interesting decay; “D” and “P” refer respectively to decay in flight or punch-through. Limits are 90% C.L.; uncertainties are due to uncertainties in published branching ratios, simulation statistics, and the statistics of the normalization mode.

Decay mode	Expected number of events
$K_L \rightarrow \mu^+ \mu^- \gamma \gamma$	0.373 ± 0.032
$K_L \rightarrow \mu^+ \mu^- \gamma + \gamma(\text{Acc})$	< 0.029
$K_L \rightarrow \pi^+ \pi^- \pi^0$ (DD)	0.252 ± 0.095
$K_L \rightarrow \pi^+ \pi^- \pi^0$ (DP)	0.007 ± 0.007
$K_L \rightarrow \pi^+ \pi^- \pi^0$ (PP)	0.007 ± 0.007
$K_L \rightarrow \pi^\pm \mu^\mp \nu + 2\gamma(\text{Acc})$ (D)	0.161 ± 0.093
$K_L \rightarrow \pi^\pm \mu^\mp \nu + 2\gamma(\text{Acc})$ (P)	0.063 ± 0.037
$K_L \rightarrow \pi^0 \pi^\pm \mu^\mp \nu$ (D)	0.009 ± 0.009
$K_L \rightarrow \pi^0 \pi^\pm \mu^\mp \nu$ (P)	< 0.009
Total	0.87 ± 0.15

Data	Bgd	observed	BR
1997	0.87 ± 0.15	2	$< 3.8 \times 10^{-10}$
1999			
SM prediction			$(1.5 \pm 0.5) \times 10^{-11}$

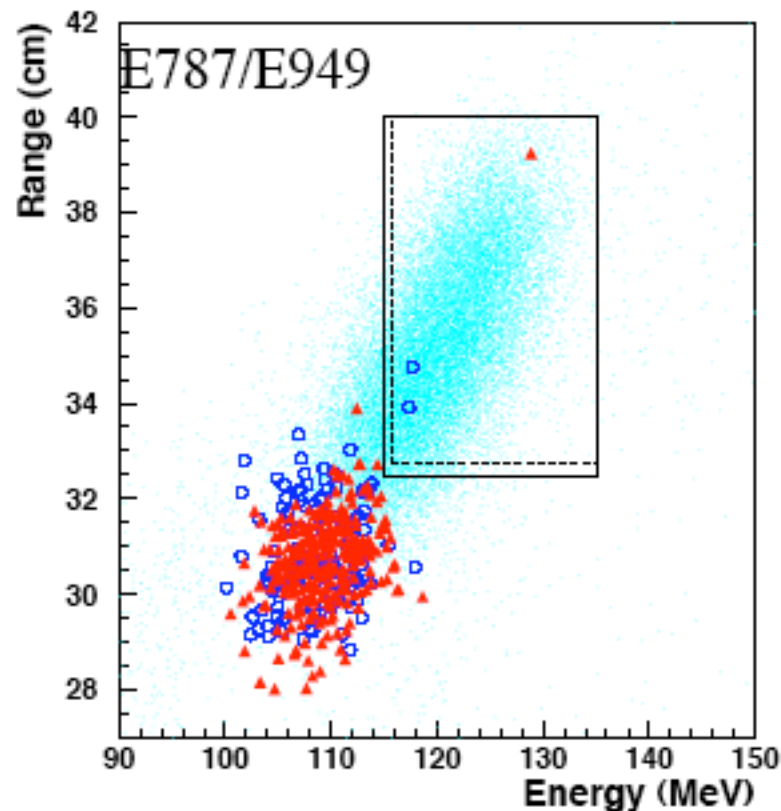
K⁺ → π⁺νν̄ at BNL-E949

- AGS: 22GeV, 70×10¹² protons/spill
- 2.2-sec spill in every 5.4 sec (duty cycle = 41%)
- 0.710 GeV/c, K⁺/π⁺ = 3



Improved Measurement of the $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ Branching Ratio

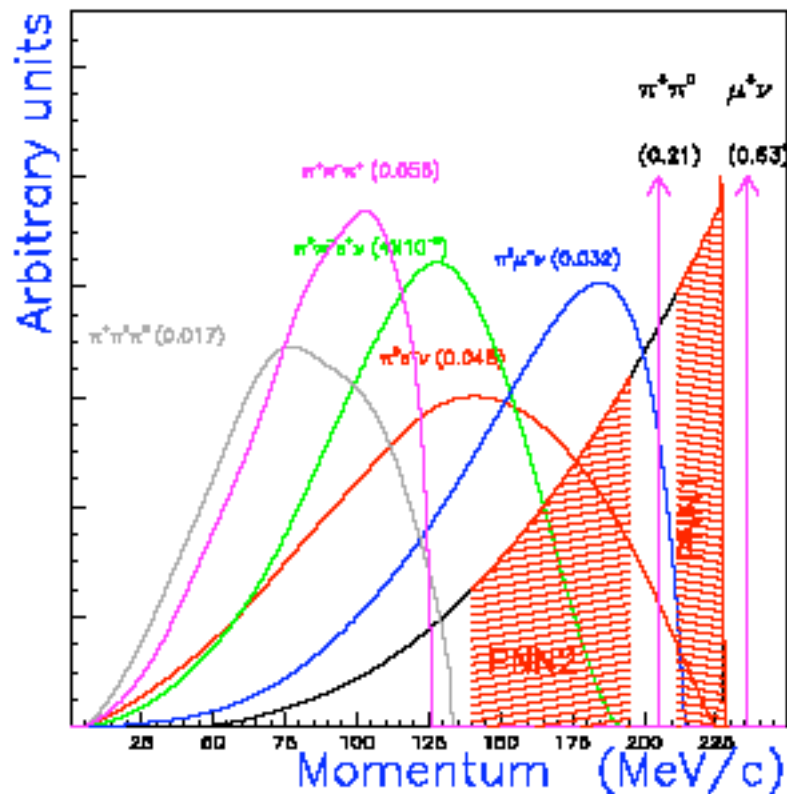
E949 2002 dataset ($\sim 30\%$ of E787), PRL 93 (2004) 031801



- π^+ Range vs Energy
- | | | |
|-----------|------|------------|
| E949-2002 | E787 | MonteCarlo |
|-----------|------|------------|
- background: 0.30 ± 0.03 events
 - “Blind” analysis
 - Likelihood analysis to the candidate events
- $B.R. = \frac{(1.47^{+1.30}_{-0.89}) \times 10^{-10}}{\text{in } 68\% \text{ C.L. intervals}}$
- $P_b = 0.1\%$

E787/E949 events

	PNN1		PNN2	
P_{π} (MeV/c)	[211,229]		[140,195]	
Years	1995-98 (E787)	2002 (E949)	1996-97 (E787)	2002 (E949)
Stopped K^+	5.9×10^{12}	1.8×10^{12}	1.7×10^{12}	1.8×10^{12}
Candidates	2	1	1	S/b = (BR-SES)/b ≈ 0.1 GOAL: ~ 1
Background	0.15 ± 0.05	0.30 ± 0.03	1.22 ± 0.24	
BR($K^+ \rightarrow \pi^+ _$)	$(1.47^{+1.30}_{-0.89}) \times 10^{-10}$ (68% CL)		$< 22 \times 10^{-10}$ (90% CL)	
				?



K⁺ → π⁺νν̄: Letter of Intent for NA48/3 @ CERN

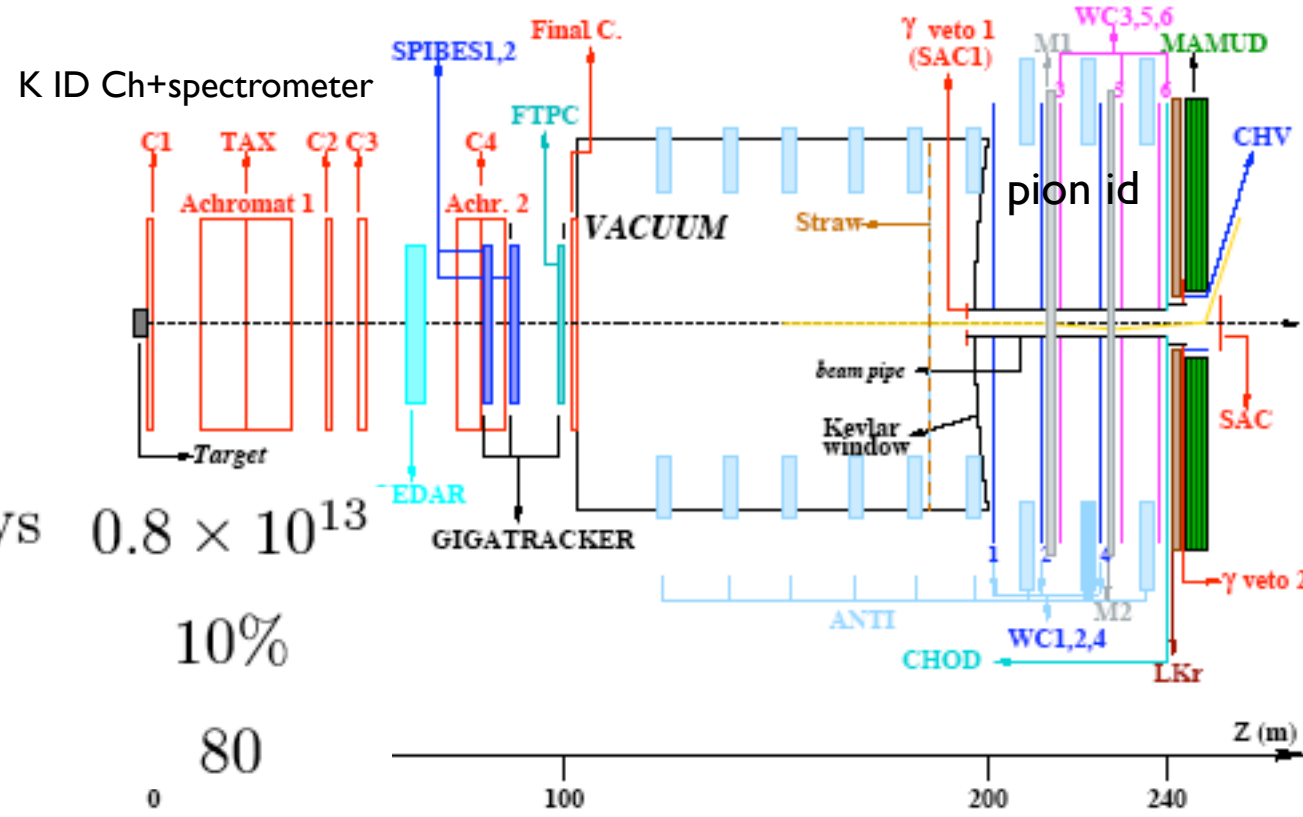
75 GeV

p/π⁺/K⁺ MHz
160/480/48

Sensitive K decays 0.8 × 10¹³

Acceptance 10%

pnn Total 80



- un-separated K⁺ beam at ~75 GeV/c, π⁺νν̄ decay in flight
- testbeam run in August:
rate-capable KAon BEam Spectrometer with Micromegas-type TPC's,

Signal/bkgd 2

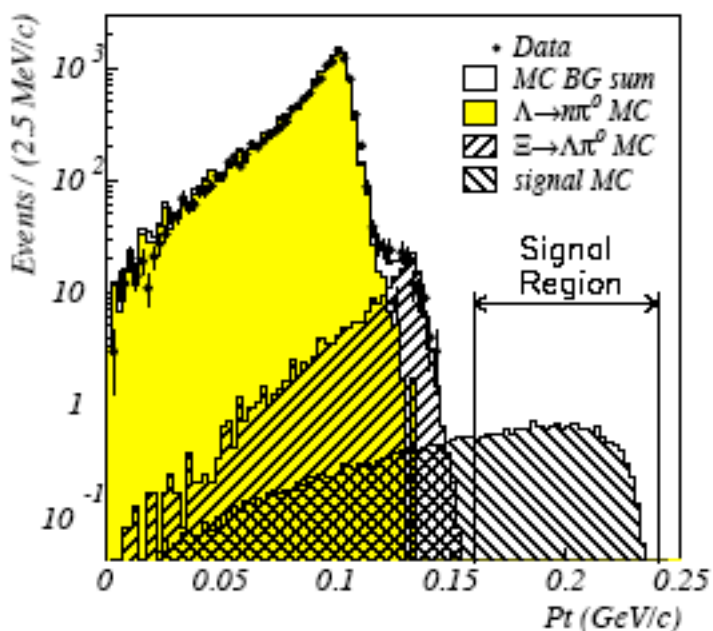
σ(B)/B 14% E787/E949 acc~0.2%

Year 2009

in-flight K_L^0 decay $\rightarrow \pi^0 +$ “nothing”

$[\pi^0 \rightarrow e^+e^-\gamma]$

background $0.12^{+0.05}_{-0.04}$ events

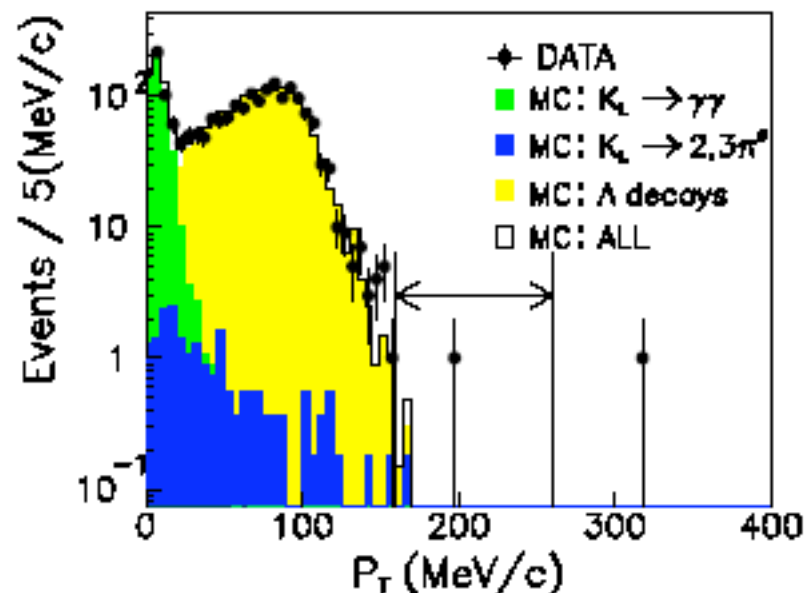


$< 5.9 \times 10^{-7}$

KTEV '97 PRD 61(2000)072006

$[\pi^0 \rightarrow \gamma\gamma] \leftarrow$ We need this !

background 3.5 ± 0.9 events



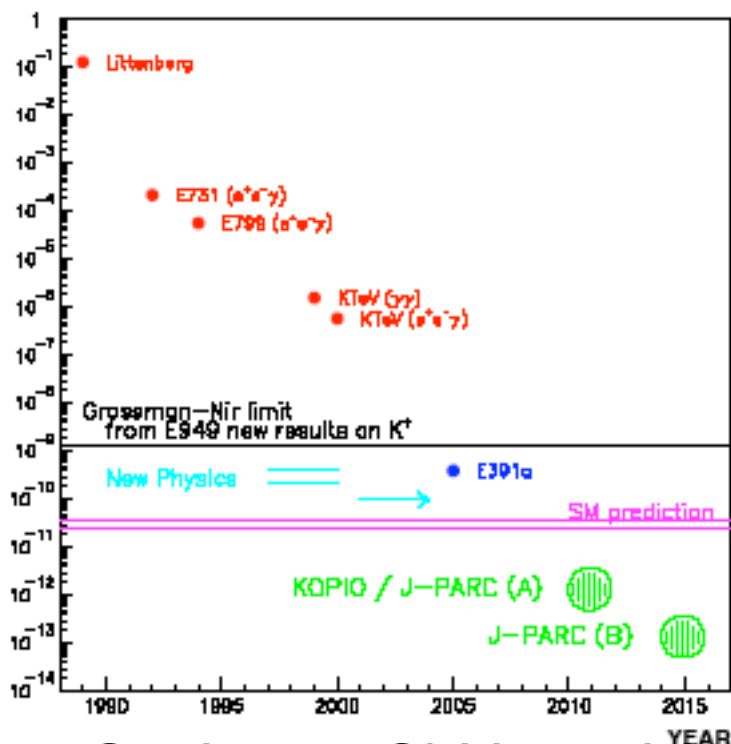
$< 1.6 \times 10^{-6}$

one-day PL B447(1999)240

major background from $K_L \rightarrow \pi^0\pi^0$ (2 out of 4 γ 's escape)

photon detection with very-low inefficiency ($< 10^{-3} \sim 10^{-4}$)

KEK-E391a: the first experiment dedicated to $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$



goal: Get below GN bound for new physics

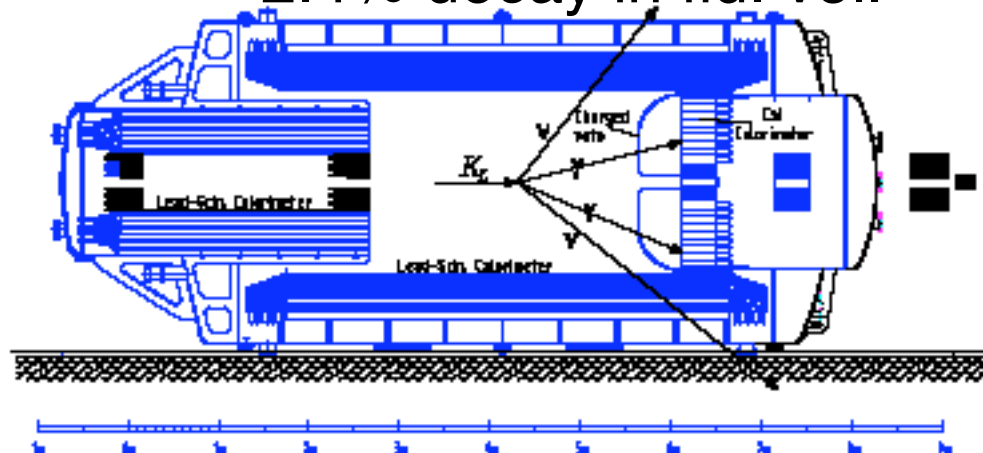
- KEK-PS: 12GeV, 2.5×10^{12} protons/spill
- 2.0-sec spill in every 4.0 sec

Run I 2004 • S.E.S (ratio to $K_L^0 \rightarrow \pi^0 \pi^0 \pi^0$): $\sim 4 \times 10^{-10}$ w/o very tight PV

- collimated "pencil" beam $\pm 2\text{mrad}$
- CsI calorimeter to detect $\pi^0 \rightarrow \gamma\gamma$
 - decay vertex along the beam line (m_{π^0} constraint)
 - the events with $P_T(\pi^0) > 120 \text{ MeV}/c$

- calorimeters for perfect photon veto

$P(k) \sim 2\text{-}3\text{GeV}$, 500k(30M) K(n) per pulse, 2.4% decay in fid. vol.

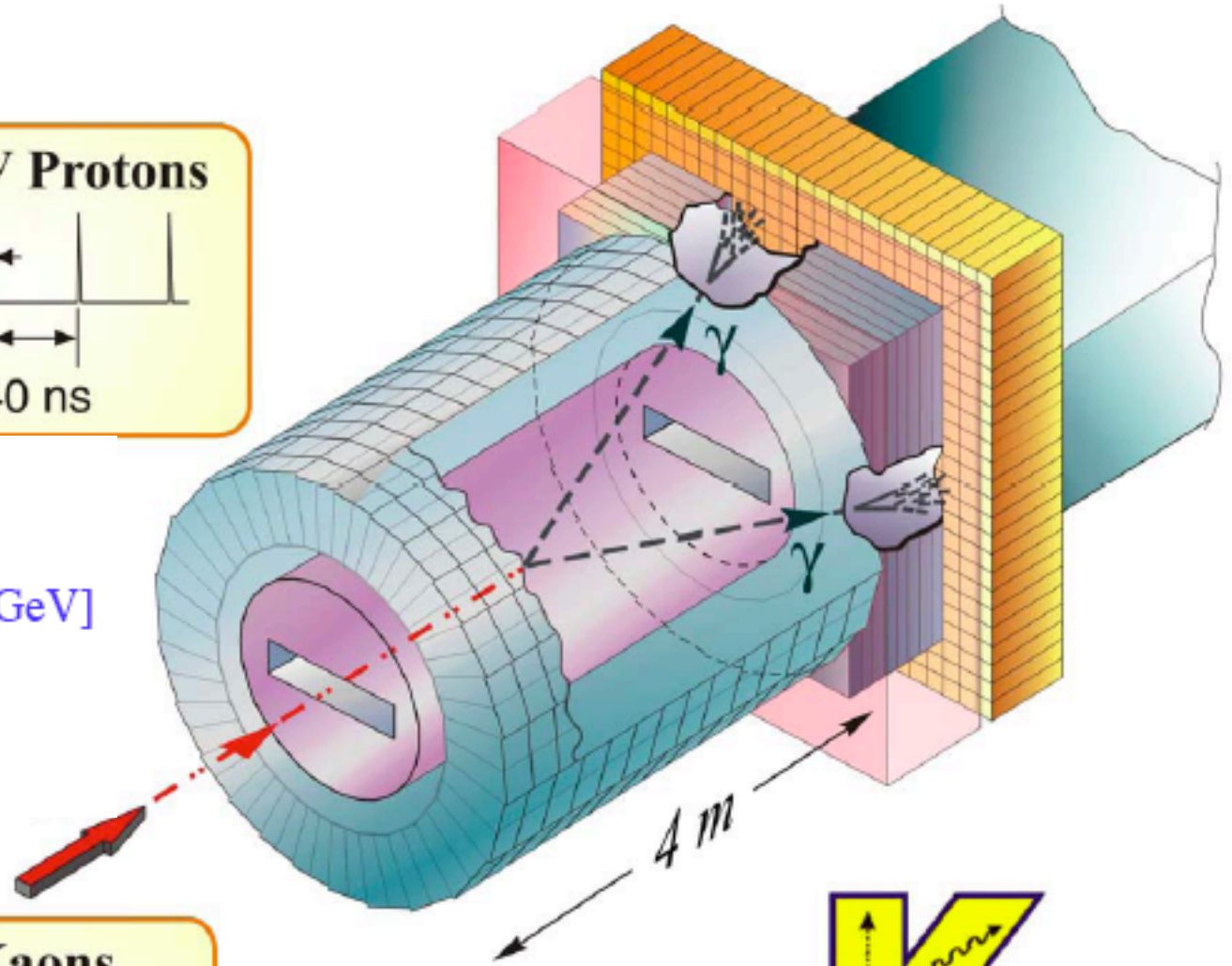
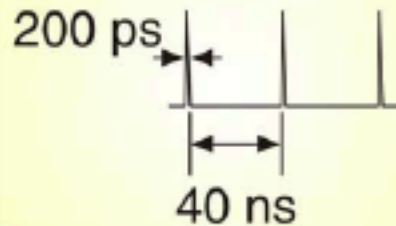


- requesting Run-2 in 2005

KOPIO Concepts

Try to measure everything in K center of mass.

25 GeV Protons



Kaon Beam:

42.5 degree take-off angle

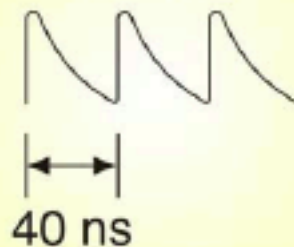
Soft momentum spectrum [0.5, 1.5 GeV]

$3 \times 10^8 K_L$ / spill, 8 % decay

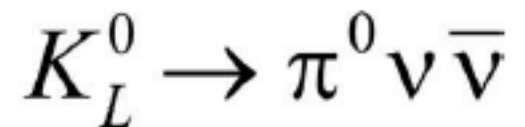
10 GHz neutrons

6000 hrs
~100 Signal
~20 bkg

Kaons



K_{opio}



Conclusions

- Situation with $K_L \rightarrow \pi^0 l^+ l^-$ is getting less murky because of the measurements from NA48 of $K_S \rightarrow \pi^0 l^+ l^-$.

Is it good enough for a dedicated experiment ?

- Theory of $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ ($\sim 10^{-10}$) and $K_L \rightarrow \pi^0 \nu \bar{\nu}$ ($\sim 3 \times 10^{-11}$) is very robust.

New understanding of how $K_L \rightarrow \pi^0 \nu \bar{\nu}$ has sensitivity to new physics. (Bryman, Buras, Isidori, Littenberg, TUM-HEP-583/05)

- JPARC has many LOI for rare decays. 2×10^{14} protons/3.4sec

Pencil beam for $K_L \rightarrow \pi^0 \nu \bar{\nu}$.

Stopping beam for $K^+ \rightarrow \pi^+ \nu \bar{\nu}$.

- $K^+ \rightarrow \pi^+ \nu \bar{\nu}$: NA48/3.

Perhaps incorporate some CKM features: ring imaging, separated beam. Seriously consider lower momentum (PNN2) region

- $K^+ \pi^0 \nu \bar{\nu}$: KOPIO waiting for funding.